# Magnetic order in 2D antiferromagnets revealed by spontaneous anisotropic magnetostriction

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The temperature dependent order parameter provides important information on the nature of magnetism. Using traditional methods to study this parameter in two-dimensional (2D) magnets remains difficult, however, particularly for insulating antiferromagnetic (AF) compounds. Here, we show that its temperature dependence in AF MPS<sub>3</sub> (M(II) = Fe, Co, Ni) can be probed via the anisotropy in the resonance frequency of rectangular membranes, mediated by a combination of anisotropic magnetostriction and spontaneous staggered magnetization. Density functional calculations followed by a derived orbital-resolved magnetic exchange analysis confirm and unravel the microscopic origin of this magnetization inducing anistropic strain. We further show that the temperature and thickness dependent order parameter allows to deduce the material's critical exponents characterising magnetic order. Nanomechanical sensing of magnetic order thus provides a future platform to investigate 2D magnetism down to the single-layer limit.

Layered two-dimensional (2D) magnetic materials offer an emerging platform for fundamental studies of magnetism in the 2D limit. Their stackability into van der Waals heterostructures opens pathways to non-trivial magnetic phases and technological applications, including sensors, memories and spintronic logic devices [1]. In addition to ferromagnetism, first observed in CrI<sub>3</sub> [2] and Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub> [3], antiferromagnetism in 2D materials has also been studied in FePS<sub>3</sub> [4] and CrSBr [5]. Antiferromagnetic (AF) materials are of particular technological interest due to their high spin-wave propagation speed and lack of macroscopic stray fields, making them strong candidates for spintronic and magnonic applications [6– 10].

For insulating, thin AF materials, such as  $MPS_3$  (M(II) = Fe, Co, Ni), few methods are available to study their intrinsic magnetism. Conventional techniques, such as neutron scattering, magnetization measurement by a superconducting quantum interference device (SQUID) or vibrating sample magnetometry are challenging, due to the small volumes of exfoliated 2D materials. Other methods, suited to 2D materials, require electrical conductance, the presence of specific optical modes or ferromagnetic order; they are therefore difficult to apply [1]. In contrast, strain applied to 2D magnetic materials was shown to be extremely powerful, inducing magnetization reversal [11], reorientating the easy-axis [12], or reversing the exchange interaction [13]. In addition, the direct coupling between strain, resonance frequency and magnetization in membranes of 2D magnets, makes nanomechanical resonance a sensitive method for studying their

phase transitions [14–16]. Here, we show, guided by density functional theory (DFT), that the magnetic order parameter of MPS<sub>3</sub> AF membranes can be quantified through the anisotropy in their magneto-elastic response; from its temperature dependence the critical exponents are determined, and their thickness dependence is investigated.

#### **RESULTS AND DISCUSSION**

## First principles analysis of spontaneous magnetostriction in $\mathbf{MPS}_3$

Transition-metal phosphorus trisulphides, with general formula  $MPS_3$ , are layered materials stacked in a monoclinic lattice with symmetry group C2/m [17], as shown in the top view of a single-layer in the paramagnetic phase, Fig. 1a, top panel. The spins of  $FePS_3$  point outof-plane, whereas both  $CoPS_3$  and  $NiPS_3$  are in-plane systems with their spins preferentially aligned along the a axis. The intralayer AF order forms a zigzag configuration, as shown in bottom panel of Fig. 1a, leading to two opposite aligned magnetic sub-latices. The difference of the magnetisation between these sub-latices is the Néel vector. In bulk CoPS<sub>3</sub> and NiPS<sub>3</sub>, these layers with this staggered magnetism are stacked in a ferromagnetic (FM) fashion with Néel transition temperatures,  $T_{\rm N}$ , around 119 and 155 K, respectively [18, 19]. The interlayer magnetic interactions in  $FePS_3$  are AF with a transition around 118 K [20].

To analyse the effect of magnetic ordering on the lattice, we performed first principles structural optimiza-

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FIG. 1. Magnetostriction in MPS<sub>3</sub> membranes. a, top panel, Crystalline structure of MPS<sub>3</sub> in the paramagnetic phase  $(T > T_N)$ . Black hexagons indicate the organisation of magnetic atoms in the lattice. a, bottom panel, Crystalline structure of MPS<sub>3</sub> at the AF phase  $(T < T_N)$  as it elongates in the *b* and contracts in the *a* direction. Light blue and red arrows indicate the axial lattice distortion. b, Illustration of the exchange interaction parameters included into the Heisenberg spin Hamiltonian. c-d, Calculated maximally localized Wannier orbitals. Green arrows illustrate the most relevant FM superexchange channels for J<sub>1</sub> (J<sub>1</sub><sup>'</sup>) (c) and J<sub>2</sub> (d), corresponding with the d<sub>yz</sub>-d<sub>yz</sub> (d<sub>xz</sub>-d<sub>xz</sub>) and d<sub>xy</sub>-d<sub>xy</sub> orbitals, respectively. e-f, Electron configuration of the Fe<sup>2+</sup> magnetic ions connected by J<sub>1</sub> (e) and J<sub>2</sub> (f), showing parallel and antiparallel spin orientations, respectively.

tions of FePS<sub>3</sub>, CoPS<sub>3</sub> and NiPS<sub>3</sub> based on density functional theory (DFT). For the ground state zigzag magnetic configuration, the calculations predict a compression of the *a* lattice parameter with respect to the crystallographic, non-magnetic structure of 2.545% and 1.328% for the Co and Fe derivatives respectively (see Table 1). In addition, the *b* axis expands by 0.402% (Co) and 0.359% (Fe). In contrast, in NiPS<sub>3</sub> the lattice parameters remain almost unchanged. The crystal and magnetic structures are strongly connected in these compounds, which is further corroborated by simulations of different spin configurations (see Supplementary Note 1).

The microscopic mechanism governing the spontaneous magnetostriction in these materials is studied using orbital-resolved magnetic exchange analyses based on maximally localized Wannier functions, (see Supplementary Note 1). The analysis shows that the spontaneous magnetostriction calculated in  $FePS_3$  and  $CoPS_3$  arises from isotropic magnetic exchange interactions between  $t_{2q}-t_{2q}$  orbitals. Specifically, for FePS<sub>3</sub> the main magnetic exchange channels, substantially affected by the compression of the a and expansion of the b lattice parameters, are the ones involving  $t_{2q}-t_{2q}$  interactions of FM nature. The changes in the lattice parameters result in an increase in  $J_1$  and  $J'_1$  due to a decrease in distance between the  $d_{yz}$ - $d_{yz}$  and  $d_{xz}$ - $d_{xz}$  orbitals, respectively (Fig. 1c). Simultaneously, these changes cause a decrease of  $J_2$  due to a larger separation of the  $d_{xy}$ - $d_{xy}$  orbitals (Fig. 1d). This is compatible with the electron configuration of  $Fe^{2+}$  (d<sup>6</sup>), which has these orbitals partially filled and allows FM hopping between them (Fig. 1e,f).

This hopping effect also occurs for  $\operatorname{Co}^{2+}(d^7)$  although the additional electron present for Co blocks the  $d_{xy}$  $d_{xy}$  pathway (Supplementary Note 1, Fig. S2). This results in a stronger effect along  $J_1$  and  $J'_1$  for the optimized structure, maximizing FM interactions in the zigzag chain, which involve the  $d_{yz}$ - $d_{yz}$  and  $d_{xz}$ - $d_{xz}$  orbitals, respectively. For the Ni<sup>2+</sup> derivative (d<sup>8</sup>), the  $t_{2g}$ energy levels are fully occupied (Supplementary Note 1, Fig. S3), which results in a blocking of the  $t_{2g}$ - $t_{2g}$  magnetic super-exchange channels. This leads to an almost negligible modification in the lattice parameters of the optimized structure with respect to the crystallographic non-magnetic one.

### Resonance frequency changes due to spontaneous magnetostrictive strain

The predicted anisotropic change of lattice parameters when going from the paramagnetic to the AF phase, causes compressive stress,  $\sigma_{\rm a}$ , and tensile stress,  $\sigma_{\rm b}$ , along the *a* axis and *b* axis respectively, as illustrated in Fig. 1a, bottom pannel. To quantify this anisotropy appearing at the phase transition, we use rectangular membranes, shown in Fig. 2b, to nanomechanically probe stress variations, along a specific crystallographic axis [21] (see Supplementary Note 2). In the following analysis, we neglect

TABLE 1. CoPS<sub>3</sub>, FePS<sub>3</sub> and NiPS<sub>3</sub> lattice parameters of the crystallographic non-magnetic (NM) and fully optimized zigzag antiferromagnetic (AF-zigzag) configurations, as calculated by DFT (see Supplementary Note 1).

	$\mathbf{CoPS}_3$		$\mathbf{FePS}_3$		$\mathbf{NiPS}_3$	
Lattice parameter (Å)	a	b	a	b	a	b
$\mathbf{N}\mathbf{M}$	5.895	10.19	5.947	10.301	5.812	10.07
AF-zigzag	5.745	10.231	5.868	10.338	5.817	10.061
Change (%)	-2.545	+0.402	-1.328	+0.359	+0.086	-0.089

the stress contribution from the thermal expansion of the substrate, as this is small compared to that of the  $MPS_3$  compounds [14].

The resonance frequency of the fundamental mode of a rectangular membrane,  $f_{\text{res}}$ , is approximately given by [22]:

$$f_{\rm res} \approx \frac{1}{2} \sqrt{\frac{1}{\rho}} \left[ \frac{1}{w^2} \sigma_{\rm w} + \frac{1}{l^2} \sigma_{\rm l} \right],$$
 (1)

where  $\rho$  is the mass density, w and l are respectively the width and length of the membrane, as indicated in Fig. 2b, and  $\sigma_{w,l}$  are the stresses parallel to these directions. For high-aspect-ratio membranes ( $w \ll l$ ), the mechanical resonance frequency is mostly determined by the stress along the shortest direction,  $\sigma_w$ .

We study the resonance frequency of thin MPS<sub>3</sub> flakes suspended over star-shaped cavities with 30° angular resolution, as shown in an example device in Fig. 2b. When the longest side of the cavity is aligned along a crystallographic axis (*a* or *b*) and  $w \ll l$ , its fundamental resonance frequency ( $f_a$  or  $f_b$ ) is determined by the stress along the perpendicular axis ( $\sigma_b$  or  $\sigma_a$ ):

$$f_{\rm a} \approx \frac{1}{2} \sqrt{\frac{1}{\rho w^2} \sigma_{\rm b}} \text{ and } f_{\rm b} \approx \frac{1}{2} \sqrt{\frac{1}{\rho w^2} \sigma_{\rm a}} \,.$$
 (2)

On cavities oriented at an intermediate angle,  $\theta$ , (defined with respect to the *b* axis), the resonance frequency is:

$$f_{\theta}(T) \approx \frac{1}{2} \sqrt{\frac{1}{\rho w^2} \left[ \sigma_{\mathrm{a},\theta} + \sigma_{\mathrm{b},\theta} \right]}, \qquad (3)$$
$$\sigma_{\mathrm{a},\theta} = \frac{E}{(1-\nu^2)} (\cos^2 \theta + \nu \sin^2 \theta) (\bar{\epsilon} - \epsilon_{\mathrm{ms,a}}),$$
$$\sigma_{\mathrm{b},\theta} = \frac{E}{(1-\nu^2)} (\sin^2 \theta + \nu \cos^2 \theta) (\bar{\epsilon} - \epsilon_{\mathrm{ms,b}}),$$

where we have used the constitutive equations for a magnetostrictive membrane with plane stress [23], while only keeping the anisotropy in the magnetostriction coefficient, Supplementary Note 2. Here, E is the Young's modulus and  $\nu$  is Poisson's ratio of the material. Moreover, we have  $\bar{\epsilon} = \epsilon_{\rm fab} - \epsilon_{\rm th}$ , with  $\epsilon_{\rm fab}$  the residual fabrication strain and  $\epsilon_{\rm th}$  the phononic thermal expansion induced strain variation. The magnetostrictive strain along the a and b-axes is given by  $\epsilon_{\rm ms,a,b} = \lambda_{\rm a,b}L^2$ , respectively (see Supplementary Note 3 for a detailed derivation of Eq. (3)), where  $\lambda_{a,b}$  are magnetostriction coefficients and  $L^2$  is the AF order parameter squared.

The temperature dependence of the resonance frequency comprises two contributions: one due to the phononic thermal expansion coefficient  $\alpha$ , given by  $\epsilon_{\rm th}(T) = \int_{T_0}^T \alpha(\tilde{T}) d\tilde{T}$ , where  $T_0$  is a reference temperature and  $\tilde{T}$  the integration variable, and the magnetostrictive contribution  $\epsilon_{{\rm ms},{\rm a},{\rm b}}(T) = \lambda_{{\rm a},{\rm b}}L^2(T)$ . The former contribution is a slowly varying function of T, while the latter term contains the staggered magnetization, which increases abruptly near the phase transition; it thus can be used to determine L(T), as we will show below. We assume  $\lambda_{{\rm a},{\rm b}}$  to be T independent, as its temperature dependence will be negligible when compared to that of L(T).

#### Nanomechanical determination of the order parameter

To quantify the anisotropy in the magnetic membranes, a laser interferometry technique is used to measure their resonance frequency as a function of temperature [24]. A MPS<sub>3</sub> flake, suspended over holes in a patterned Si/SiO<sub>2</sub> chip, Fig. 2b, is placed inside a cryostat with optical access as shown in Fig. 2a. Both actuation and detection are done optically, by means of a powermodulated blue laser which opto-thermally excites the fundamental resonance, and a constant red laser which measures the change in the reflected signal resulting from the membrane's motion [14]. A typical resonance is shown in Fig. 2c, along with the damped harmonic oscillator model fit defining the resonance frequency. Figure 2d shows that in  $\text{CoPS}_3$   $f_a$  and  $f_b$  exhibit a similar temperature dependence for  $T > T_N$ , while opposite behaviour below the phase transition is visible, namely an increase of  $f_{\rm a}$  and a relative decrease of  $f_{\rm b}$ . This sudden change in f(T) for the perpendicular cavities, occurring near  $T_{\rm N}$ , constitutes, in accordance with the DFT calculations, the central result of this work as it shows that the magnetic ordering in MPS<sub>3</sub> leads to anisotropic strain and thus spontaneous magnetostriction. We further note that strictly speaking,  $T_{\rm N}$  should be replaced by  $T_{\rm N}^*$  which includes the effects of strain (see Supplementary Note 2). For simplicity, we here use the notation  $T_{\rm N}$  for the measured transition temperatures.



FIG. 2. Angle-resolved mechanical characterization via laser interferometry. a, Schematic illustration of the laser interferometry setup and sample with rectangular cavity array. b, Optical image of the rectangular membranes array for a CoPS<sub>3</sub> sample. The *a* and *b* axis are determined from the resonance frequency behaviour. Scale bar:  $12 \mu m$ . Schematic of 0° and 90° membranes from the array where *w* is the width of the membrane and *l* its length. c, Measured amplitude of the fundamental resonance peak in a CoPS<sub>3</sub> drum at T = 10 K and Lorentzian fit used to extract the fundamental resonance frequency,  $f_{\rm res}$ , and quality factor, *Q*. d, Temperature dependence of  $f_{\rm res}$  of a CoPS<sub>3</sub> rectangular membrane orientated along the *a* and *b* axes. The dashed line indicates the transition temperature  $T_{\rm N}$  extracted from the data. e, Resonance frequency difference,  $f_{\rm res}(T) - f_{\rm res}(140 \, {\rm K})$ , as a function of angle and temperature. The dashed line indicates the transition as in d f, Polar plot of  $f_{\rm res}(T) - f_{\rm res}(140 \, {\rm K})$  taken along the red dashed line in (e). Panels g-i, follow the same structure as (c-e) for NiPS<sub>3</sub> resonators with negligible anisotropy, measured between 5 K and 190 K.

The anisotropic behavior of CoPS<sub>3</sub> in the AF state is even more evident in Fig. 2e, where  $f_{\rm res}(T) - f_{\rm res}(140 \text{ K})$ for the different cavities of the star-shaped sample are plotted as a function of  $\theta$  and temperature. The polar plot in Fig. 2f shows the data along the red dashed line at T = 70 K in Fig. 2e and results in a characteristic dumbbell-shape. Similar anisotropic behaviour is observed in FePS<sub>3</sub> as shown in Supplementary Note 4. On the contrary, for NiPS<sub>3</sub> negligible anisotropy is observed in the angle-resolved magnetostriction data in Fig. 2g-i.

To obtain L(T) from the data, we first subtract the pretension contribution from the resonance frequency  $f_{\theta}(T_0)$ 



FIG. 3. Anisotropy and critical behaviour in resonance frequency of MPS<sub>3</sub> (M(II) = Co, Fe, Ni) membranes. a, Pretension corrected resonance frequency ( $\tilde{f}_{a}^{2}(T) = f_{a}^{2}(T) - f_{a}^{2}(150\text{K})$  and  $\tilde{f}_{b}^{2}(T) = f_{b}^{2}(T) - f_{b}^{2}(150\text{K})$ ) of rectangular membranes of CoPS<sub>3</sub> oriented along the *b* axis (blue) and *a* axis (red) **b**, Difference of the corrected frequency squared  $\tilde{f}_{b}^{2} - \tilde{f}_{a}^{2}$  proportional to the order parameter  $L^{2}$  from Eq. 4. The dashed-dotted line indicates the measured transition temperature  $T_{N}$ . The dashed black line is a powerlaw fit through the data close to  $T_{N}$  (see Supplementary Note 6). **c**, Difference of the corrected frequency squared  $\tilde{f}_{b}^{2} - \tilde{f}_{a}^{2}$  as a function of the reduced temperature  $1 - T/T_{N}$ . The dashed black line is the fit from b where the slope defines the critical exponent  $2\beta$ . **d-f**, and **g-i**, follow the same structure as (a-d) for FePS<sub>3</sub> and NiPS<sub>3</sub> resonators, respectively.

by calculating  $\tilde{f}_{\theta}^2(T) = f_{\theta}^2(T) - f_{\theta}^2(T_0)$ , for each angle, where  $T_0 = 150$  K is the highest temperature in our measurements. The resulting values of  $\tilde{f}_{\theta}^2(T)$  along the crystalline axes a and b are shown in Fig. 3a,d,g for the three MPS<sub>3</sub> compounds. With Eq. (3), we then calculate the difference  $\tilde{f}_{b}^2(T) - \tilde{f}_{a}^2(T)$  which yields

$$\tilde{f}_{\rm b}^2 - \tilde{f}_{\rm a}^2 = \frac{E}{4\rho w^2 (1+\nu)} \left[\lambda_{\rm a} - \lambda_{\rm b}\right] L^2.$$
 (4)

We can now use Eq. (4) to access the critical behaviour of L below  $T_{\rm N}$  by plotting  $\tilde{f}_{\rm b}^2 - \tilde{f}_{\rm a}^2$  as a function of temperature. As shown in Fig. 3b,e,h, the trend presents the typical critical behaviour with a non-zero order parameter appearing in the ordered state for  $T < T_{\rm N}$ . Figures 3c,f,i show the same critical curve as Fig. 3b,e,h respectively, plotted on a logarithmic scale against the reduced temperature  $(1 - T/T_{\rm N})$ . Note that the difference  $\tilde{f}_{\rm b}^2 - \tilde{f}_{\rm a}^2$  for NiPS<sub>3</sub>, is substantially smaller than that of the  ${\rm Fe}/{
m CoPS_3}$  membranes indicative of a weaker anisotropic magnetostrictive behaviour.

The angle dependence of the resonance frequencies allows us to estimate the ratio  $r_{\rm ab} = \lambda_{\rm a}/\lambda_{\rm b}$  between the magnetostriction parameters,  $\lambda_{\rm a,b}$ , (see Supplementary Note 3). This ratio we directly compare to DFT calculations: Experimentally, we find for FePS<sub>3</sub>,  $r_{\rm ab} =$  $-2.3 \pm 0.3$  while from the DFT calculations we estimate  $r_{\rm ab} = -3.70$ . For CoPS<sub>3</sub> (taking [25]  $\nu_{\rm CoPS_3} = 0.293$ ), the experimental value is  $-1.42 \pm 0.07$  and the DFT one -6.33. We conclude that although both the sign and order of magnitude of the magnetostrictive anisotropy in these compounds are well reproduced in the current work, more detailed studies will be needed to obtain full quantitative correspondence with theory.

#### Thickness dependence of critical behaviour

As follows from Landau's theory of phase transitions (see Supplementary Note 2), L(T) near  $T_N$  is given by

$$L^{2}(T) = \begin{cases} 0 & \text{if } T > T_{\rm N} \\ \frac{A}{2B} (T_{\rm N} - T)^{2\beta} & \text{if } T < T_{\rm N}, \end{cases}$$
(5)

where A and B are constants and  $\beta$  is a critical exponent representative of the magnetic order. We fit Eq. (5) to the data in Fig. 3b,e,h in the region close to  $T_{\rm N}$  (indicated by the black dashed line in Fig. 3b,e,h) to extract the critical exponent  $\beta$  and  $T_{\rm N}$  for the three materials (see Supplementary Note 6 for more details on the fitting procedure). In the logarithmic plot of the critical curve the fitting of a straight line shows good agreement to the data points, consistent with the result of Eq. (5). The values for  $\beta$  and  $T_{\rm N}$  are plotted in Fig. 4 as a function of thickness, t, and listed in Supplementary Note 6, Table 49.

For the weakly anisotropic NiPS<sub>3</sub>,  $\beta = 0.218 \pm 0.016$ , comparable to the value ( $\beta = 0.22 \pm 0.02$ ) found in Ref. [27], and consistent with the expected 2D XY magnetic dimensionality ( $\beta_{2DXY} = 0.233$ ) of NiPS<sub>3</sub> [28]. For FePS<sub>3</sub> we find  $\beta = 0.208 \pm 0.033$ , comparable with literature values [29]. For both  $\beta$  and  $T_N$  no appreciable thickness dependence is observed, similar to what has previously been reported in Ref. [30], where changes in the critical behaviour mostly become visible in the monolayer limit.

For thicker CoPS<sub>3</sub> samples (t = 40 - 60 nm) we find  $\beta = 0.289 \pm 0.034$  close to what is reported in literature for the bulk ( $\beta_{\text{bulk}} = 0.3 \pm 0.01$  [18]) and consistent with the 3D Ising model. For samples with t < 10 nm the measured  $\beta$ , on the other hand, is  $0.195 \pm 0.045$ , closer to  $\beta_{2\text{DXY}}$  as shown in the top panel of Fig. 4. This constitutes a noticeable change in  $\beta$  while going from bulk to thinner samples. Similarly, we observe for CoPS<sub>3</sub> a decrease in  $T_{\text{N}}$  from the bulk value of 118 K down to  $\sim 100$  K, similar to what was previously reported in Ref. [26]. We fit a power law to the dependence of  $T_{\text{N}}$  on



FIG. 4. Thickness dependence of critical behaviour. Average critical exponent,  $\beta$ , and critical temperature,  $T_{\rm N}$ , of MPS<sub>3</sub> resonators plotted as a function of thickness. The blue stars indicate CoPS<sub>3</sub> bulk values from [26]. Critical parameters have been determined from power law fits to  $\tilde{f}_{\rm b}^2 - \tilde{f}_{\theta}^2$ , as shown in Fig. 3b,e,h, and then taking the average value over the fit parameter for all angles  $\theta \neq 0$ . Error bars are calculated from standard deviation of fit results for all  $\theta$ . The horizontal gray dashed lines in the upper plot indicate the expected values of  $\beta$  for the 3D or 2D versions of the Heisenberg (H), XY or Ising (Is) models. The blue dashed line in the lowe panel indicates a fit to Eq. (6) through the CoPS<sub>3</sub> data with  $\nu_{\rm eff} = 0.84 \pm 0.13$ .

thickness,

$$T_{\rm N}(t)/T_{\rm N}^{\rm 3D} \propto 1 - (C/t)^{1/\nu_{\rm eff}},$$
 (6)

where C is a non-universal constant related to the interlayer coupling, and  $\nu_{\rm eff}$  is an effective critical exponent related to the correlation length [31]. Fitting the CoPS<sub>3</sub> data points with  $T_{\rm N}^{\rm 3D} = 118$  K [26] yields  $C = 1.43 \pm 0.457$  nm and  $\nu_{\rm eff} = 0.84 \pm 0.096$ . This value of  $\nu_{\rm eff}$  is intermediate between the expected values of  $\nu_{\rm eff} = 0.630$  for the 3D Ising and  $\nu_{\rm eff} = 1$  for the 2D Ising models, and indicative of a transition regime [32].

#### CONCLUSIONS

In conclusion, we provide a comprehensive analysis of the anisotropic magnetostriction effect in  $MPS_3$  compounds and its implications to the dynamics of membrane made from them. DFT calculations provide a microscopic explanation for the anisotropic lattice deformation in CoPS<sub>3</sub>, FePS<sub>3</sub> and NiPS<sub>3</sub> which are consistent with our measurements. We further demonstrate the relation between magnetic ordering and anisotropy in the mechanical resonance frequency of suspended  $MPS_3$  resonators, providing a direct measure of the AF order parameter in absence of an external magnetic field. We observe a thickness dependence in the critical behaviour of  $CoPS_3$  resonators [18, 26], which is absent in the case of FePS<sub>3</sub>. The presented technique is of particular interest for the study of 2D magnetism given the scarcity of methods available to investigate critical phenomena of van der Waals materials in the atomically thin limit.

#### METHODS

Sample fabrication. Substrates consist of thermal  $SiO_2$  of 285 nm thickness, grown on highly doped  $(Si^{++})$  silicon. The rectangular cavities are defined via e-beam lithography using AR-P 6200 resist. After development, the exposed  $SiO_2$  areas are fully etched via reactive ion etching. The AR-P 6200 resist is stripped in PRS-3000 and the sample is cleaned in an  $O_2$  plasma before stamping. The exfoliation and transfer of multi-layer MPS<sub>3</sub> flakes is done using a polydimethylsiloxaan (PDMS) transfer method. First, MPS<sub>3</sub> crystals are exfoliated onto the PDMS through scotch tape. Selected flakes are then transferred on the star-shaped cavities in the  $SiO_2/Si$  substrate.

Laser interferometry. Samples are mounted on a heater stage which is cooled down to 4 K using a Montana Instruments Cryostation s50 cryostat with optical access. A blue diode laser ( $\lambda = 405$  nm) is used to excite the membrane optothermally via AC powermodulation from a vector network analyzer (VNA) [33]. Displacements are detected by focusing a red He-Ne laser beam ( $\lambda = 632$  nm) on the cavity formed by the membrane and Si substrate. The reflected light, which is modulated by the position-dependent membrane motion, is recorded by a photodiode and processed by a phase-sensitive VNA. Laser spot size is ~ 1  $\mu$ m.

**DFT calculations.** First principles spin-polarized DFT calculations in the plane wave formalism are preformed as implemented in the Quantum ESPRESSO package [34]. The exchange-correlation energy is calculated using the generalized gradient approximation using the Perdew–Burke–Ernzerhof functional [35] and standard Ultra-soft (USPP) solid-state pseudopotentials. The electronic wave functions are expanded with

well-converged kinetic energy cut-offs for the wave functions (charge density) of 75 (800), 85 (800) and 85 (800) Ry for Fe, Co and Ni, respectively. The crystal structures are fully optimized using the Broyden-Fletcher-Goldfarb-Shanno (BFGS) algorithm [36] until the forces on each atom are smaller than  $1 \times 10^{-3}$  Ry/au and the energy difference between two consecutive relaxation steps is less than  $1 \times 10^{-4}$  Ry. In order to avoid unphysical interactions between images along the non-periodic direction, we add a vacuum of 18 Å in the z direction for the monolayer calculations. The Brillouin zone is sampled by a fine  $\Gamma$ -centered  $5 \times 5 \times 1$  k-point Monkhorst–Pack [37]. A tight-binding Hamiltonian derived from first-principles is constructed in the base of Maximally-localized Wannier functions, as implemented in the Wannier90 code [38]. For that, we select the d orbitals of the metal centre (Fe, Co, Ni) and the s and p orbitals of P and S to construct the connected subspace. Magnetic interactions are determined using the Green's function method in the TB2J software [39]. The orbital resolved analysis is performed after rotating the coordinate system of the crystal to align the metal-sulfur bonds direction of the octahedra with the cartesian axes.

**Crystal growth** Crystal growth of  $MPS_3$  (M(II) = Ni, Fe, Co) is performed following a solid-state reaction inside a sealed evacuated quartz tube (pressure  $\sim 5 \times 10^{-5}$  mbar). I<sub>2</sub> was used as a transport agent to obtain large crystals. A three-zone furnace is used, where a tube with the material was placed in the leftmost zone. This side is then heated up to 700 °C in 3 hours so that a temperature gradient of 700/650/675 °C is established. The other two zones are heated up in 24 hours from room temperature to 650  $^{\circ}\mathrm{C}$  and kept at that temperature for one day. The temperature is kept constant for 28 days and cooled down naturally. With this process crystals with a length up to several centimeters are obtained. Detailed description of the crystal growth and characterization can be found in earlier work [14].

#### Data availability

All data supporting the findings of this article and its Supplementary Information will be made available upon request to the authors.

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#### Author contributions

D.L.E., A.M.R. performed the DFT and orbital resolved tight-binding calculations, supervised by J.J.B. M.Š., M.J.A.H. and G.B. performed the laser interferometry measurements and fabricated and inspected the samples. M.L. and M.J.A.H. fabricated the substrates. S.M.-V., C.B.-C. and E.C. synthesized and characterized the FePS<sub>3</sub>, CoPS<sub>3</sub> and NiPS<sub>3</sub> crystals, supervised by E.c. M.Š., M.J.A.H. and G.B. analysed the experimental data. M.Š., M.J.A.H., Y.M.B., and P.G.S. modeled the experimental data. H.S.J.v.d.Z. and P.G.S. supervised the project. The paper was jointly written by all authors with a main contribution from M.J.A.H. All authors discussed the results and commented on the paper.

#### **Competing interests**

The authors declare no competing interests.

- Mak, K. F., Shan, J. & Ralph, D. C. Probing and controlling magnetic states in 2D layered magnetic materials. *Nat. Rev. Phys.* 1, 646–661 (2019).
- [2] Huang, B. et al. Layer-dependent ferromagnetism in a van der Waals crystal down to the monolayer limit. Nature 546, 270–273 (2017).
- [3] Gong, C. et al. Discovery of intrinsic ferromagnetism in two-dimensional van der Waals crystals. Nature 546, 265–269 (2017).
- [4] Lee, J.-U. et al. Ising-type magnetic ordering in atomically thin FePS<sub>3</sub>. Nano Lett. 16, 7433–7438 (2016).
- [5] Telford, E. J. et al. Layered antiferromagnetism induces large negative magnetoresistance in the van der Waals semiconductor CrSBr. Adv. Mater. 32, 2003240 (2020).
- [6] Němec, P., Fiebig, M., Kampfrath, T. & Kimel, A. V. Antiferromagnetic opto-spintronics. *Nat. Phys.* 14, 229– 241 (2018).
- [7] Rahman, S., Torres, J. F., Khan, A. R. & Lu, Y. Recent developments in van der Waals antiferromagnetic 2D materials: Synthesis, characterization, and device implementation. ACS Nano 15, 17175–17213 (2021).
- [8] Mertens, F. et al. Ultrafast coherent THz lattice dynamics coupled to spins in the van der Waals antiferromagnet FePS<sub>3</sub>. Adv. Mater. 2208355 (2022).
- [9] Boix-Constant, C. et al. Probing the spin dimensionality in single-layer CrSBr van der Waals heterostructures by magneto-transport measurements. Adv. Mater. 34, 2204940 (2022).
- [10] Esteras, D. L., Rybakov, A., Ruiz, A. M. & Baldoví, J. J. Magnon straintronics in the 2D van der Waals ferromagnet CrSBr from first-principles. *Nano Lett.* 22, 8771–8778 (2022).
- [11] Wang, Y. et al. Strain-sensitive magnetization reversal of a van der Waals magnet. Adv. Mater. 32, 2004533 (2020).
- [12] Ni, Z. et al. Imaging the Néel vector switching in the monolayer antiferromagnet MnPSe<sub>3</sub> with straincontrolled Ising order. Nat. Nanotechnol. 16, 782–787 (2021).
- [13] Cenker, J. et al. Reversible strain-induced magnetic phase transition in a van der Waals magnet. Nat. Nan-

otechnol. 1-6 (2022).

- [14] Šiškins, M. et al. Magnetic and electronic phase transitions probed by nanomechanical resonators. Nat. Commun. 11, 2698 (2020).
- [15] Šiškins, M. et al. Nanomechanical probing and strain tuning of the Curie temperature in suspended Cr<sub>2</sub>Ge<sub>2</sub>Te<sub>6</sub>based heterostructures. npj 2D Mater. Appl. 6, 41 (2022).
- [16] Jiang, S., Xie, H., Shan, J. & Mak, K. F. Exchange magnetostriction in two-dimensional antiferromagnets. *Nat. Mater.* 19, 1295–1299 (2020).
- [17] Chittari, B. L. *et al.* Electronic and magnetic properties of single-layer MPX<sub>3</sub> metal phosphorous trichalcogenides. *Phys. Rev. B* 94 (2016).
- [18] Wildes, A. R., Simonet, V., Ressouche, E., Ballou, R. & McIntyre, G. J. The magnetic properties and structure of the quasi-two-dimensional antiferromagnet CoPS<sub>3</sub>. J. Phys. Condens. Matter. **29**, 455801 (2017).
- [19] Joy, P. A. & Vasudevan, S. Magnetism in the layered transition-metal thiophosphates MPS<sub>3</sub> (M=Mn, Fe, and Ni). *Phys. Rev. B* 46, 5425–5433 (1992).
- [20] Takano, Y. et al. Magnetic properties and specific heat of MPS<sub>3</sub> (M=Mn, Fe, Zn). J. Magn. Magn. Mat. 272-276, E593–E595 (2004).
- [21] Šiškins, M. *et al.* Highly anisotropic mechanical and optical properties of 2D layered As<sub>2</sub>S<sub>3</sub> membranes. ACS Nano 13, 10845–10851 (2019).
- [22] Leissa, A. W. & Qatu, M. S. Vibrations of continuous systems (New York: McGraw-Hill, 2011).
- [23] Landau, L. D., Pitaevskii, L. P. & Lifshitz, E. M. Electrodynamics of continuous media, vol. 8 (Butterworth, New York, 1984), 2 edn.
- [24] Bunch, J. S. et al. Electromechanical resonators from graphene sheets. Science 315, 490–493 (2007).
- [25] Gui, Q. et al. Extrinsic-structured bimetallic-phase ternary metal phosphorus trisulfides coupled with ndoped graphitized carbon for superior electrochemical lithium storage. Adv. Energy Mater. 11, 2003553 (2021).
- [26] Liu, Q. et al. Magnetic order in XY-type antiferromagnetic monolayer CoPS<sub>3</sub> revealed by Raman spectroscopy. *Phys. Rev. B* 103, 235411 (2021).

- [27] Afanasiev, D. et al. Controlling the anisotropy of a van der Waals antiferromagnet with light. Sci. Adv. 7, eabf3096 (2021).
- [28] Kim, K. et al. Suppression of magnetic ordering in XXZtype antiferromagnetic monolayer NiPS<sub>3</sub>. Nat. Commun. 10, 345 (2019).
- [29] Yao-Dong, D. et al. A Mössbauer study of the magnetic coupling in iron phosphorous trisulfides. *Chinese Phys.* 13, 1652 (2004).
- [30] Zhang, Q. et al. Observation of giant optical linear dichroism in a zigzag antiferromagnet FePS<sub>3</sub>. Nano Lett. 8 (2021).
- [31] Zhang, R. & Willis, R. F. Thickness-dependent Curie temperatures of ultrathin magnetic films: Effect of the range of spin-spin interactions. *Phys. Rev. Lett.* 86, 2665– 2668 (2001).
- [32] Gibertini, M., Koperski, M., Morpurgo, A. F. & Novoselov, K. S. Magnetic 2D materials and heterostructures. *Nat. Nanotechnol.* 14, 408–419 (2019).
- [33] Steeneken, P. G., Dolleman, R. J., Davidovikj, D., Alijani, F. & van der Zant, H. S. J. Dynamics of 2D material membranes. 2D Mater. 8, 042001 (2021).

- [34] Giannozzi, P. et al. QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials. J. Phys. Condens. Matter 21, 395502 (2009).
- [35] Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. *Phys. Rev. Lett.* 77, 3865–3868 (1996).
- [36] Head, J. D. & Zerner, M. C. A Broyden—Fletcher—Goldfarb—Shanno optimization procedure for molecular geometries. *Chem. Phys. Lett.* **122**, 264–270 (1985).
- [37] Monkhorst, H. J. & Pack, J. D. Special points for Brillouin-zone integrations. *Phys. Rev. B* 13, 5188–5192 (1976).
- [38] Mostofi, A. A. et al. wannier90: A tool for obtaining maximally-localised wannier functions. Comput. Phys. Commun. 178, 685–699 (2008).
- [39] He, X., Helbig, N., Verstraete, M. J. & Bousquet, E. Tb2j: A python package for computing magnetic interaction parameters. *Comput. Phys. Commun.* 264, 107938 (2021).