# Antiferromagnetic domains in a single crystal of the A-type spin-7/2 trigonal topological insulator $EuSn_2As_2$

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EuSn<sub>2</sub>As<sub>2</sub> is a trigonal A-type antiferromagnetic topological insulator with the moments aligned in the *ab* plane and with a Néel temperature  $T_{\rm N} = 23.5$  K. Here we report that an EuSn<sub>2</sub>As<sub>2</sub> crystal exhibits a broad peak at  $H_{c1} = 1100$  Oe in the field derivative  $dM_{ab}/dH$  of the *ab*-plane magnetization  $M_{ab}(H)$  at temperature T = 2 K, demonstrating the presence of trigonal antiferromagnetic domains. We model these  $M_{ab}(H, T = 2$  K) data and obtain the trigonal anisotropy-energy coefficient  $K_3$ that is 13.3 and 3.7 times larger than those we previously reported for single crystals of the trigonal compounds EuMg<sub>2</sub>Sb<sub>2</sub> and EuMg<sub>2</sub>Bi<sub>2</sub>, respectively.

#### I. INTRODUCTION

FIG. 1. Trigonal crystal structure of  $\text{EuSn}_2\text{As}_2$  [2]. The Eu atoms are colored dark purple, the Sn atoms blue, and the As atoms green. The Eu atoms form a hexagonal (triangular) layer situated between two buckled SnAs honeycomb layers, with four Eu layers within each *c*-axis height. The Eu magnetic structure is A-type with the Eu<sup>2+</sup> moments aligned in the *ab* plane [2]. The height of the magnetic unit cell is twice the *c*-axis lattice parameter.

 $EuSn_2As_2$  is a topological insulator that has been reported to exhibit Dirac surface states at energies within the bulk band gap from angle-resolved photoemission spectroscopy (ARPES) measurements [1]. The compound crystallizes in the trigonal NaSn<sub>2</sub>As<sub>2</sub>-type structure with space group  $R\overline{3}m$  shown in Fig. 1 [2]. It orders antiferromagnetically below its Néel temperature  $T_{\rm N} \approx 23.5 \text{ K} [2, 3]$ . Neutron-diffraction measurements [2] showed that the antiferromagnetic (AFM) structure is A-type, where the Eu<sup>+2</sup> moments have spin S = 7/2, spectroscopic splitting factor g = 2, and ordered moment  $\mu = gS\mu_{\rm B} = 7\mu_{\rm B}$ , where  $\mu_{\rm B}$  is the Bohr magneton. The Eu moments are aligned ferromagnetically in an *ab* plane layer with the Eu moments in adjacent layers along the c axis aligned antiferromagnetically [2]. Other



FIG. 2. Magnetic anisotropy free energy  $E_{\text{anis}}$  of ferromagnetic moments aligned at an angle  $\phi$  with the positive x axis, normalized by the trigonal anisotropy constant  $K_3$  in Eq. (1).

studies of the magnetic and thermodynamic properties of  $EuSn_2As_2$  single crystals were also presented in Ref. [2].

The related topological compounds EuMg<sub>2</sub>Sb<sub>2</sub> and EuMg<sub>2</sub>Bi<sub>2</sub> crystallize in the trigonal CaAl<sub>2</sub>Si<sub>2</sub>-type crystal structure with space group  $P\bar{3}m1$  and order antiferromagnetically at  $T_{\rm N} = 8.2$  and 6.7 K, respectively. Neutron-diffraction measurements demonstrated that both compounds exhibit A-type AFM order with the Eu moments aligned in the ab plane [4, 5]. Remarkably, crystals of both compounds showed a distinct positive curvature in  $M(H_{ab})$  isotherms at low fields  $0 \leq H_{ab} \lesssim H_{c1}$  at T = 1.8 K, where  $H_{c1} \approx 220$  and  $\approx 465$  Oe for EuMg<sub>2</sub>Sb<sub>2</sub> and and EuMg<sub>2</sub>Bi<sub>2</sub>, respectively [6]. At higher fields up to the respective saturation critical fields which were  $H_c^c = 3.4 \text{ T}$  for EuMg<sub>2</sub>Sb<sub>2</sub> at 1.8 K [4] and 4.0 T at 2 K for  $\text{EuMg}_2\text{Bi}_2$  [7], it was found that  $M_{ab} = \chi(T_N)H_{ab}$  as expected from molecular-field theory [8] since the moments were initially nearly perpendicular to  $\mathbf{H}_{ab}$  at the respective critical field  $H_{c1}$ .

These observations motivated us to consider the presence of equally-populated trigonal AFM domains below the respective  $T_{\rm N}$  of EuMg<sub>2</sub>Bi<sub>2</sub> and EuMg<sub>2</sub>Sb<sub>2</sub>. These



FIG. 3. (a) Domain model for trigonal A-type antiferromagnets in  $H_x = 0$  [6]. Moments 1, 4, and 6 are the magnetic moments in a central layer in zero field according to Fig. 2, whereas moments 2, 3, and 5 represent moments in adjacent layers in the collinear A-type AFM structure. The arrows and  $\Delta\phi$  indicate the direction of rotation of the moments in a domain for  $H_x \leq H_{c1}$ . (b) Orientation of the moments when  $H = H_{c1}$ , apart from a slight canting toward  $H_x$  that gives rise to the measured magnetization. (c) Rotation of the moments in each domain towards  $H_x$  for  $H_{c1} < H_x < H_{ab}^c$ , where  $H_{ab}^c$  is the *ab*-plane saturation (critical) field.

domains result from the existence of a trigonal anisotropy free energy of the form

$$F(\phi) = K_3 \cos(3\phi), \tag{1}$$

where  $K_3$  is the anisotropy energy amplitude and  $\phi$  is the angle between moments in an A-type AFM domain and

the x axis, which is assumed to be the axis in which a magnetic field  $H_x$  is applied. A plot of  $F(\phi)$  is shown in Fig. 2, where three minima in  $F(\phi)$  are at  $\phi/\pi = -5/6$ , -1/6, and 1/2.

The critical field  $H_x = H_{c1}$  is the *ab*-plane field at which all moments in each domains become nearly perpendicular to  $H_{ab}$ , apart from a small canting  $\leq 1^{\circ}$  toward the field that gives rise to the observed magnetization. The  $M(0 \leq H_{ab} \leq H_{c1})$  data for both EuMg<sub>2</sub>Sb<sub>2</sub> and EuMg<sub>2</sub>Bi<sub>2</sub> were successfully fitted by a model in which the positive curvature in  $M(H_{ab})$  below  $H_{c1}$  arose from the field response of the Eu spins in trigonal domains in Fig. 3 [6]. These fits allowed the respective *ab*-plane trigonal anisotropy parameters  $K_3$  to be determined.

### II. THEORY

Here we analyze the low-field  $M(H_{ab}, T = 2 \text{ K})$  data for EuSn<sub>2</sub>As<sub>2</sub> [2] in Fig. 4(b) by our model [6] for the magnetic response of the moments in isolated trigonal domains at T = 0 K and derive therefrom the value of its trigonal anisotropy constant  $K_3$ . We will then compare this value with the values of  $K_3$  previously obtained for trigonal domains in EuMg<sub>2</sub>Sb<sub>2</sub> and EuMg<sub>2</sub>Bi<sub>2</sub> [6].

With increasing *ab*-plane field  $H_x$  at T = 2 K, the three AFM domains initially at 120° to each other as shown in Fig. 3(a) begin to align nearly perpendicular to  $H_x$ , which according to Fig. 4(c) occurs at  $H_x \approx 1100$  Oe. Then with a further increase in  $H_x$  the collinear spins in each domain progressively cant towards  $H_x = H_{ab}$  until they reach FM alignment at the critical field  $H_{ab}^c \approx 3.7$  T according to Fig. 4(a).

Following Ref. [6], the anisotropy energy (1) averaged over the three domains and then normalized by  $K_3$  is

$$\frac{E_{\text{anis ave}}}{K_3} = -\frac{1}{3} [1 + 2\cos(3\Delta\phi)], \qquad (2)$$

and the magnetic energy normalized by  $K_3$  is

$$\frac{E_{\text{mag ave}}}{K_3} = -\frac{\chi_\perp H_x^2}{3K_3} \Big[ 1 + 2\sin^2\left(\frac{\pi}{6} + \Delta\phi\right) \Big], \quad (3)$$

where  $\Delta \phi$  in Fig. 3(c) is the rotation angle of the moments due to a particular  $H_x$  and  $\chi_{\perp} = \chi_c$  is the magnetic susceptibility perpendicular to the *ab* plane, which according to molecular-field theory [8] is  $\chi_c = \chi(T_{\rm N})$ . Then setting

 $h_x = \chi_\perp H_x^2 / K_3$ 

gives

$$\frac{E_{\text{mag ave }2}}{K_3} = -\frac{h_x}{3} \left[ 1 + 2\sin^2\left(\frac{\pi}{6} + \Delta\phi\right) \right]. \tag{5}$$

(4)

Thus the total average energy  $E_{\text{tot ave}}$  normalized by  $K_3$  is

$$\frac{E_{\text{tot ave}}}{K_3} = \frac{E_{\text{anis ave}}}{K_3} + \frac{E_{\text{mag ave }2}}{K_3}.$$
 (6)



FIG. 4. (a) Magnetization versus x-axis field  $H_x$  up to 55 kOe. The critical field for the *ab*-plane field is  $\approx 37$  kOe. (b) Expansion of  $M_{ab}(H)$  for  $H \leq 5$  kOe. (c) Low-field slope  $dM_{ab}/dH$ , yielding  $H_{c1} \approx 1100$  Oe. The small peak at  $H \approx 200$  Oe was also observed to occur for  $dM_{ab}/dH$  with  $\mathbf{H} \parallel c$  [2] and was postulated to arise from the presence of magnetic defects.

Then using Eqs. (2) and (5) and minimizing  $E_{\text{tot ave}}/K_3$ in Eq. (6) with respect to  $\Delta \phi$  gives a simple solution for  $h_x$  in terms of  $\Delta \phi$  as

$$h_x(\phi) = 3\csc[(\pi + 6\Delta\phi)/3]\sin(3\Delta\phi). \tag{7}$$

From Figs. 3(a) and 3(b), we have  $\Delta \phi = \pi/3$  when  $H_x = H_{c1}$ , *i.e.*, when all moments are approximately perpendicular to  $H_x$ . Then Eqs. (4) and (7) and give

$$h_x(\pi/3) = \frac{9}{2} = \frac{\chi_\perp H_{c1}^2}{K_3}.$$
 (8)

This value is per Eu<sup>2+</sup> ion, whereas the measured  $\chi_{\perp} = \chi(T_{\rm N})$  is per mole of Eu ions, so Eq. (8) becomes

$$\frac{9}{2} = \frac{\chi_{\perp} H_{\rm c1}^2}{N_{\rm A} K_3},\tag{9}$$

where  $N_{\rm A}$  is Avogadro's number. Then using  $H_{\rm c1} = 1100$  Oe from Fig. 4(c), the anisotropy-corrected  $\chi_{\perp} = \chi(T_{\rm N}) = 0.86 \,{\rm cm}^3/{\rm mol}$  [2], and solving for  $K_3$  gives

$$K_{3} = \frac{\chi_{\perp} H_{c1}^{2}}{(9/2)N_{A}}$$
(10)  
= 2.4 × 10<sup>-7</sup> eV/Eu.

This  $K_3$  value is 13.3 and 3.7 times larger than those found for single crystals of the two previouslystudied trigonal A-type antiferromagnets EuMg<sub>2</sub>Sb<sub>2</sub> and EuMg<sub>2</sub>Bi<sub>2</sub>, respectively [6].

# III. CONCLUDING REMARKS

The present work is part of an ongoing effort to characterize the *ab*-plane magnetic-field dependence of  $Eu^{2+}$  and  $Gd^{3+}$  spin S = 7/2 trigonal and tetragonal A-type antiferromagnets with the moments aligned in the *ab* plane. In addition to the present study of  $EuSn_2As_2$ , these compounds have so far included trigonal  $EuMg_2Sb_2$ and  $EuMg_2Bi_2$  [6] as noted in the text, and also trigonal  $EuAl_2Ge_2$  [9] and tetragonal  $EuGa_4$  [10]. In future work, it would be interesting to determine if the *ab*-plane magnetic-field-induced changes in the domain structure also affects the topological properties of relevant A-type antiferromagnets.

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