

# Frustration-induced quantum criticality in Ni-doped CePdAl as revealed by the $\mu$ SR technique

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In CePdAl, the 4f moments of cerium arrange to form a geometrically frustrated kagome lattice. Due to frustration in addition to Kondo- and RKKY- interactions, this metallic system shows a long-range magnetic order (LRO) with a  $T_N$  of only 2.7 K. Upon Ni doping at the Pd sites,  $T_N$  is further suppressed, to reach zero at a critical concentration  $x_c \approx 0.15$ . Here, by using muon-spin relaxation and rotation ( $\mu$ SR), we investigate at a local level CePd<sub>1-x</sub>Ni<sub>x</sub>Al for five different Ni-concentrations, both above and below  $x_c$ . Similar to the parent CePdAl compound, for  $x = 0.05$ , we observe an incommensurate LRO, which turns into a quasi-static magnetic order for  $x = 0.1$  and 0.14. More interestingly, away from  $x_c$ , for  $x = 0.16$  and 0.18, we still observe a non-Fermi liquid regime, evidenced by a power-law divergence of the longitudinal relaxation at low temperatures. In this case, longitudinal field measurements exhibit a time-field scaling, indicative of a cooperative spin dynamics that persists for  $x > x_c$ . Furthermore, similar to the externally applied pressure, the chemical pressure induced by Ni doping suppresses the region below  $T^*$ , characterized by a spin-liquid like dynamical behavior. Our results suggest that the magnetic properties of CePdAl are similarly affected by the hydrostatic- and the chemical pressure. We also confirm that the unusual non-Fermi liquid regime (compared to conventional quantum critical systems) is due to the presence of frustration that persists up to the highest Ni concentrations.

## I. INTRODUCTION

Heavy-fermion compounds with partially localized  $d$ - or  $f$  magnetic moments have long been at the center of numerous theoretical- and experimental studies [1]. The interest on these strongly-correlated electron systems stems from the plethora of phenomena they exhibit, such as quantum criticality [2, 3], hidden order [4], charge-density wave [5], or the possibility to behave as superconductors [6], topological insulators [7], or topological Weyl semimetals [8, 9]. In magnetic heavy-fermion compounds, two types of interactions dominate. One of them is the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction, where the conduction electrons mediate the interaction between the local magnetic moments which, consequently, tend to form a long-range order. If the coupling between the local moments and the conduction electrons is  $J$ , the strength of the RKKY interaction varies as  $T_{\text{RKKY}} \propto J^2$  [10, 11]. On the other hand, the Kondo interaction arises because of the formation of many-body singlet states between the local moments and the conduction electrons. Since it screens the local moments, it tends to suppress the long-range magnetic ordering temperature. The strength of the Kondo interaction varies as  $T_K \propto e^{(-1/J)}$  [12]. In 1977, Doniach proposed a phase diagram which reflects the  $J$  dependence of the two interactions and indicates that, for small values of  $J$ , the RKKY interaction dominates, while, for high values of  $J$ , the Kondo interaction dominates [13]. Because of the competition between these two interactions, at a particular value of  $J$ , the long-range magnetic ordering disappears. Thus, by utilizing a non-thermal tuning parameter (such as pressure, magnetic field, or doping), one can tune  $J$  and continuously suppress the second-order phase transition to  $T = 0$ , to reach the so-called quantum critical point (QCP). Quantum fluctuations at the QCP break down the Fermi-liquid model, and a non-Fermi-liquid behavior [14, 15] is expected to show up in different physical properties, such as magnetic susceptibility, heat capacity, spin-lattice relaxation rate, etc.

Recently, a “global phase diagram” has been proposed on

top of the Kondo- and RKKY interactions [16], incorporating also the effects of quantum fluctuations (which increase with increasing frustration). The inclusion of frustration, arising from local moments arranged into a triangular, kagome, Shastry-Sutherland, or pyrochlore lattice, induces different types of quantum criticality (local- and SDW-type) [17, 18] and exotic phases of matter, e.g., quantum-spin liquids (QSL) [19]. A QSL is an entangled state where magnetic moments, despite being highly correlated, do not break any symmetry, even down to  $T = 0$ . Unlike in insulators, where QSL states are more common, in metallic systems they are quite rare. Yet, in some frustrated metallic systems, such as CeRhSn [20], Pr<sub>2</sub>Ir<sub>2</sub>O<sub>7</sub> [21], CeRh<sub>1-x</sub>Pd<sub>x</sub>Sn [22], and CeIrSn [23], a QSL-type spin dynamics has been observed. The study of metallic systems with magnetic moments lying in a frustrated lattice is comparatively less explored, but nonetheless intriguing. For instance, in the absence of Dzyaloshinskii-Moriya interactions, skyrmion spin textures have been observed in 4f-based metallic systems with a frustrated lattice [24, 25].

In this respect, CePdAl, where the Ce moments are arranged in a highly frustrated kagome lattice [26], is a very promising system for exploring the above mentioned topics. CePdAl (with  $T_N \approx 2.7$  K) is also very susceptible to tuning. Thus, hydrostatic pressure can suppress the LRO and a QCP emerges at a  $P_c$  of about 0.9 GPa. More interestingly, an extended non-Fermi liquid regime with QSL-like dynamic correlations has been observed up to about twice  $P_c$ . Such a phase was claimed to be due to the presence of frustration [27, 28]. Thus, the presence of frustration not only stabilizes the QSL state, but it also changes the generic features of QCP by producing an extended NFL regime well beyond the critical point. As the lattice parameters were found to decrease with increasing Ni-doping [26], the resulting chemical pressure caused by Ni replacement at the Pd sites suppresses  $T_N$  to 0 K at a critical concentration  $x_c \approx 0.15$ . In this case, the relevant questions are: “What is the nature of the critical fluctuations around QCP? Is there any extended non-Fermi liquid regime/state also with chemical pressure? What are

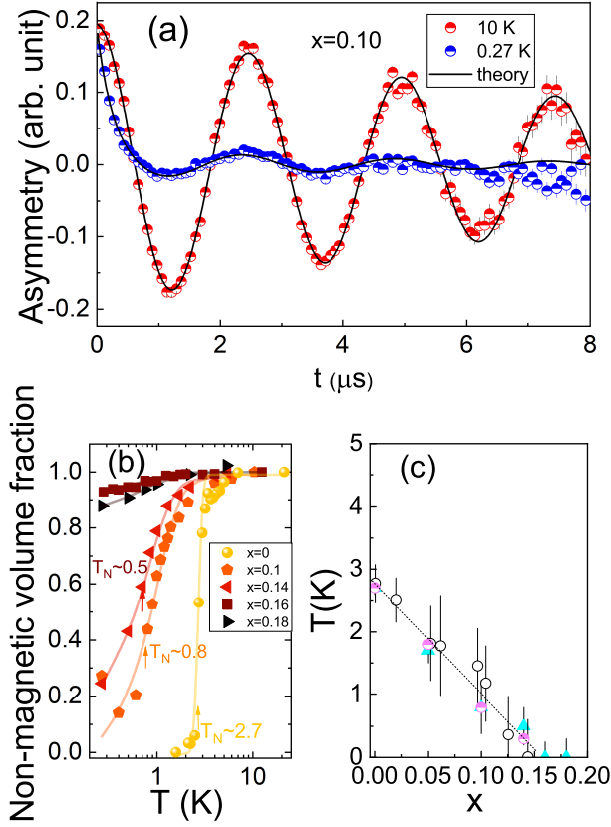


FIG. 1. (a) wTF- $\mu$ SR asymmetry of  $x = 0.1$  in a 3-mT applied field. (b) Nonmagnetic volume fraction vs. temperature estimated from wTF measurements for different Ni concentrations. Solid lines are fits using Eq. (2). (c) Temperature-concentration diagram of Ni-doped CePdAl resulting from wTF- $\mu$ SR data. The dotted line is a linear fit. Triangles represent  $T_N$  from the present study, while heat-capacity data (open circles), and neutron-scattering results (half-filled circles) are taken from Ref. 26 and 29, respectively.

the similarities or dissimilarities between the hydrostatic and chemical pressure? Is frustration responsible for the non-Fermi-liquid behavior, or the (chemical-doping induced) disorder can account for it?" To answer these questions, we employed a well-known local-probe technique such as muon-spin relaxation/rotation ( $\mu$ SR). All samples were specimens of Czochralski-grown single crystals which were powderized and pressed into pellets for the measurements. The  $\mu$ SR experiments were performed on  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$  with five different Ni-concentrations  $x$ , both above and below  $x_c = 0.15$ : 0.05, 0.1, 0.14, 0.16, and 0.18 on the Dolly spectrometer of the Swiss Muon Source (S $\mu$ S) at the Paul Scherrer Institute, Switzerland. The base temperature for the Dolly spectrometer is 270 mK reached by using a  $^3\text{He}$  cryostat. Such an extensive investigation allowed us not only to answer the above questions, but also to construct a comprehensive phase diagram of CePdAl under Ni doping.

## II. EXPERIMENTAL RESULTS

The NFL behavior in a metal arises from its low-lying quasi-particle excitations, to which a low-frequency probe like  $\mu$ SR is quite sensitive. Thus, extensive ( $\mu$ SR) measurements were performed to elucidate the complex phase diagram of  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$ . The details of the different  $\mu$ SR

experiments, along with the results obtained, are discussed in the following sections.

### A. Weak transverse field (wTF) measurements

Weak transverse field (wTF) measurements allow us to extract the temperature dependence of the non-magnetic volume fraction from which the magnetic ordering temperature can be estimated. The terms weak and transverse indicate that the applied field is less than the internal field (and low enough, so that it does not deviate the muon beam) and that the applied magnetic field is transverse with respect to the direction of the muon spin, respectively. The wTF spectra were collected in a 3-mT applied field at several temperatures and in samples with different Ni-concentrations. Figure 1(a) depicts the wTF asymmetry of the  $x = 0.1$  sample at 0.27 and 10 K. The wTF asymmetries were fitted by a combination of an exponentially relaxing oscillatory component, representing the paramagnetic spins, and a fast exponentially relaxing non-oscillatory component, representing the spins taking part in the magnetic ordering [solid lines in Fig. 1(a)]:

$$A(t) = A_0[f_{\text{pm}} \cos(\omega t + \phi_{\text{TF}})e^{-\lambda_{\text{pm}} t} + (1 - f_{\text{pm}})e^{-\lambda_{\text{ord}} t}]. \quad (1)$$

Here,  $A(t)$  is the time-dependent muon asymmetry, with  $A_0$  the initial asymmetry.  $f_{\text{pm}}$ ,  $\omega$ ,  $\phi_{\text{TF}}$ ,  $\lambda_{\text{pm}}$  are the fraction of spins, the muon Larmor frequency, the initial phase, and the relaxation rate in the paramagnetic state. Finally,  $\lambda_{\text{ord}}$  is the relaxation rate in the magnetically ordered phase. At the highest temperature, the externally applied field dominates the internal field ( $H_{\text{ext}} \gg H_{\text{int}}$ ), thus giving rise to asymmetry oscillations with the highest  $f_{\text{pm}}$ , indicative of a fully paramagnetic state. As  $T$  decreases, the oscillation amplitude  $f_{\text{pm}}$  decreases, indicating the onset of a spontaneous internal field. At the same time,  $(1 - f_{\text{pm}})$  increases as the temperature decreases, indicating the enhanced magnetic contribution related to the long-range magnetic order. As shown in Fig. 1(b), the temperature dependence of  $f_{\text{pm}}$  (the non-magnetic volume fraction) was fitted with an empirical sigmoidal function:

$$A(T) = A_a + \frac{A_b - A_a}{1 + \exp \frac{T - T_N}{\Delta T}} \quad (2)$$

Here,  $T_N$  is the ordering temperature and  $\Delta T$  is the transition width.  $A_a$  and  $A_b$  are the asymmetries above and below  $T_N$ , respectively. The suppression of  $T_N$  of CePdAl as the Ni doping increases is shown in Fig. 1(c). Our results are consistent with those from magnetization- and heat-capacity measurements [26, 29]. The linear suppression of  $T_N$  with Ni doping yields a critical concentration  $x_c \approx 0.15$ .

### B. Zero-field measurements

Zero-field (ZF)  $\mu$ SR measurements are sensitive to small magnetic moments (as small as  $0.001 \mu_B$ ) and, thus, are a powerful tool to study weak internal fields and a possible magnetic order. The time dependence of ZF- $\mu$ SR asymmetry provides useful hints into the nature of the long-range ordered state and the quantum critical behavior of the electron spin dynamics close to the QCP

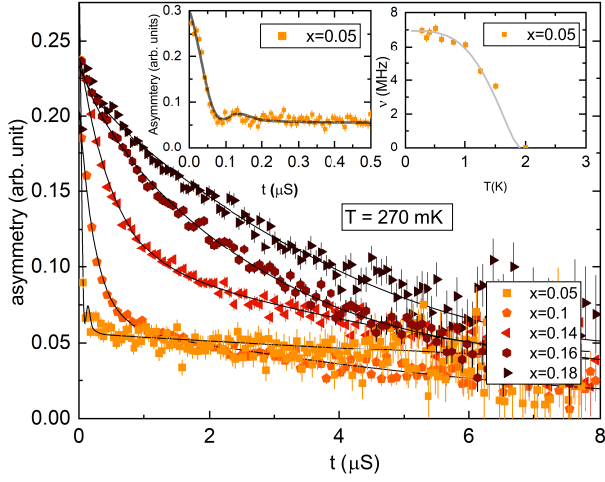


FIG. 2. Zero-field  $\mu$ SR asymmetry for different Ni-concentrations. Solid lines are fits to the equations described in the text. Insets show the short-time  $\mu$ SR asymmetry (left) and  $\nu$  vs. temperature (right) for the  $x = 0.05$  case.

### 1. Magnetically ordered state (for $x < x_c$ )

Figure 2 shows the ZF- $\mu$ SR asymmetry spectra of all the samples ( $x = 0.05, 0.1, 0.14, 0.16$ , and  $0.18$ ), recorded at  $0.27$  K. For  $x = 0.05$ , the zero-field  $\mu$ SR asymmetry is very similar to that of the CePdAl parent compound. In this case, the same function used for CePdAl [27] provides perfect fits:

$$A(t) = A_0 \left\{ f_{\text{sample}} \left[ \frac{2}{3} j_0(2\pi\nu t + \phi) e^{-\frac{\sigma^2 t^2}{2}} + \frac{1}{3} e^{\lambda_L t} \right] + (1 - f_{\text{sample}}) e^{-\lambda_{\text{bkg}} t} \right\} \quad (3)$$

Here,  $A_0$  is the initial asymmetry and  $\sigma$  is the depolarization rate caused by the distribution of internal fields.  $\nu$  is the frequency of the oscillating component and  $\phi$  is its phase (here, kept at zero).  $\lambda_L$  is the longitudinal relaxation rate,  $f_{\text{sample}}$  is the fraction of moments involved in the long-range order (LRO), and  $\lambda_{\text{bkg}}$  the background relaxation contribution. As shown in the inset of Fig. 2, below  $T_N$ , the order parameter can be mapped into the oscillation frequency, whose temperature dependence for the  $x = 0.05$  case is described by  $\nu(T) = \nu_0 [1 - (T/T_N)^\delta]^\eta$ , with  $\delta = 3.5$  and  $\eta = 2$ . Here,  $\nu_0$  is the local field at the muon site, extrapolated to  $T = 0$ . This is shown to vary linearly with the ordering temperature  $T_N$  (see inset in Fig. 6), here, an implicit function of pressure [27].  $T_N$  is shown to correlate linearly also with the ordered magnetic moment (estimated from neutron diffraction experiments [29]), thus strongly suggesting that, as expected, the local magnetic field at the muon stopping site is proportional to the ordered moment.

Interestingly, at higher Ni doping ( $x = 0.1$  and  $0.14$ ), no spontaneous muon spin precession is observed down to  $0.27$  K, despite a magnetic ordering taking place at  $0.8$  K and  $0.5$  K, respectively (as determined from wTF- $\mu$ SR data). Below these ordering temperatures, the zero-field  $\mu$ SR asymmetry of the  $x = 0.1$  and  $0.14$  samples is well fitted by the sum of two exponential functions, one with a slow- and one with a fast relaxation rate:

$$A(t) = A_0 [f_s (e^{-\lambda_s t}) + f_f (e^{-\lambda_f t})] \quad (4)$$

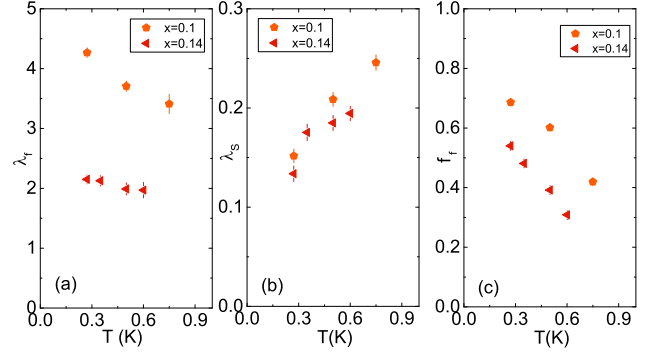


FIG. 3. Temperature dependence of  $\lambda_f$  (a),  $\lambda_s$  (b), and  $f_f$  (c) for  $x = 0.1$  and  $x = 0.14$ .

Here,  $A_0$  is the initial asymmetry, fixed at the highest temperature.  $f_s$  and  $f_f$  ( $= 1 - f_s$ ) are the fractions of the slow- and the fast relaxation components, while  $\lambda_s$  and  $\lambda_f$  are the respective muon-spin relaxation rates. The temperature dependence of  $\lambda_f$ ,  $\lambda_s$  and  $f_f$  is shown in Fig. 3. As the temperature is lowered,  $\lambda_f$  and  $f_f$  increase, while  $\lambda_s$  decreases. Since the  $f_f$  fraction increases to approximately  $0.66$  ( $\sim 2/3$ ) and  $\lambda_f$  shows an order-parameter-like behavior, we identify the fast- and the slow component with the transverse- and the longitudinal relaxation, respectively. Their behavior can be ascribed either to a quasi-static magnetic ordering, as found also in other disordered systems, or to an incommensurate ordering, the latter leading to a broad distribution of local magnetic fields at the muon stopping site [30, 31]. The incommensurate ordering, however, may be discarded for the present systems, as we observe clear oscillations in the asymmetry due to incommensurate ordering at ambient- and under applied pressure [27] which indicates that the local magnetic field distribution here is not broad enough to completely wipe-out the oscillation. On the other hand, disorder originating from Ni doping is a more likely explanation for the evolution of the long-range magnetic order (in  $x = 0.05$ ) into a quasi-static magnetic order at higher Ni concentrations (see Fig. 6). The role of disorder is confirmed also by the increased broadening of the magnetic Bragg peak at  $Q_{AF}$  ( $0.5, 0, 0.35$ ) with increasing Ni content [29], a result at least partially attributed to disorder which further corroborates our hypothesis. Note that, we attempted to fit the ZF- $\mu$ SR asymmetry with various functions relevant for different types of disordered states, e.g., spin glass [32], inhomogeneous magnetic moments with short-range correlations [33–36], quantum Griffiths states [37]. Since none of them fits the data adequately, we conclude that the degree of disorder in CePd $_{1-x}$ Ni $_x$ Al is rather small compared to those states. In the Discussion section, we elaborate in more detail about the role of disorder.

### 2. Paramagnetic state

In the paramagnetic state, the ZF- $\mu$ SR asymmetry can be well fitted by a static Gaussian Kubo-Toyabe function, representing the nuclear moment contribution, multiplied by a stretched exponential function, representing the contribution of the electronic moments:

$$A(t) = A_0 [1/3 + 2/3 (1 - \sigma_n^2 t^2) e^{-(\sigma_n^2 t^2/2)} e^{-(\lambda t)^\beta}] \quad (5)$$

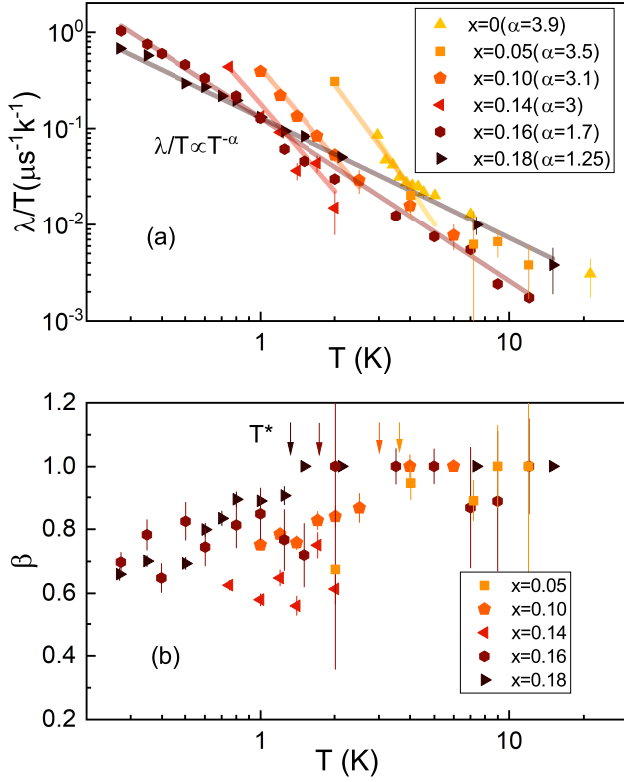


FIG. 4. Temperature dependence of the longitudinal relaxation rate  $\lambda/T$  for all the Ni concentrations (a). Solid lines represent power-law fits,  $T^{-\alpha}$ . Stretching exponent  $\beta$  for various Ni concentrations as a function of temperature (b). Arrows indicate the onset of the spin-liquid regime at  $T^*$ .

Here,  $\lambda$  and  $\sigma_n$  are the exponential- and the Gaussian relaxation rates, the latter found to be temperature independent, with  $\sigma_n = 0.13 \mu\text{s}^{-1}$ . Conversely, both  $\lambda$  and  $\beta$  depend on temperature. At high temperatures, the value of  $\beta$  is 1, representing a fixed-field distribution and simple random rapid fluctuations. Upon lowering the temperature,  $\beta$  decreases from 1 and  $\lambda$  increases. In Fig. 4(a), we show the temperature dependence of the relaxation rate  $\lambda/T = 1/T_{1\mu} T \propto \chi''(q, \omega)$ , where  $\chi''(q, \omega)$  is the imaginary part of the dynamical spin susceptibility. For  $x = 0.05, 0.1$  and  $0.14$ ,  $\lambda/T$  diverges towards  $T_N$  due to the critical slowing down of spin fluctuations by following a power-law,  $T^{-\alpha}$ , whose exponent  $\alpha$  decreases with increasing Ni concentration.

More interestingly, above the critical  $x_c \approx 0.15$  value (for  $x = 0.16$  and  $0.18$ ), the power-law behavior of  $\lambda/T$  still persists. Such an extension of the non-Fermi liquid regime above the critical value of the tuning parameter (here,  $x_c$ ) has also been seen in pressurized CePdAl, indicating the same effect of chemical- and hydrostatic pressure on CePdAl.

### C. Longitudinal field measurements

$\mu\text{SR}$  measurements in a longitudinal field (LF) allowed us to determine the nature of the electron-spin dynamics close to the QCP. Figure 5(a) shows the LF dependence of  $\lambda$  at  $0.27 \text{ K}$  for  $x = 0.16$  and  $x = 0.18$  (i.e., both above  $x_c$ ). The main cause of the muon-spin relaxation is usually the spin fluctuations of  $4f$  electrons, whose magnetic moments couple with those of the implanted muons. To have a

quantitative idea about the nature of spin dynamics at low temperature, we utilized the following function[38–40]:

$$\lambda(H) = 2\Delta^2 \tau^{x'} \int_0^\infty t^{-x'} e^{-\nu t} \cos(2\pi\mu_0\gamma_\mu H t) dt, \quad (6)$$

where  $t$  is time,  $\tau$  is an early-time cut-off,  $\Delta$  is the width of the internal-field distribution,  $\gamma_\mu$  is the gyromagnetic ratio, and  $\nu$  is the fluctuation frequency of local moments. A fit of the LF dependence of  $\lambda$  [see Fig. 5(a)] yields  $x' \neq 0$ , which indicates that the spin-spin autocorrelation function is not a simple exponential,  $C(t) = \exp(-\nu t)$ , but rather  $C(t) = (\tau/t)^{x'} \exp(-\nu t)$ . The fluctuation frequency  $\nu$ , for  $x = 0.16$  and  $0.18$ , is estimated to be  $315 \text{ MHz}$  and  $172 \text{ MHz}$ , respectively. In either case,  $\nu$  is two orders of magnitude higher than commonly found in other spin-liquid candidate materials:  $\text{NaYbS}_2$  [41],  $\text{YbMgGaO}_4$  [39],  $\text{Sr}_3\text{CuSb}_2\text{O}_9$  [42], and  $\text{BaTi}_{0.5}\text{Mn}_{0.5}\text{O}_3$  [40], but of similar order of magnitude to other metallic heavy-fermion compounds close to quantum criticality [43, 44]. Yet, the present  $\nu$  values are slower than those of many spin-glass materials [45].

Interestingly, for applied magnetic fields  $\mu_0 H$  between  $3$  and  $200 \text{ mT}$ , we identify also a time-field scaling  $A(t/H^\gamma)$ , where  $\gamma$  is an exponent. Such field dependence corresponds to evaluating the Fourier transform of  $C(t) = \langle S_i(0) \cdot S_i(t) \rangle$ , throughout the  $0.4$  to  $28 \text{ MHz}$  frequency range ( $\gamma_\mu H/2\pi$ ). Time-field scaling is a signature of slow dynamics that is encountered in both classical spin glasses and in NFL systems with local  $4f$  moments. Independent information on the behavior of the spin-spin autocorrelation function  $C(t)$  may be gained by examining the time-field scaling. While  $\gamma < 1$  signifies a power-law behavior of  $C(t)$ ,  $\gamma > 1$  implies a stretched exponential behavior, typical of inhomogeneous systems. In Fig. 5(c) and (d) we show the asymmetry vs. the time-scaling variable  $A(t/H^\gamma)$ , for  $x = 0.16$  and  $0.18$ , respectively. Since in both cases we find an exponent  $\gamma < 1$ , this indicates a power-law behavior of  $C(t)$ , consistent with an analysis by means of Eq. (6). The exponent  $\gamma$  also matches the power-law exponent in the  $\lambda$ -vs-applied-field plot shown in Fig. 5(b) up to  $0.2 \text{ T}$ . A similar time-field scaling has been found in  $\text{UCu}_{5-x}\text{Pd}_x$  [46],  $\text{CePtSi}_{1-x}\text{Ge}_x$  [47], and  $\text{CePd}_{0.15}\text{Rh}_{0.85}$  [48]. The high-field data (here, above  $0.2 \text{ T}$ ) deviate from the scaling curve as well as from the power-law behavior [Fig. 5(b)], indicating that higher applied fields have a direct effect on  $C(t)$ . A similar kind of deviation has also been seen in  $\text{Ce}(\text{Cu}_{1-x}\text{Co}_x)_2\text{Ge}_2$  [49]. Our LF experiments strongly suggest a cooperative spin dynamics in the spin-liquid regime above  $x_c$  and below  $T^*$ . Furthermore, the LF experiments also indicate that even a field of  $0.8 \text{ T}$  is not enough to completely suppress the relaxation process and suggests that the correlations are dynamic in nature as can be expected in the QSL state.

### III. DISCUSSION

Our pressure-temperature phase diagram [27] shows that the extended non-Fermi-liquid regime is exclusively due to frustration, as pressure does not introduce significant disorder. Since chemical doping may introduce disorder and an extended NFL regime also occurs in several disordered heavy-fermion compounds [50, 51], it is important to clarify whether disorder or frustration is responsible for the magnetic properties of  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$  above  $x_c$ .



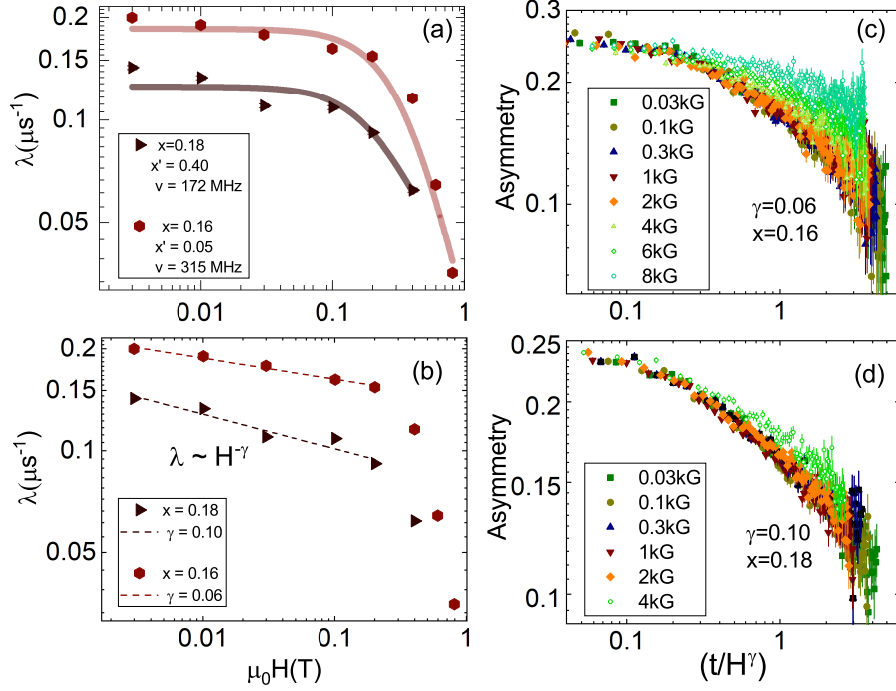


FIG. 5.  $\mu$ SR relaxation rate  $\lambda$  vs. longitudinal field for  $x = 0.14, 0.16$ , and  $0.18$  (a, b). Solid lines (a) represent fits using Eq. (6), while dashed lines (b) are power-law fits,  $\lambda \propto H^{-\gamma}$ . Time-field scaling of the  $\mu$ SR asymmetry at  $0.27$  K for  $x = 0.16$  (c) and  $0.18$  (d).

*Effect of disorder:* Disorder-induced states include the quantum Griffiths phase (QGP), spin glasses (SG), etc. QGP appears in systems where the quenched disorder radically affects a quantum-phase transition giving rise to an additional QGP phase. In such a case, a smeared phase transition can occur near the QCP. In  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$ , however, this smearing effect is not observed (at least not down to  $0.27$  K), which is low enough with respect to the temperatures below which QGPs have been found in other systems [37, 49, 52]. Thus, we can discard the possibility of such a phase. It should be noted that  $\lambda/T$  obeys a power-law  $T^{-\alpha}$  behavior, with  $\alpha > 1$  in the  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$  case. In other QGP systems, however, the power-law exponent is found to be less than 1, e.g., in  $\text{Ce}(\text{Cu}_{1-x}\text{Co}_x)_2\text{Ge}_2$  ( $\alpha = 0.55$ ) [49], in  $\text{CeCoGe}_{3-x}\text{Si}_x$  ( $\alpha = 0.72$ ) [53], and in  $\text{CePd}_{0.15}\text{Rh}_{0.85}$  ( $\alpha = 0.8$ ) [48]. This indicates that disorder suppresses the critical fluctuations.

Now we consider the possibility of a spin-glass (SG) state occurring in  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$ . The absence of spin freezing in Ni-doped  $\text{CePdAl}$  is supported by the following observations: (i) Spin glass is also a disordered magnetic state, where spins are statically aligned randomly, so that the dynamics is very slow, usually between  $0.01$  and  $0.1$  ns [45]. Our LF- $\mu$ SR measurements indicate a time scale of about  $3$ – $5$  ns, more than an order of magnitude larger than that of SG systems (mentioned in the previous section). (ii) The stretching exponent  $\beta$  decreases gradually from 1 at high temperatures to a constant value of  $0.6$  at low temperatures [see Fig. 4(b)]. On the other hand, for spin-glass systems,  $\beta$  is expected to decrease to  $1/3$  at the spin freezing temperature [54, 55]. (iii) As already discussed in the previous section, we were unable to fit the  $\mu$ SR asymmetry by considering any function relevant for the spin-glass state.

At the same time, resistivity measurements at higher Ni doping [56] show a negligible distribution of Kondo temperatures. This further indicates that Ni doping introduces at most only a weak disorder. Thus, it can be stated that the weak disorder introduced by Ni doping, is unable to form

neither QGP nor SG states in  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$ . The quasi-static state observed for  $x = 0.1$  and  $0.14$  may be an unconventional, weak disorder-induced state. Along with the above mentioned points, the incompatibility of fitting the asymmetry with different fit functions used for various disordered states supports the absence of strong disorder effects.

Usually, the lower the value of the exponent  $\gamma$ , the lesser the chance of having a disordered ground state. Thus, in the present case,  $\gamma \ll 1$  (discussed in the previous section) excludes a dominant effect of disorder in the critical fluctuations around the QCP. Since the effect of chemical- and hydrostatic pressure on  $\text{CePdAl}$  is identical (as far as the magnitude of  $\lambda/T$  and the power-law exponents are concerned), this again supports the weak effect of disorder in determining the non-Fermi liquid regime in this compound.

*Effect of frustration:* It is interesting to note that, for  $x = 0, 0.05$ , and  $0.1$ , the enhancement of  $\lambda/T$  [see Fig. 4(a)] starts from a temperature tenfold above  $T_N$ , indicating a high degree of frustration in  $\text{CePd}_{1-x}\text{Ni}_x\text{Al}$ . Neutron scattering also detects short-range correlations at a temperature much higher than  $T_N$ . Also for  $x = 0.16$  and  $0.18$  the enhancement of  $\lambda/T$  from a very high temperature suggests the significant role of frustration on the quantum critical nature of spin fluctuations. Note that, such an enhancement of  $\lambda/T$  from a very high temperature, was not observed in other Ce-based systems [22, 48, 49] lacking a geometrically frustrated lattice. This implies that frustration persists throughout the full doping range studied in the present work and it provides evidence that frustration is responsible for the extended non-Fermi-liquid regime (at  $x > x_c$ ) in  $\text{CePdAl}$ .

The presence of finite frustration is also reflected in the temperature dependence of  $\beta$  shown in Fig. 4(b). Our pressure dependent  $\mu$ SR study identifies a characteristic temperature  $T^*$ , below which  $\beta$  deviates from 1. This was assigned to the temperature below which spin-liquid-like correlations develop [27]. In the present case, too, such a characteristic temperature  $T^*$  exists and is found to decrease with

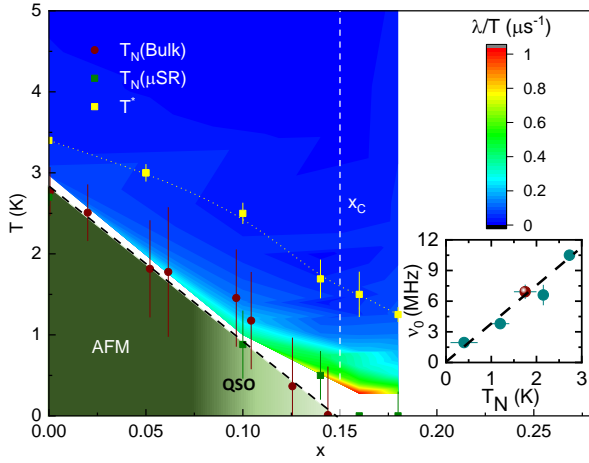


FIG. 6. Temperature-concentration magnetic phase diagram of Ni-doped CePdAl combined with a contour plot of the concentration and temperature-dependent relaxation rate  $\lambda/T(x, T)$ . The Neel temperatures  $T_N$  estimated from wTF- $\mu$ SR (green squares, with error bars indicating the width of transition) agree well with the reported values from susceptibility measurements (filled circles). Yellow squares represent  $T^*(x)$ . QSO stands for quasi-static magnetic ordering, as discussed in the text. Inset shows  $\nu_0$  vs. ordering temperature  $T_N$  (the dashed line is a linear fit). The brown- and the cyan circles correspond to the doping- and pressure evolution of  $T_N$  and  $\nu_0$ , respectively.

increasing Ni concentration, as shown in Fig. 4(b). This again confirms the similarity between the hydrostatic- and chemical-pressure effects in the magnetic properties of CePdAl. These observations indicate the importance of frustration on the quantum critical fluctuations and also the persistence of frustration throughout the full doping range.

From the above discussion, we have established that disorder has only a limited role in originating the non-Fermi liquid regime in CePd<sub>1-x</sub>Ni<sub>x</sub>Al, while the persistent frustration is clearly responsible for the extended NFL regime. The weak disorder seems to affect and stabilize only the quasi-static ordered state for  $x < x_c$ .

#### IV. CONCLUSION

In conclusion, by utilizing the local-probe  $\mu$ SR technique, we investigated the quantum critical Ni-doped CePdAl system across the full range of Ni concentrations, both above and below  $x_c = 0.15$ . For  $x = 0.05$ , we observe an incommensurate LRO state, similar to that of the CePdAl parent compound. Upon increasing the Ni concentration, disorder appears and the LRO changes into a quasi-static magnetic order for  $x = 0.1$  and  $0.14$ . This state does not exhibit the properties expected for a conventional spin-glass- or a quantum Griffiths state, thus indicating a relatively low amount of Ni-induced disorder in this system. Interestingly, a power-law dependence of the longitudinal relaxation rate and a time-field scaling are observed for  $x = 0.16$  and  $0.18$ , suggesting a non-Fermi liquid regime. Since both values lie above  $x_c$ , our results indicate that the non-Fermi liquid regime extends beyond  $x_c$ , thus mimicking the behavior of the pressure-induced phase diagram of CePdAl. Since frustration is shown to persist up to  $x = 0.18$ , the extended non-Fermi liquid regime is, therefore, due to frustration. Akin to the pressure effect on the magnetic properties of pure CePdAl, the chemical pressure in the Ni-doped case also reduces a characteristic temperature  $T^*$ , below which spin-liquid-like dynamical fluctuations occur in the  $x = 0.16$  and  $0.18$  case. In summary, all our observations suggest a similar role for the hydrostatic- and chemical pressure on the magnetic properties of CePdAl, with frustration being the main driving force behind such unusual behavior. In the future it might be interesting to see how far (in terms of Ni doping) such a frustration-driven non-Fermi liquid regime persists until the Fermi liquid emerges.

#### V. AUTHOR CONTRIBUTIONS

V.F. and O.S. prepared the sample and initiated the study of CePdAl. T.S. performed the  $\mu$ SR measurements, with the online assistance of I.I. and M.M.. I.I. and M.M. analysed the data. I.I., M.M. and T.S. wrote the manuscript with notable inputs from all the co-authors. M.M. supervised the project.

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