

Does DESI 2024 Confirm Λ CDM?

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We demonstrate that a $\sim 2\sigma$ discrepancy with the Planck- Λ CDM cosmology in DESI Luminous Red Galaxy (LRG) data at $z_{\text{eff}} = 0.51$ translates into an unexpectedly large Ω_m value, $\Omega_m = 0.668^{+0.180}_{-0.169}$. We independently confirm that this anomaly drives the preference for $w_0 > -1$ in DESI data confronted to the w_0w_a CDM model. We show that redshift bins of DESI constraints allow Ω_m to wiggle at the $\sim 2\sigma$ level with increasing effective redshift in the Λ CDM model. Given that LRG data at $z_{\text{eff}} = 0.51$ is at odds with Type Ia supernovae in overlapping redshifts, we expect that this anomaly will decrease in statistical significance with future DESI data releases leaving an increasing Ω_m trend with effective redshift at higher redshifts. We estimate the significance of the latter in DESI data at $\sim 1.8\sigma$ and comment on how it dovetails with independent observations. It is imperative to understand what makes DESI LRG data at $z_{\text{eff}} = 0.51$ an outlier when it comes to Ω_m determinations.

I. INTRODUCTION

In the absence of observational systematics, cosmological tensions [1–3] and pre-calculus demand that we see changes in the Λ CDM model parameters when confronted to data in different redshift bins [4, 5]. Conversely, if one recovers the same Λ CDM parameters within the errors when one confronts the model to data at different redshifts, then systematics are at play. In practice, testing all redshift ranges is not feasible, but we should endeavour to test as many redshift ranges as possible. The community is in the process of testing the consistency of the (flat) Λ CDM model. See [6] for an overview of results.

Recently, the Dark Energy Spectroscopic Instrument (DESI) collaboration has released its first round of cosmological constraints based on baryon acoustic oscillations (BAO) [7, 8], providing hints of evolution in the dark energy (DE) sector [9]. Consider the w_0w_a CDM model with redshift dependent DE equation of state, $w(z) = w_0 + (1 - a)w_a = w_0 + z/(1+z)w_a$, where a is the scale factor, z is the redshift, and $(w_0, w_a) = (-1, 0)$ [10, 11] recovers Λ CDM. In this context, DESI reports a preference for $w_0 > -1$, which is driven by the Luminous Red Galaxy (LRG) sample with effective redshift $z_{\text{eff}} = 0.51$. Combining DESI with Planck CMB data [12] and Type Ia supernovae (SNe), including Pantheon+ [13], Union3 [14] and DES [15], the preference for w_0w_a CDM model over Λ CDM increases to 2.5σ , 3.5σ and 3.9σ , respectively [9].

While nothing precludes folding different data sets together and confronting them to the w_0w_a CDM model, care is required with physics. In cosmology, physics demands that observables are singing from the same hymn sheet. In short, late-

time accelerated expansion is only believable if CMB, BAO, SNe, and many other data sets agree on its existence. Turning this argument around, DESI claims of dynamical dark energy are only believable if BAO and SNe show consistent deviations from the Λ CDM model in similar redshift ranges. If they contradict each other, then statistical fluctuations, systematics, or evolutionary effects with redshifts not properly treated, are at play somewhere.

In this letter we take a closer look at the implications of DESI data for the Λ CDM model on the grounds that if w_0w_a CDM model is preferred over Λ CDM model, then this must be evident in changes or evolution of the Λ CDM parameters with binned or effective redshift. Through this exercise, we find that DESI LRG data prefers larger $\Omega_m \sim 0.65$ values of matter density at $z_{\text{eff}} = 0.51$. Independent of DESI analysis [9], we confirm that this redshift range is responsible for the preference for $w_0 > -1$ in the w_0w_a CDM model. Moreover, binning DESI data reveals $\sim 2\sigma$ variations in Ω_m between bins. Given that no other cosmological probe has a preference for $\Omega_m \sim 0.65$ at lower redshifts, in particular SNe do not, we argue that a statistical fluctuation and/or systematics are at play either in DESI or SNe data. Finally, we speculate that an increasing Ω_m trend with effective redshift at higher redshift, one discernible in DESI data, is physical by invoking similar observations in independent probes.

II. FLAT Λ CDM

In this section we look for signatures of varying Λ CDM cosmological parameters in DESI data [9]. The motivation

is cosmological tensions [1–3], where it is necessary to diagnose potential shortcomings of the model by performing consistency checks of the model [6].

A. Markov Chain Monte Carlo

In Table I we employ MCMC [16] to determine the 68% confidence intervals for Λ CDM parameters from anisotropic BAO constraints in Table 1 of [9]. The observables include LRG, emission line galaxies (ELG) and the Lyman- α forest (Ly α QSO). The justification for focusing largely on anisotropic BAO is that, as is evident from Fig. 2 [9], isotropic BAO from the bright galaxies (BGS) and QSO cannot determine Ω_m , and isotropic BAO only constrains posteriors to curves in the (H_0, Ω_m) -plane. One can combine the posteriors, but the price one pays is putting observables at $z_{\text{eff}} = 0.3$ and $z_{\text{eff}} = 1.49$ in the same bin. Throughout we incorporate the correlation between D_M/r_d and D_H/r_d constraints, where r_d denotes the radius of the sound horizon at the baryon drag epoch and

$$D_M(z) := \frac{c}{H_0} \int_0^z \frac{dz'}{E(z')}, \quad D_H(z) := \frac{c}{H(z)} \quad (1)$$

where H_0 is the Hubble parameter, $H(z) = H_0 E(z)$ is the Hubble diagram and c is speed of light. Without external data or assumptions, it is impossible to separate H_0 from r_d , so we quote confidence intervals for the combination $H_0 r_d$ alongside Ω_m .

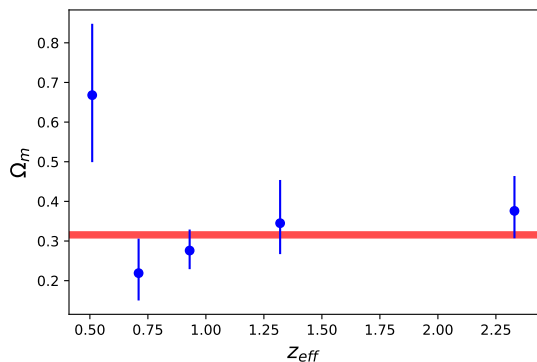


FIG. 1. 68% confidence intervals for Ω_m versus effective redshift z_{eff} . Neglecting the DESI LRG constraint at $z_{\text{eff}} = 0.51$, the data shows excellent agreement with the corresponding Planck- Λ CDM confidence interval in red.

From Table I, there are essentially two features to highlight. First, the LRG data at $z_{\text{eff}} = 0.51$ leads to a surprisingly large value of Ω_m that is discrepant with the Planck value $\Omega_m = 0.315 \pm 0.007$ [12] at the $\sim 2.1\sigma$ level. It is difficult to interpret this result, as it is also at odds with the Pantheon+ SNe constraint $\Omega_m = 0.334 \pm 0.018$ [13] at the $\sim 2\sigma$ level.¹

¹The relatively large LRG Ω_m errors mean that doubling the Ω_m error

Note, SNe samples typically have low effective redshifts of $z_{\text{eff}} \sim 0.3$. Thus, in contrast to Planck versus DESI LRG, where one has observables at different redshifts, Pantheon+ versus DESI LRG, is a disagreement in an overlapping redshift range. While it may be tempting to interpret the DESI result as a fluctuation in data, DESI has confirmed that the constraint in that redshift range is consistent with SDSS [9]. Unsurprisingly, as can be seen from Fig. 5 of [17], SDSS BAO [18] does lead to larger Ω_m values in similar redshift ranges. This makes a statistical fluctuation explanation less likely.

tracer	z_{eff}	$H_0 r_d$ [100 km/s]	Ω_m
LRG	0.51	$88.34^{+5.66}_{-4.75}$	$0.668^{+0.180}_{-0.169}$
LRG	0.71	$109.36^{+6.08}_{-6.08}$	$0.219^{+0.087}_{-0.069}$
LRG+ELG	0.93	$102.17^{+4.10}_{-4.02}$	$0.276^{+0.053}_{-0.047}$
ELG	1.32	$97.78^{+7.65}_{-8.02}$	$0.345^{+0.109}_{-0.078}$
Ly α QSO	2.33	$92.79^{+7.60}_{-7.46}$	$0.375^{+0.088}_{-0.069}$

TABLE I. 68% confidence intervals from DESI anisotropic BAO constraints at effective redshift z_{eff} .

The second feature of interest is an increasing Ω_m /decreasing $H_0 r_d$ with effective redshift beyond the anomalous LRG constraint. The trend is evident in Fig. 1 and Table I. This trend is expected if observations of similar trends in strong lensing time delay, both lensed QSOs [19–21] and SNe [22, 23],² type Ia SNe [17, 25–29] (see also [30–32] for related discussions), observational Hubble data (OHD) [26, 33], combinations of OHD and SNe [26, 34], GRBs [35], and standardisable QSOs [17, 26, 36–41] hold up.

As an aside, there is a growing body of work in literature either questioning [42–46] or improving the Risaliti-Lusso standardisable QSO prescription [39, 47, 48]. Nevertheless, despite the corrections imposed on the QSO data, residual evolution of the Ω_m parameter is still reported [47–49]. Moreover, DES SNe have a higher effective redshift [15], so the larger Ω_m value is consistent with these observations. Going beyond established probes such as SNe, QSOs [36, 37] and GRBs [50–56] calibrated by SNe, may also return larger values of Ω_m at higher redshifts.³ Returning to the main point, if not for the LRG Ω_m constraint at $z_{\text{eff}} = 0.51$, one could add the four highest redshift DESI constraints from Fig. 1 to the corroborating support for the increasing Ω_m /decreasing H_0 trend.

from CMB to SNe, while shifting the central value upwards, has little bearing on the statistical significance of the disagreement.

²The claim is particularly clear from Fig. 5 of [23] (see also [24]), where it is evident that the error bars of H_0 determined from SN Refsdal and SN H0pe do not overlap, placing the disagreement at $\sim 1.5\sigma$. Note that SN H0pe has a lens redshift of $z = 0.35$, whereas the lens redshift of SN Refsdal is $z = 0.54$, thereby making Fig. 5 of [23] consistent with the descending trend of H_0 with lens redshift reported originally in Wong et al. [19] (see appendix).

³This could be mundanely due to large scatter in the data and not due to any variation in the Λ CDM parameters. One can separate these two possibilities by comparing to SNe in overlapping redshift regimes [17].

z	$H_0 r_d$ [100 km/s]	Ω_m
$0.1 < z < 0.6$	$96.13^{+3.81}_{-3.94}$	$0.459^{+0.120}_{-0.098}$
$0.6 < z < 1.1$	$106.82^{+3.09}_{-3.08}$	$0.231^{+0.036}_{-0.033}$
$1.1 < z < 4.16$	$98.59^{+4.29}_{-4.27}$	$0.324^{+0.044}_{-0.038}$

TABLE II. 68% confidence intervals from DESI anisotropic and isotropic BAO binned by redshift. From bin 1 to bin 2 Ω_m shifts downwards by $\sim 2.2\sigma$ and from bin 2 to bin 3 Ω_m shifts upwards by $\sim 1.8\sigma$.

To assess the statistical significance of the increasing Ω_m /decreasing $H_0 r_d$ trend at higher redshifts, as well as the impact of the DESI constraint at $z_{\text{eff}} = 0.51$, we introduce the remaining two isotropic BAO constraints from Table 1 of the DESI paper [9]. The corresponding 68% confidence intervals are shown in Table II in redshift bins, where it is evident that Ω_m starts off high at lower redshifts, decreases at intermediate redshifts, before increasing again at larger redshifts. The statistical significance of the shifts in the Ω_m parameter are $\sim 2.2\sigma$ and $\sim 1.8\sigma$, respectively. As DESI is designed to produce a much larger number of constraints at a wide range of redshifts [57], it will be important to revisit these two features with future releases. Note, at $\sim 2\sigma$ one can of course ignore these results, but it is well established that matter density is approximately 30% in the Λ CDM Universe. This now comes with the caveat that there is a corner of the Universe probed by DESI where matter density is 65%; the inconsistency is striking.

Before moving on, we revisit Fig. 3 of [9] to comment on the discrepancies with Planck, $\Omega_m = 0.315 \pm 0.007$ [12], Pantheon+, $\Omega_m = 0.334 \pm 0.018$ [13], Union3, $\Omega_m = 0.356^{+0.028}_{-0.026}$ [14], and DES, $\Omega_m = 0.352 \pm 0.017$ [15], data sets. Once again, we use all the data, both anisotropic and isotropic BAO constraints. For all constraints in Table 1 of [9] we find $\Omega_m = 0.290^{+0.015}_{-0.014}$. This agrees well with our best fit or maximum likelihood estimator (MLE) of $\Omega_m = 0.289$. Note, the central value we find is slightly lower than Table 3 of the DESI paper [9]. This sets the disagreement with Planck, Pantheon+, Union3 and DES at $\sim 1.5\sigma$, $\sim 1.9\sigma$, $\sim 2.2\sigma$ and $\sim 2.7\sigma$, respectively. While all disagreements are below a 3σ threshold, they are serious enough that further study is warranted. It is fitting to recall the claim originally made in [17] that the fitting parameter Ω_m is not a constant and evolves, or more precisely increases, with effective redshift.

Finally, we remove the LRG constraint at $z_{\text{eff}} = 0.51$. Doing so, we expect the Ω_m value to decrease, and it does to $\Omega_m = 0.287^{+0.016}_{-0.015}$ with an MLE of $\Omega_m = 0.286$. Overall, the shift downwards is not pronounced, and the error inflates, but this increases the tension with DES to $\sim 2.8\sigma$. Evidently, the working assumption that Ω_m is a constant in the Λ CDM Universe is under pressure at close to 3σ . This needs to be put in context. Given H_0 tension, a problem in background cosmology,⁴ and $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$ tension, a seemingly perturbative

problem, it is important to recognise that both these problems can be related provided we find a discrepancy in Ω_m [6]. The reason being that H_0 is correlated with Ω_m at the background level in the late Universe and S_8 clearly depends on Ω_m . If Ω_m is not a constant in the Λ CDM model, then H_0 and S_8 tensions are symptoms of the same underlying problem.

B. A second look

In this section we adopt complementary methodology following [17]. This provides an independent check on the results from anisotropic BAO in Table I. The basic idea is to employ the fact that the ratio

$$\frac{D_M/r_d}{D_H/r_d} = E(z) \int_0^z \frac{1}{E(z')} dz', \quad (2)$$

only depends on Ω_m in the Λ CDM model for which $E(z) = \sqrt{1 - \Omega_m + \Omega_m(1+z)^3}$.

Eq. (2) allows one to numerically solve for Ω_m .⁵ To incorporate the errors, one employs the 68% confidence intervals and the correlation r to construct a 2×2 covariance matrix for each effective redshift. From the covariance matrix, one randomly generates a large number (approx. 10,000) of $(D_M/r_d, D_H/r_d)$ pairs in a multivariate normal distribution. For each pair $(D_M/r_d, D_H/r_d)$, one solves the right hand side of (2) for Ω_m . This builds up a distribution of Ω_m values from which one extracts the mean and the 68% confidence intervals in Table III. More precisely, we determine the 68% confidence interval by identifying the 15.9 and 84.1 percentiles. Throughout we assume that the Ω_m distribution is Gaussian, but as is evident from the errors in Table III, and Fig. 2, this is not a bad approximation⁶. The main take-away is that Table I and Table III show excellent agreement in central values and errors. From the outset, this may not have been expected as (2) removes all dependence on $H_0 r_d$, so one is only constraining Ω_m . Smaller errors may have been expected, but this was not the case.

tracer	z_{eff}	Ω_m
LRG	0.51	$0.652^{+0.212}_{-0.169}$
LRG	0.71	$0.210^{+0.082}_{-0.068}$
LRG+ELG	0.93	$0.268^{+0.052}_{-0.045}$
ELG	1.32	$0.330^{+0.101}_{-0.076}$
Lyman- α QSO	2.33	$0.362^{+0.084}_{-0.066}$

TABLE III. 68% Ω_m confidence intervals from DESI anisotropic BAO constraints at effective redshift z_{eff} using Eq. (2).

⁵We check solutions to a precision of 10^{-10} by reinserting the solution in (2).

⁶In principle, for non-Gaussian posteriors one may fit a different distribution and this has a bearing on the errors [58]. Here we expect any difference to be small.

⁴ $H_0 = H(z=0)$ is determined by extrapolating the Hubble parameter, itself a solution to the Einstein equations, from low redshifts to $z=0$.

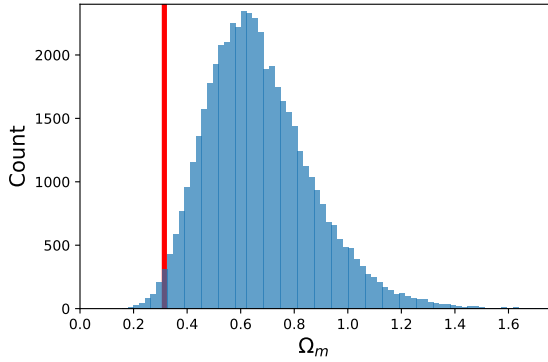


FIG. 2. Distribution of 50,000 Ω_m values at $z_{\text{eff}} = 0.51$ alongside Planck constraints $\Omega_m = 0.315 \pm 0.007$ in red. The probability of finding an Ω_m value within the Planck 1σ confidence interval or lower is $p = 0.015$ corresponding to 2.2σ .

Using Eq. (2) we revisit the anomaly in LRG data evident in Fig. 2. We increase the number of configurations to 50,000, where we find a probability of $p = 0.0147$ of getting a value lower than $\Omega_m = 0.322$, the upper bound on the Planck 68% confidence intervals. This places the disagreement in Ω_m at no less than 2.2σ .

III. w_0w_a CDM MODEL

From Fig. 1 and Fig. 2 it is clear that LRG data at $z_{\text{eff}} = 0.51$ disagrees with the Planck- Λ CDM model at the $\geq 2\sigma$ level. Moreover, as explained earlier, this constraint on Ω_m also disagrees with Pantheon+ [13] at the $\sim 2\sigma$ level, despite Type Ia SNe being most sensitive to comparable redshift ranges. As emphasised, this disagreement between DESI and Pantheon+ SNe, and more generally any SNe data set, since all closely agree on $\Omega_m \sim 0.3$ at lower redshifts, warrants further exploration. That point aside, while DESI constraints on the w CDM model from Table 3 of [9] are consistent with a cosmological constant interpretation ($w = -1$) within 1σ , fits of the w_0w_a CDM model leads to a different conclusion that $w = w_0 > -1$ is preferred at in excess of 2σ . This overestimates the significance as the w_a parameter is poorly constrained and this necessitates combining DESI with CMB and SNe.

We demonstrate here that this deviation from Λ CDM is driven by LRG data at $z_{\text{eff}} = 0.51$. This is acknowledged in the DESI paper [9], so our goal here is to provide independent confirmation. We employ MCMC with uniform DESI priors, $w_0 \in [-3, 1]$, $w_a \in [-3, 2]$ and $w_0 + w_a < 0$. The key point is that if data prefers the w_0w_a CDM model over Λ CDM, then changes in the Λ CDM parameters with effective (or binned) redshift must be evident in the Λ CDM model. In Fig. 3 we confirm that removing the most striking deviation from Planck- Λ CDM behaviour in Fig. 1 returns w_0 to $w_0 \sim -1$. We remark that one can clearly see the effect of DESI priors, especially the w_a and $w_0 + w_a$ priors, on confi-

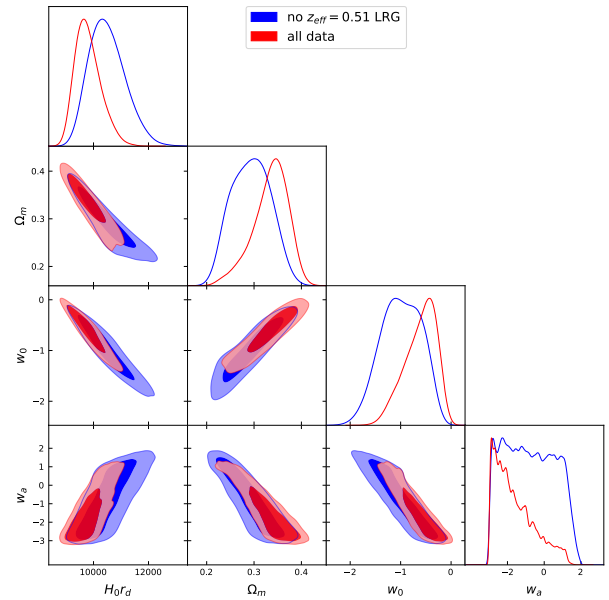


FIG. 3. w_0w_a CDM model with and without LRG data at $z_{\text{eff}} = 0.51$. Any hint of dynamical DE, in particular $w_0 > -1$, in DESI data is driven by LRG data. We acknowledge use of *GetDist* [59].

dence intervals in the (w_0, w_a) -plane; w_a is poorly constrained without external data.

Concretely, we find $w_0 = -0.560^{+0.266}_{-0.384}$ with the anomalous LRG data and $w_0 = -0.984^{+0.427}_{-0.422}$ without. Evidently, w_a is pushed to large negative values that are beyond the priors to accommodate $w_0 > -1$. This comes as no surprise, since neglecting the LRG data, DESI shows excellent agreement with Planck- Λ CDM. One concludes that any hint of dynamical DE in DESI data is driven by the LRG data. Moreover, one also concludes that the strong significances for dynamical DE quoted in the DESI paper when DESI is combined with CMB and SNe, rest at least in part on an inconsistency between BAO and SNe at lower redshifts, $z_{\text{eff}} \sim 0.5$. Without understanding the origin of this disagreement, claims of dynamical DE are premature.

IV. DISCUSSION

With its own data DESI has reported hints [9] of a preference for an evolving DE equation of state in the w_0w_a CDM model. As explained in the original paper, and confirmed here in Fig. 1 and Fig. 3, the preference for $w_0 > -1$ can be traced to the LRG data with $z_{\text{eff}} = 0.51$. While the tension with Planck- Λ CDM is only at the $\sim 2\sigma$ level, translated into familiar Λ CDM parameters, DESI LRG data at $z_{\text{eff}} = 0.51$ favours a $\Omega_m \sim 0.65$ best fit. This places DESI LRG constraints at odds not only with Planck, but also with multiple type Ia SNe samples [13–15], where it should be stressed that the effective redshift is not dissimilar; SNe samples are typically biased to lower redshifts. Given that SDSS and DESI constraints agree [9], it should come as no surprise that SDSS also prefers larger

Ω_m in the same range [17] (see Fig. 5), but admittedly not quite as large. Thus, it may be hard to argue that $\Omega_m \sim 0.65$ at $z_{\text{eff}} = 0.51$ is a statistical fluctuation in the data.

Arguably the great success of the Λ CDM model is that CMB, BAO and SNe agree that the Universe is 70% dark energy, $\Omega_m \sim 0.3$. In cosmology, physics must be supported by multiple observables, otherwise one is looking at statistical fluctuations or observational systematics, here either in LRG constraints at $z_{\text{eff}} = 0.51$ or in 3 SNe samples.⁷ This is the main take-away message from this letter. Of course, one can draw comparisons in the behaviour of the $w_0 w_a$ CDM model, but care is required to make sure one is seeing consistent deviations from Λ CDM in independent observables in the same redshift ranges, otherwise claims of new physics are not compelling, no matter what interest is generated [60–65].

As is evident from Table II, even in DESI data confronted to the Λ CDM model, shifts of $\sim 2\sigma$ are evident in Ω_m as the data is binned. Concretely, Ω_m decreases with effective redshift before increasing again. $H_0 r_d$ is anti-correlated with Ω_m , so it increases and decreases again. Historically, type Ia SNe samples have shown similar trends [66, 67], but this is not overly surprising given that large SNe samples are typically compiled from different surveys. As the number of surveys grows, observational systematics become a greater concern. Nevertheless, in recent years, the Pantheon+ sample has been demonstrated to largely return consistent Ω_m values [13], provided one neglects high redshift SNe [29]. In the case of DESI, one is looking at a single survey, but multiple tracers.

The big picture here is that persistent Λ CDM tensions, most notably discrepancies in H_0 and $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$ [1–3], assuming they are physical in origin, demand that the Λ CDM model breaks down through cosmological (fitting) parameters that change with effective redshift [4, 5].⁸ In support, observations of decreasing H_0 /increasing Ω_m values with increasing

effective redshift have been reported in a host of observables [17, 19–23, 25–29, 33–37, 41]. If substantiated, these findings point to a breakdown of the Λ CDM model at the *background level* in the late Universe. Coincidentally, observations also exist to localise S_8 tension, an apparent problem *at the perturbative level*, to the late Universe, $z \lesssim 2$ [71–74]. See [6] for a review of the science case supporting redshift evolution of Λ CDM parameters.

The situation is finely balanced. DESI has started data releases and constraints are expected to improve in coming years [57]. If the anomaly in LRG data at $z_{\text{eff}} = 0.51$ persists, then BAO and CMB+SNe, and potentially even CMB and SNe [15], are at odds on Ω_m . On the flip side, if improved data quality decreases the tension with Planck, Pantheon+ etc, it is plausible that the decreasing Ω_m /increasing $H_0 r_d$ trend at lower redshifts disappears leaving an increasing Ω_m /decreasing H_0 that is seen elsewhere.

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⁷These samples are not fully independent, so it is not implausible that systematics persist in SNe. Pantheon+ and Union3 share ~ 1360 SNe, while Pantheon+ and DES share 196 SNe.

⁸One could argue that S_8 is a scale problem, e. g. [68, 69], but this cannot resolve the statistically more significant H_0 tension problem. Moreover, shifts in S_8 due to changes in scale appear too small to resolve S_8 tension [70].

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