Exceptionally High Two-Photon Absorption in Diazaacene-Bithiophene Derivatives: A Combined Experimental and Theoretical Approach

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Abstract

This study delves into the enhancement of two-photon absorption (2PA) properties in diazaacene-bithiophene derivatives through a synergistic approach combining theoretical analysis and experimental validation. By investigating the structural modifications and their impact on 2PA cross sections, we identify key factors that significantly influence the 2PA efficiency. For all molecular systems studied, our state-of-the-art quantum chemical calculations show a very high involvement of the first excited singlet state (S₁) in the 2PA processes into higher excited states, even if this state itself has only a small 2PA cross section for symmetry reasons. Consequently, both the oscillator strength of S₁ and the transition dipole moments between S₁ and other excited states are of importance, underscoring the role of electronic polarizability in facilitating effective two-photon interactions. The investigated compounds exhibit large 2PA cross sections over a wide near-infrared spectral range reaching giant values of $\sigma_{2,\text{max}} = 42000$ GM. The introduction of diazine and diazacene moieties into bithiophene derivatives not only induces charge transfer but also opens up pathways for the creation of materials with tailored nonlinear optical responses, suggesting potential applications in nonlinear optics.

Introduction

Two-photon absorption (2PA) represents a cornerstone in the field of nonlinear optics, characterized by the simultaneous absorption of two photons by a molecule to transition into an excited state. This phenomenon stands in contrast to linear one-photon absorption (1PA), offering unique advantages. The nonlinear nature not only enables heightened spatial selectivity, occurring at the focal point with sufficient photon flux, but also ensures tightly confined spatial excitation due to its quadratic dependence on light intensity. Moreover, 2PA's utilization of longer wavelengths for excitation, specifically in the near-infrared (NIR) spectral range, allows for deeper penetration into biological tissues without significant scattering or absorption. Those advantages are particularly beneficial in high-resolution microscopy and bioimaging,¹⁻⁴ allowing for detailed visualization of biological processes with minimal background noise and reduced tissue damage. Additionally the precise delivery of energy gives rise to applications in various areas such as nanofabrication processes,⁵ targeted photodynamic therapy⁶ and advanced optical data storage solutions⁷ that are unattainable through conventional optical techniques.

Aiming at applications in photonics, a great effort has been put into synthesizing materials with high two-photon absorption cross sections (σ_2) as well as understanding the relationship between the molecular structure and the nonlinear optical processes. In this context, our study focuses on the enhancement of 2PA properties within organic molecules, particularly targeting the diradicaloid diazaacene-bithiophene derivatives⁸ (see Fig. 1) that have recently been found to exhibit high nonlinear responses.⁹



Figure 1: Molecules under investigation and their nomenclature: a) Bithiophene (BT) in *trans-* and *cis-*configuration, b) Diazine Bithiophene (DA-BT), and c) Diazaacene Bithiophenes with different acene length from n=0 (DAA-BT) over n=1 (DAT-BT) to n=2 (DAP-BT).

The bithiophene (BT) core is part of a series of heteroquaterphenoquinones, which have demonstrated promising properties in previous studies.¹⁰ In particular, the sulfur derivative exhibited an intense absorption band in the near-infrared region, suggesting its potential utility in high-density optical storage materials for diode lasers and other applications. Another significant aspect of our investigation is the incorporation of N-heteropolycyclic aromatic compounds. This modification not only serves as an efficient electron acceptor but also facilitates the tuning of the electronic structure of the molecules. The presence of nitrogen in the aromatic backbone introduces a push-pull electronic effect, significantly influencing the 2PA cross sections by enhancing the polarizability and electronic responsiveness of the molecule. Our approach combines both quantum chemical analyses and experimental methodologies to shed light on the factors that govern the 2PA characteristics of these molecules, with the ultimate goal of optimizing their performance for NIR-2PA applications.

Our experimental investigations reveal that the 2PA cross sections of these molecular systems rank among the highest reported for organic compounds, underscoring their potential in applications requiring high 2PA efficiency.^{11,12} Concurrently, our theoretical studies provide a deeper understanding of the 2PA mechanisms in the diazaacene-bithiophene derivatives, employing a sum-over-states (SOS) approach to elucidate the underlying principles. If two photons with the same energy $\left(\frac{\omega_f}{2}\right)$ are absorbed, the so-called SOS expression for a component of the 2PA transition moment between the ground state and the final state freads

$$S_{AB}^{f} = \sum_{n \neq 0} \left(\frac{\langle 0|\mu_{A}|n\rangle \langle n|\overline{\mu}_{B}|f\rangle}{\omega_{n} - \frac{\omega_{f}}{2}} + \frac{\langle 0|\mu_{B}|n\rangle \langle n|\overline{\mu}_{A}|f\rangle}{\omega_{n} - \frac{\omega_{f}}{2}} \right).$$
(1)

Here, $A, B \in x, y, z$ denote the Cartesian components of the electric dipole operator $\vec{\mu}$. As can be seen from Eq. (1), several properties contribute to the 2PA cross sections: the transition dipole moments between ground state and excited states $(\langle 0|\vec{\mu}|n\rangle)$, the transition dipole moments between final state and other excited states (for $n \neq f$: $\langle n|\vec{\mu}|f\rangle$) and the difference dipole moment between the ground state and the final state (for n = f: $\langle f|\vec{\mu}|f\rangle$) as well as the difference between the excitation energies and the energy of the incident photons $(\omega_n - \frac{\omega_f}{2})$. These considerations will make it possible to investigate the excited states involved in the 2PA processes more closely in the following.

Results and discussion

The 2PA cross sections were determined by the so-called Z-scan method (see Experimental Section). In addition, they were calculated at the time-dependent density functional theory (TDDFT) level using the SOS approach (see Computational Methodology). The most notable characteristic of all two-photon spectra of the molecular systems (see Fig. 1) in benzene is the presence of two distinct bands at $\approx 1.6 \text{ eV}$ ("low-energy band") and at > 2.6 eV ("high-energy band"), as summarized in Table 2. The measured Z-scan traces in the higher energy domain exhibit an overlap of a concave curve with a convex one, suggesting the simultaneous occurrence of 2PA and saturable absorption (SA) - as further elaborated in the Supplementary Information. This overlap complicates the identification and determination of the exact maximum position of the 2PA band, given the nonlinear competing effect of SA. Consequently, in Table 2, the energy values for the high-energy transition carry a minimum estimation uncertainty.

	Low-energy band		High-en	High-energy band	
	$E_{\mathbf{a}}{}^{a}$	$\lambda_{ m a}^{(1)}$	$E_{\rm b}{}^a$	$\lambda_{ m b}^{(1)}$	
BT	$1.83\mathrm{eV}$	$678\mathrm{nm}$			
DA-BT	$1.75\mathrm{eV}$	$708\mathrm{nm}$	$2.57\mathrm{eV}$	$482\mathrm{nm}$	
DAA-BT	$1.72\mathrm{eV}$	$721\mathrm{nm}$	$3.12\mathrm{eV}$	$7200\mathrm{nm}$	
DAT-BT	$1.71\mathrm{eV}$	$725\mathrm{nm}$	$2.89\mathrm{eV}$	$14900\mathrm{nm}$	
DAP-BT	$1.72\mathrm{eV}$	$725\mathrm{nm}$	$2.57\mathrm{eV}$	$19900\mathrm{nm}$	

Table 1: Absorption maximum of the one-photon excitation for the investigated systems in benzene. For all compounds, the maximum linear absorption lays in the low-energy band.

 $\overline{{}^{a}E_{a}}$ is the energy of the peak in the absorption band.

	Low-ene	ergy band	High-e	High-energy band		
	E_{\max}^{a}	$\sigma_{2,\max}$	E_{\max}^{a}	$\sigma_{2,\mathrm{max}}$		
BT	$0.86\mathrm{eV}$	$5500\mathrm{GM}$	$1.46\mathrm{eV}$	$42000\mathrm{GM}$		
DA-BT	$0.93\mathrm{eV}$	$900\mathrm{GM}$	$1.32\mathrm{eV}$	$6800\mathrm{GM}$		
DAA-BT	$0.77\mathrm{eV}$	$1300{\rm GM}$	$1.31\mathrm{eV}$	$7200\mathrm{GM}$		
			$1.43\mathrm{eV}$	$14800\mathrm{GM}$		
DAT-BT	$0.85\mathrm{eV}$	$1650{\rm GM}$	$1.33\mathrm{eV}$	$14900\mathrm{GM}$		
DAP-BT	$0.78\mathrm{eV}$	$6900{\rm GM}$	$1.30\mathrm{eV}$	$19900\mathrm{GM}$		

Table 2: Measured 2PA parameters for the investigated systems in benzene.

 ${}^{a}E_{\max} = \frac{hc}{\lambda_{\min}}$ is the energy of the incident photons.

2PA Properties of BT BT is the core component of the DA-BT derivatives.⁸ As shown by Takahashi et al., BT (heteroquaterphenoquinone) exists predominantly as the *trans*-isomer in solution.¹⁰ This will result in a centrosymmetric system. Notably, it is well-established that the selection rules governing one-photon absorption and two-photon absorption are mutually exclusive for centrosymmetric molecules such as BT. Thus, for symmetry reasons, a state that is bright in the 1PA spectrum must be dark in the 2PA spectrum. In the experimental UV-vis data depicted in Figure 2, a distinct 1PA band is observed at 1.66 eV (1.82 eV and 2.01 eV). This peak corresponds to an excitation into the first excited singlet state and is faithfully reproduced in the calculated spectrum, albeit with a slight blueshift of about $0.2 \,\mathrm{eV}$. The shoulders can be attributed to vibronic contributions and are therefore not present in the calculated spectrum, since only electronic contributions were taken into account. Despite the inversion symmetry, this first excitation is not completely dark in the experimental 2PA spectrum, which is due to several factors: the presence of both *trans*- and *cis*-configurations of BT in the measured solution (see Figure S1 (SI)) as well as vibrational distortions that relax the selection rules. When examining the higher energy regime, the situation is exactly the opposite: there is no band in the linear absorption spectrum, but an extremely high peak in the 2PA spectrum, which can be assigned to the second excited state. In the experiment, this transition appears at a photon energy of 1.45 eV, consistent with the calculated spectrum at 1.48 eV. This high-energy peak reaches $\sigma_2 = 42000$ GM, which documents a giant 2PA



Figure 2: Experimental and theoretical analysis of the 1PA and 2PA characteristics of BT in benzene.

cross section compared to organic molecules of similar size.^{11,12} The BT unit has a large acceptor– π –donor– π –acceptor (A– π –D– π –A)-type structure as illustrated in Figure 3 a. The resulting quadrupolar structure typically involves a central donor (D) moiety flanked by π -conjugated linkers and terminal acceptor (A) groups. It has been demonstrated that conjugated molecules, when substituted with donor or acceptor groups in an essentially centrosymmetric pattern, exhibit significantly enhanced two-photon cross sections, often surpassing the corresponding unsubstituted molecules by at least an order of magnitude.^{13–16}



Figure 3: The BT geometry offers a quadrupolar A- π -D- π -A configuration in a). b) The additional azaacene moiety gives rise to additional electron withdrawing.

Figure 2 shows that the calculations at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory not only reproduce the shape of the experimental 1PA spectrum very well, but also that of the experimental 2PA spectrum. According to Beerepoot et al.,¹⁷ range-separated functionals such as CAM-B3LYP are well suited to correctly predict qualitative trends of 2PA strengths, even if the underestimation of excited-state dipole moments as well as the overestimation of excitation energies leads to a tendency for the absolute values to be too low, albeit in a rather systematic way. In order to gain a deeper insight into the 2PA processes of the BT molecule and thus explain the extraordinarily high 2PA cross section of the second excited state, the individual contributions of the SOS expression must be investigated. For this purpose, the calculated molecular properties relevant for this study are summarized in Table 3. Resonance effects can still be ruled out in the energy range under consideration, which is why the excitation energy ω_f is of rather minor importance in this analysis. Since the states with the large σ_2 themselves have an oscillator strength close to zero, the terms for n = f in the sum in Eq. (1) cannot make a large contribution, and therefore the difference dipole moments of the excited states do not play a major role either. However, the particularly bright first excited state of the BT molecule in the UVvis spectrum in Figure 2 is striking. Consequently, those excited states that have a large transition dipole moment with the first excited state should also have a large 2PA transition moment, since the term for n = 1 then has a particularly high contribution in the sum in Eq. (1), which is confirmed by Table 3. This is especially true if $\langle 0|\vec{\mu}|1\rangle$ and $\langle 1|\vec{\mu}|f\rangle$ are aligned,¹⁸ which is the case here for the second excited state (see Figure 4). The high σ_2 of S_2 thus results from the strongly allowed one-photon transition into S_1 in combination with the strong coupling of the first two excited states with each other. Looking at the attachment/detachment densities of the first and second excited states in Figure 5, their great similarity is also noticeable.

Table 3: Excitation energies (ω_f) , oscillator strengths (f_L) , 2PA cross sections (σ_2) , transition dipole moments from the ground state, difference dipole moments, and state-to-state transition moments for the first 5 excited singlet states of BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory.

f	$\omega_f \; [eV]$	f_L [a.u.]	$\sigma_2 \; [GM]$	$ \left<0 \vec{\mu} f\right> $ [a.u.]	$ \langle f \vec{\overline{\mu}} f \rangle $ [a.u.]	$ \langle 1 \vec{\mu} f\rangle $ [a.u.]
1	1.99	3.568	0	8.560	0.000	-
2	2.96	0.000	49211	0.000	0.000	7.839
3	3.10	0.000	0	0.003	0.093	0.007
4	3.10	0.000	0	0.007	0.093	0.011
5	3.46	0.000	6163	0.001	0.005	1.240



Figure 4: Visualization of $\langle 0|\vec{\mu}|1\rangle$ (green) and $\langle 1|\vec{\mu}|2\rangle$ (blue) transition dipole in BT.



Figure 5: Attachment/detachment densities in blue/red of the first two excited singlet states of BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory. The other excited states can be found in the Supplementary Information.

Modification with Diazine Moiety (DA-BT) Derivatization of the bithiophene with a diazine (DA) moiety, increases the planarity and eliminates the *trans*-configuration, leads to a C_{2v} symmetry. This modification introduces an additional dipolar push-pull unit from the electron-donating sulfur site to the newly added electron-withdrawing diazin (see Fig. 3b). Both the 1PA and 2PA spectra (see Figure 6) display similar behavior compared to BT, the peaks are only slightly red-shifted. Although the molecule has lost the center of symmetry, the first excited state, which still exhibits the largest one-photon transition strength in the UV-vis spectrum at 1.75 eV, has only a small 2PA cross section; the calculated σ_2 is almost negligible. In contrast, the two-photon transition into the second excited state, which occurs in the experimental spectrum at $1.32 \,\mathrm{eV}$ and in the theoretical data at $1.39 \,\mathrm{eV}$, is again significantly stronger. However, the calculated 2PA peak is much more pronounced than the measured one, indicating experimental limitations in extracting the full σ_2 due to the competing linear absorption, which already begins in this range as a result of vibrational broadening. However, also for DA-BT, the correlation between a high 2PA cross section and a large transition dipole moment between the first and final excited states is evident (see Supporting Information).



Figure 6: Measured and calculated 1PA and 2PA characteristics of DA-BT

Extension to Diazaacene Bithiophenes (DA(n)-BT) When the diazine is extended by further annulated benzene rings, a strong 2PA can still be observed despite the competing saturable absorption, which occurs at excitation energies of $E_{\text{exc}} = 1.30 \text{ eV}$ and above (see Figure 7). For DAA-BT, there is a double peak structure with $\sigma_2(E_{exc} = 1.31 \text{ eV}) =$ 7250 GM separated by SA from a second maximum with $\sigma_2(E_{exc} = 1.43 \text{ eV}) = 14800 \text{ GM}$. Further modification by extending the acene length in diazaacene-bithiophene (DA(n)-BT) results in tuning of the 2PA band position. Increasing the acene length from n=0 to n=2 leads to an uneffected magnitude of σ_2 in the higher energy region and an increase in two-photon absorption in the lower energy region, highlighting the versatility of structural modifications in optimizing photophysical properties. For the detailed analysis the data of the DAT-BT



Figure 7: 1PA and 2PA measurements and calculations of DA(n)-BT with increasing length (n=0-2).

will be discussed, the corresponding data for the two other compounds can be found in the Supporting Information. If one compares the spectra in Figure 7 with the spectra in Figure 2, it is noticeable that the two "low-energy" and "high-energy" bands remain almost unchanged except for a red-shift, since the respective excitations are still localized at the BT unit and the acene has only a small influence, as can be seen from the attachment/detachment densities of S_1 and S_7 (see Figure 8). Compared to BT, however, there are additional low-lying



Figure 8: Attachment/detachment densities in blue/red of selected excited states of DAT-BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory.

excitations that also involve the acene moiety. The TDDFT calculations show that two new states emerge that are visible in both the 1PA and 2PA spectra. In both cases, these involve charge-transfer excitations that extend over the entire molecule: for S_2 from the BT unit to the acene unit and for S_3 vice versa (see Figure 8). Based on its position, one could assume at first glance that the enhanced absorption band between $0.75 \,\mathrm{eV}$ and $1.00 \,\mathrm{eV}$ in the experimental 2PA spectra (Figure 7) can be attributed to excitations into the first excited state. However, since these states are only about $0.1-0.3 \,\mathrm{eV}$ higher in energy than S_1 state (depending on the molecule, see Supporting Information), and according to the calculations have a significantly higher 2PA cross section, these are assigned to charge-transfer excitations. A slight shift in peak position between 1PA and 2PA spectra is common due to vibronic effects not accounted for in our calculations.¹⁹ In the case of DAP-BT, a σ_2 of up to 6900 GM can be measured as a result of this charge-transfer excitation. The calculated values are smaller, but a severe underestimation of absolute 2PA transition strengths by range-separated functionals is already known.^{17,20} It can also be observed that the 2PA cross section still correlates with the transition strength between the first excited state and the final state (see Supporting Information). For all states with significant σ_2 (S₂, S₃, and S_7 , $\langle 0|\vec{\mu}|1\rangle$ and $\langle 1|\vec{\mu}|f\rangle$ are aligned. However, since the molecule has no inversion center, the transition dipole moments between the ground state and the final states are no longer negligible, so that the terms for n = f and thus the excited-state dipole moments also have a contribution.

Conclusion

Our comprehensive study on the 2PA properties of bithiophene derivatives emphasizes the significant impact of structural modifications on their photophysical behavior. We have shown that extended $A-\pi-D-\pi-A$ compounds show large 2PA cross sections peaking at 42000 GM for BT. All molecules under investigation show a significant 2PA (over 100 GM) in a wide range of the low-energy band (0.75 – 0.95 eV). By introducing diazine and diazaanthracene moieties to the BT, we have demonstrated the ability to induce charge transfer, enhance 2PA properties, and tune the absorption band positions in the high-energy band (1.25–1.4 eV), offering promising avenues for the development of advanced materials for NIR-2PA applications. We thus have demonstrated that relatively small changes in molecular structure can lead to a large impact on the optical properties in this class of materials. The observed correlation not only enhances our understanding of the underlying mechanisms governing 2PA but also provides a valuable framework for the design and development of materials with optimized nonlinear optical properties.

Experimental Methods

Two-Photon Absorption Measurements

Sample Preparation

The two-photon absorption (2PA) measurements were conducted on solutions containing the derivatives of interest. These derivatives were dissolved in benzene to reach a concentration of 1.7 mM (for BT), 2 mM (for DA-f-BT) and 1 mM (for DA(n)-f-BT), all under a nitrogen atmosphere to avoid reduction reactions that might alter sample's properties. The prepared solutions were then placed into 2 mm path length Infrasil cuvettes (Starna 1/ST/C/I/2) to

ensure accurate and consistent path length for the measurements.

Open-Aperture Z-Scan Technique

The 2PA properties of the solutions were assessed using the open-aperture Z-scan technique, a reliable method for determining nonlinear absorption characteristics.²¹ A picosecond Nd:YAG laser (Ekspla PL2230) operating at a 50 Hz repetition rate was utilized, ensuring complete thermal relaxation between pulses. To cover a broad spectral range in the nearinfrared region, the laser beam was modified using a harmonic generator and a parametric generator, achieving a narrow pulse width ($\lambda_p = 3.7$ nm). The laser pulses, characterized by a Gaussian temporal profile with a full width at half maximum (FWHM) of 18 ps, were spatially reshaped using a Gaussian filter. The transmittance *T* for each pulse and z-stage position was recorded by comparing the pulse energy after and before propagation through the sample, using a pyroelectric energy meter (Ophir Optronics PE9-C) for pulse energy measurements.

Analysis

The analysis of the open-aperture Z-scan traces focused on the absence of beam distortion, indicating that the transmittance changes were solely due to nonlinear absorption. For a temporally Gaussian pulse, the normalized transmitted energy as a function of sample position z is given by:²²

$$T(z) = \frac{1}{\sqrt{\pi q_0(z,0)}} \int_{-\infty}^{\infty} \ln\left[1 + q_0(z,0)e^{-t^2}\right] dt,$$
(2)

where $q_0(z,t) = \beta I_0 L_{\text{eff}}/(1+x^2)$, and $x = z/z_0$ with z_0 being the Rayleigh length, β the nonlinear absorption coefficient, I_0 the maximum irradiance, and L_{eff} the effective sample length. For $|q_0| < 1$, this equation can be simplified to a summation suitable for numerical evaluation:

$$T(z) = \sum_{m=0}^{\infty} \left[\frac{-q_0(z,0)}{(m+1)^{3/2}} \right].$$
(3)

Curve fitting of the Z-scan traces was performed using this equation. The 2PA cross section σ_2 was then calculated using the formula:

$$\sigma_2 = \frac{h\nu\beta}{N_A d},\tag{4}$$

where N_A is Avogadro's constant, $h\nu$ the photon energy, β the two-photon absorption coefficient, and d the concentration. The 2PA cross section is reported in Göppert–Mayer (GM) unit (1 GM = 10^{-50} cm⁴ s molecule⁻¹ photon⁻¹) and was evaluated for every measured excitation wavelength. Measurements at the same wavelength but different input peak irradiances have been performed to exclude multiphoton effects and to verify the nonlinear correction through the fitted beta.

Computational Methodology

Computational Details

All quantum chemical calculations were carried out using a development version of the Q-Chem 6.0 program package.²³ For geometry optimizations, frequency and excited-state calculations, the conductor-like polarizable continuum model (C-PCM) was used to simulate the solvation effects of benzene ($\epsilon = 2.3$).²⁴ The geometries of the investigated systems were optimized at the B3LYP-D3(BJ)/6-31G* level of theory. It should be noted that *t*-Bu and TIPS groups were replaced by Me and TMS groups, respectively. Frequency calculations at the same level of theory confirmed in each case that the stationary point is a local minimum. Using the range-separated hybrid exchange-correlation functional CAM-B3LYP²⁵ with Grimme's D3(BJ) dispersion correction^{26,27} and aug-cc-pVDZ as the basis set,²⁸ the 100 lowest excited singlet states were computed within the Tamm-Dancoff approximation (TDA),²⁹ including the transition moments between excited states and excited-state dipole moments. In order to analyze the electronic structure of the most important states involved in the 2PA processes, attachment and detachment densities were also calculated.

Analysis

The UV-vis spectra were generated by convolving the computed stick spectra with Gaussian functions. The 2PA spectra were obtained from the calculated properties by applying a few-state model. For this purpose, the sum in Eq. (1) was formed over the first 100 excited singlet states. Since the denominator in Eq. (1) becomes larger with increasing energetic distance between the final state and the other excited states and the corresponding contributions thus become progressively smaller, this approximation is justified. For linearly polarized light with parallel polarization, the rotationally averaged 2PA strength (in atomic units) can be calculated from the obtained tensor as

$$\langle \delta^{2PA} \rangle = \frac{1}{15} \sum_{AB} (2S_{AB}S_{AB} + S_{AA}S_{BB}). \tag{5}$$

According to Ref. 20, the macroscopic 2PA cross section (in cgs units), which is compared with the experiment, can then be determined as follows

$$\sigma_2 = \frac{4\pi^3 \alpha a_0^5 \omega^2}{c} \langle \delta^{TPA} \rangle g(2\omega, \omega_f, \Gamma), \tag{6}$$

where α is the fine structure constant, a_0 the Bohr radius, ω the photon energy in atomic units, c the speed of light, and $g(2\omega, \omega_f, \Gamma)$ the lineshape function that describes spectral broadening effects. In our case, a Gaussian lineshape function

$$G(2\omega) = \frac{\sqrt{ln2}}{\Gamma\sqrt{\pi}} exp\left[-ln2\left(\frac{2\omega-\omega_f}{\Gamma}\right)^2\right]$$
(7)

was used again. Here, ω_f denotes the excitation energy of the final state f and Γ the half width at half maximum (HWHM). In accordance with the experiment, a HWHM (= $\frac{1}{2} \times FWHM$) of 0.1 eV was used throughout.

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Supporting Information Available

Concentration dependent 2PA measurements, z-scan traces of BT, reversed saturable absorption data, calculated excited-state properties and attachment/detachment densities

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Supplementary Material



Concentration Dependent 2PA Measurements

Figure S1: In a) one can see the 2PA spectra measured for different concentrations of BT solutions. In b) the linear transmission of the beam for each solution is plotted.

Concentration-dependent measurements provide insights into the interplay between linear and nonlinear optical absorption. As depicted in Figure S2b, the onset of linear absorption is observed at approximately 1.4 eV. According to the Lambert-Beer law, solutions with higher concentrations exhibit absorption at lower photon energies compared to those with lower concentrations. Consequently, the nonlinear effect of saturable absorption (SA) is initiated as competing effect at an earlier stage in more concentrated solutions. Conversely, in solutions with lower concentrations, two-photon absorption can still be measured at higher energies. However, in lower concentrated solutions the effect of saturable absorption is more pronounced due to the reduced number of molecules, which leads to a more rapid onset of saturation. This dynamic results in a steeper decline in nonlinear absorption. The observed trend culminates in the predominance of reverse saturable absorption at higher photon energies, as shown in Figure S2 a). This behavior underscores the complex relationship between molecule concentration, linear absorption, and the competing nonlinear effects within the BT solutions.



Figure S2: Exemplary z-scan traces of BT. They show just 2PA, 2PA while already SA present and mainly SA.

Reversed Saturable Absorption

The dependence of NLO response of the bithiophene on the incident intensity in the high energy regime has been investigated by adopting a wide range of input intensities and can be seen in Fig. S3. It can be clearly seen that there are overlaying effects, where in the low intensity regime SA effects dominates. When the input peak intensity is increased, a valley in the the normalized transmittance.emerges at the focal point, indicating typical response for reversed saturable absorption (RSA). In this case the RSA is attributed to the large two photon absorption at this excitation energy. It is apparent that SA and nonlinear absorption coexist, with the shape of the trace as a result of competing nonlinear effects.



Figure S3: Z-san traces of BT with different input peak intensities at a fixed excitation energy (wavelength).

 $\label{eq:excited-State Properties and Attachment/Detachment Densities$

 \mathbf{BT}



Figure S4: Attachment/detachment densities in blue/red of the first 5 excited singlet states of BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory.

DA-BT

Table S1: Excitation energies, oscillator strengths, 2PA cross sections, transition moments from the ground state, difference dipole moments, and state-to-state transition moments for the first 8 excited singlet states of DA-BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory.

f	$\omega_f \; (\mathrm{ev})$	f_L (a.u.)	$\sigma_2 (GM)$	$ \left<0 \vec{\mu} f\right> $ (a.u.)	$ \langle f \vec{\overline{\mu}} f \rangle $ (a.u.)	$ \langle 1 \vec{\mu} f\rangle $ (a.u.)
1	1.86	3.495	46	8.758	1.124	-
2	2.77	0.003	35857	0.193	2.390	6.466
3	2.95	0.000	0	0.015	3.603	0.004
4	2.95	0.000	0	0.016	3.601	0.007
5	3.00	0.334	199	2.131	1.796	0.481
6	3.14	0.208	36783	1.647	2.987	3.557
7	3.33	0.067	7472	0.910	2.265	0.956
8	3.35	0.007	2942	0.284	1.057	0.957

DA(n)-BT

Table S2: Excitation energies, oscillator strengths, 2PA cross sections, transition moments from the ground state, difference dipole moments, and state-to-state transition moments for the first 8 excited singlet states of DA(n)-BT calculated at the CAM-B3LYP-D3(BJ)/aug-cc-pVDZ level of theory.

				DAA-BT				
f	$\omega_f \; (\mathrm{ev})$	f_L (a.u.)	$\sigma_2 (GM)$	$ \langle 0 \vec{\mu} f\rangle $ (a.u.)	$ \langle f \vec{\overline{\mu}} f \rangle $ (a.u.)	$ \langle 1 \vec{\mu} f\rangle $ (a.u.)		
1	1.88	3.249	39	8.392	1.084	-		
2	2.26	0.067	2011	1.099	7.526	3.161		
3	2.90	0.297	28751	2.043	3.831	5.205		
4	2.97	0.000	0	0.004	4.533	0.006		
5	2.97	0.000	0	0.004	4.533	0.009		
6	3.00	0.001	0	0.134	2.938	0.007		
7	3.08	0.012	204	0.401	2.176	0.542		
8	3.11	0.006	44351	0.284	3.870	4.575		
	DAT-BT							
f	ω_f (ev)	f_L (a.u.)	$\sigma_2 (GM)$	$ \langle 0 \vec{\mu} f\rangle $ (a.u.)	$ \langle f \vec{\overline{\mu}} f \rangle $ (a.u.)	$ \langle 1 \vec{\mu} f\rangle $ (a.u.)		
1	1.90	3.179	43	8.265	1.097	-		
2	2.12	0.084	1304	1.269	7.854	3.043		
3	2.44	0.307	971	2.265	9.881	1.677		
4	2.53	0.302	1	2.207	3.296	0.304		
5	2.99	0.000	0	0.008	4.762	0.014		
6	2.99	0.000	0	0.002	4.762	0.005		
7	3.04	0.111	69993	1.219	0.734	6.823		
8	3.16	0.311	371	2.003	2.885	0.566		
	DAP-BT							
f	$\omega_f \; (\mathrm{ev})$	f_L (a.u.)	$\sigma_2 (GM)$	$ \left<0 \vec{\mu} f\right> $ (a.u.)	$ \langle f \vec{\overline{\mu}} f \rangle $ (a.u.)	$ \langle 1 \vec{\mu} f\rangle $ (a.u.)		
1	1.90	2.853	49	7.827	0.972	-		
2	1.99	0.070	1002	1.198	8.014	2.694		
3	2.08	0.568	1	3.337	3.967	0.948		
4	2.15	0.396	600	2.743	10.916	0.796		
5	2.99	0.000	2	0.014	6.879	0.039		
6	2.99	0.000	0	0.005	6.874	0.015		
7	3.02	0.212	66066	1.690	0.866	6.867		
8	3.17	0.231	370	1.724	3.291	0.534		