

Supercontinua from integrated gallium nitride waveguides

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Supercontinua are broadband spectra that are essential to optical spectroscopy, sensing, imaging, and metrology. They are generated from ultrashort laser pulses through nonlinear frequency conversion in fibers, bulk media and chip-integrated waveguides. For any generating platform, balancing the oppositional criteria of strong nonlinearity, transparency, and absence of multiphoton absorption is a key challenge. Here, we explore supercontinuum generation in integrated gallium nitride (GaN) waveguides, which combine a high Kerr-nonlinearity, mid-infrared transparency and a large bandgap that prevents two- and three-photon absorption in the technologically important telecom C-band where compact erbium-based pump lasers exist. With such a laser, we demonstrate tunable dispersive waves and gap-free spectra extending to almost 4 μm in wavelength, relevant to functional group chemical sensing. In addition, also leveraging the material's second-order nonlinearity, we implement on-chip f - $2f$ interferometry to detect the pump laser's carrier-envelope offset frequency, which enables precision metrology. These results demonstrate the versatility of GaN-on-sapphire as a new platform for broadband nonlinear photonics.

1 Introduction

In supercontinuum generation, an ultrashort laser pulse creates a broadband spectrum via nonlinear optical processes [1, 2]. When the input pulses are periodic in time, the emerging spectrum can be a frequency comb, i.e., a coherent spectrum that is composed of discrete optical frequency components ν_m that are given by $\nu_m = f_{\text{ceo}} + m f_{\text{rep}}$, where f_{ceo} is the carrier-envelope offset frequency and f_{rep} is the repetition rate of the pulse train; m is an integer line index. Frequency combs and supercontinua underpin a wide range of applications in photonics including, for instance, optical spectroscopy of molecules, environmental monitoring, frequency synthesis, optical clocks, and medical imaging [3–6].

Complementing nonlinear fibers and bulk media, integrated nanophotonic waveguides have emerged as a powerful platform for supercontinuum generation [2]. Dielectric and semiconductor waveguide materials including silicon [7, 8], silicon-germanium [9], (aluminum) gallium arsenide [10–12], chalcogenides [13], silicon nitride [14], aluminum nitride [15], lithium niobate [16, 17], tantalum pentoxide [18, 19], tellurium oxide [20] and diamond [21] have enabled spectral broadening with sub-nJ pulse energies. Materials with higher nonlinearity are typically characterized by a small bandgap and are ideally pumped by long wavelength table-top laser systems, such as optical parametric oscillators, to avoid two- and three-photon absorption (2PA/3PA) and associated free-carrier-induced loss. In contrast, larger bandgap materials can be pumped at shorter near-infrared wavelength. This is illustrated for different materials in Fig. 1d where we also indicate the technologically important telecom C-band, where compact and robust erbium-based pump lasers are available. Large bandgap materials have therefore enabled compact setups for the generation of broadband supercontinua extending from near-infrared into ultraviolet [22–26] and mid-infrared domains [27–30].

An unexplored material for supercontinuum generation is GaN, a III-V direct bandgap semiconductor material widely used in electronics, lighting, lasers, photovoltaics, and photo-detectors [31–33]. GaN exhibits a third-order nonlinearity $\chi^{(3)}$ larger than that of widely-used silicon nitride and, like lithium niobate and aluminum nitride, offers a high second-order nonlinearity $\chi^{(2)}$ up to 20 pm/V [34]. Compared to other semiconductors, its large bandgap of 3.4 eV implies the absence of 2PA and 3PA in the telecom C-band around 1550 nm, so that erbium-based pump lasers can be employed. Previous work on GaN has already demonstrated waveguides with transparency at near-infrared and visible wavelengths [35–39], efficient second harmonic generation [36, 40], four-wave mixing [41] and microresonator solitons [42], hinting at significant potential for supercontinuum generation.

Here, we demonstrate for the first time the generation of broadband supercontinua in integrated GaN waveguides (Fig. 1a). The waveguides are fabricated via e-beam

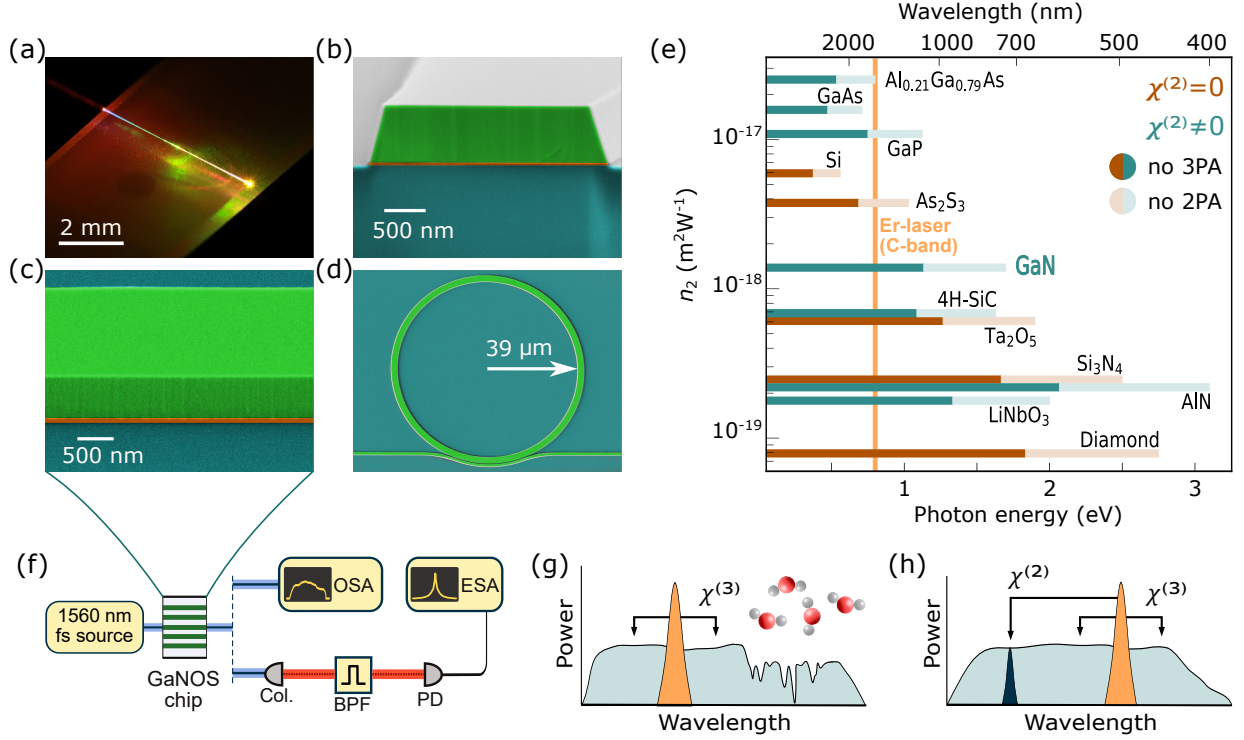


Figure 1 | (a) Photograph of a GaNOS chip pumped by a C-band femtosecond laser. (b)-(d) Colored scanning electron microscope (SEM) images of waveguide cross-section, waveguide sidewall, and microring resonator, respectively. Green marks GaN, orange marks AlN, and cyan marks sapphire. (e) Nonlinear refractive index n_2 of different materials. Horizontal bars mark the wavelength range free from 2PA (light color) and 3PA (dark color). Cyan and brown indicate the presence or absence of second-order nonlinearity, respectively. Refs: Diamond, LiNbO₃, AlN, Si₃N₄ and Si from [2]; Ta₂O₅ [18]; 4H-SiC [43]; GaN [42]; As₂S₃ [44]; GaP [45]; GaAs [46]; Al_{0.21}Ga_{0.79}As [11]. (f) Schematic setup. GaNOS: GaN-on-sapphire; OSA: optical spectrum analyzer; Col.: collimator; BPF: bandpass filter; PD: photodetector; ESA: electrical spectrum analyzer. (g) & (h) Illustration of molecular spectroscopy and f -2 f self-referencing with supercontinua.

lithography and reactive ion etching from commercially available GaN-on-sapphire (GaNOS) wafers. Both GaN and sapphire are transparent deep into the mid-infrared wavelength range beyond 6 μm. An off-the-shelf 100 MHz erbium-based mode-locked laser with a central wavelength of 1560 nm is used to pump the waveguides, resulting in the efficient generation of multi-octave spanning spectra. In tailored waveguides we demonstrate tunable dispersive wave generation and gap-free spectra extending into the mid-infrared to almost 4000 nm wavelength, ideally suited for chemical sensing and molecular spectroscopy (cf. Fig. 1g). Moreover, by simultaneously leveraging second- and third-order nonlinearities, we demonstrate chip-based detection of f_{ceo} for self-referencing and optical precision metrology (cf. Fig. 1h). These results show the potential of integrated GaN waveguides for broadband nonlinear photonics, and in particular, their ability to efficiently generate mid-infrared light from erbium-based lasers without suffering from multiphoton absorption and associated free-carrier-induced loss.

2 GaN waveguides

The GaN waveguides used in this work are fabricated from a commercially available, unintentionally n-doped, 725 nm thick wurtzite crystalline GaN layer, grown on a sapphire substrate with a 25 nm aluminum nitride buffer layer. The c-axis of the crystalline GaN is perpendicular to the wafer surface. In this crystal orientation, the transverse magnetic (TM) polarized modes experience the largest second-order nonlinear susceptibility $\chi_{33}^{(2)} = 10$ -20 pm/V [34]. The waveguides are defined via e-beam lithography with hydrogen silsesquioxane (HSQ) resist, followed by inductively-coupled plasma reactive ion etching with a chlorine/nitrogen mixture [47]. A complete etching through the GaN and aluminum nitride layers results in waveguides with a sidewall angle of 73°. Finally, the HSQ is removed by hydrofluoric acid, and the chips are cleaved to create the input and output coupling facets. Figure 1b shows a typical waveguide cross-section (after cleaving), and Fig. 1c provides a lateral view of the low sidewall roughness waveguides. Waveguides with two different lengths, 2 mm and 5 mm, are fabricated.

To measure the waveguide loss, we characterize a mi-

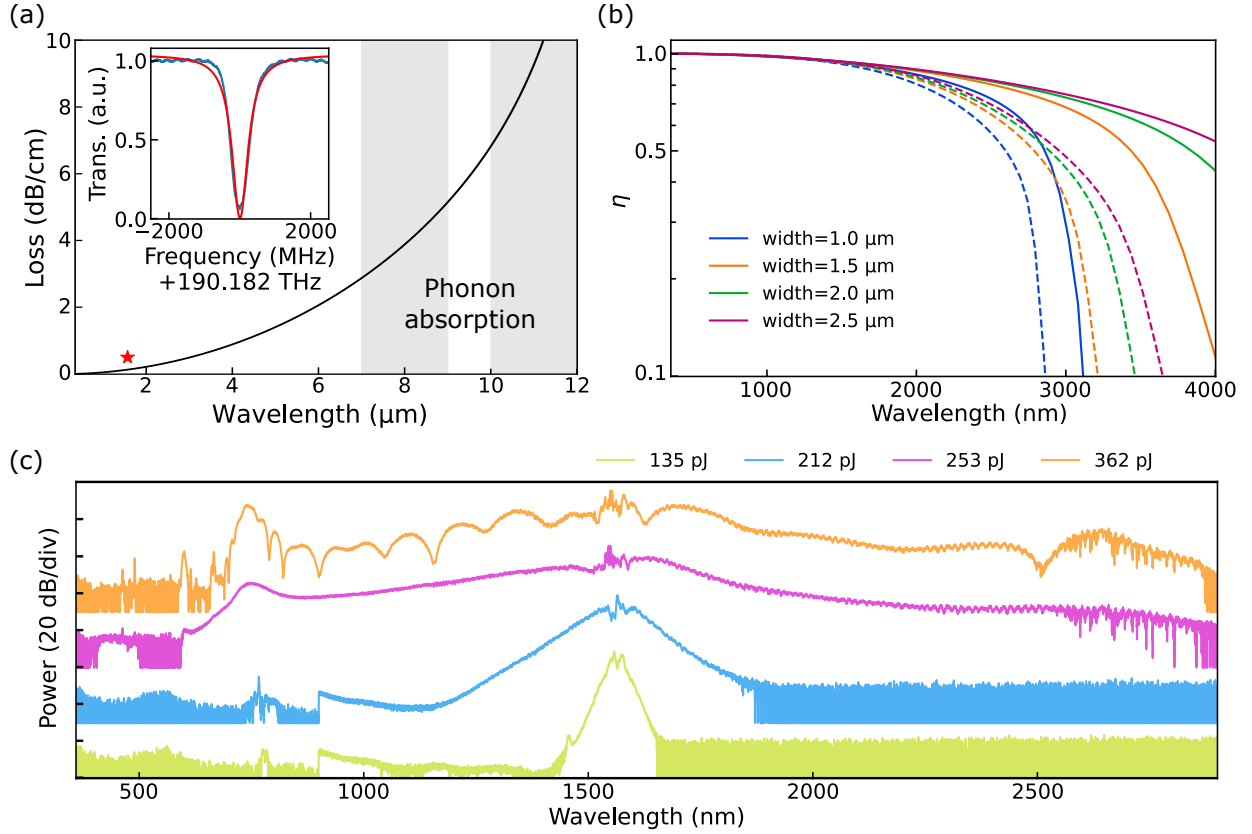


Figure 2 | (a) Estimated material loss versus wavelength with unintentionally doped GaN using the Drude model. Grey shaded areas indicate phonon absorption bands and the red star marks the propagation loss measured by a microring. Inset: resonance of the microring (blue) and Lorentzian fit (red). (b) Simulated mode confinement versus wavelength for different waveguide widths. Solid lines are fundamental TE modes, and dashed lines are fundamental TM modes. (c) Supercontinua obtained from a 2 mm long 2.5 μm wide waveguide (TM) with different on-chip pump pulse energies (for visibility the spectra are vertically offset by 30 dB).

croring resonator with a waveguide width of 2.5 μm and a ring radius of 39 μm (Fig. 1d). Under critical coupling, we observe a loaded Q-factor of 3.5×10^5 at the wavelength of 1576 nm (Fig. 2a, inset), corresponding to a waveguide propagation loss of 0.53 dB/cm. In semiconductor materials, a significant contribution to the propagation loss can arise from free-carriers. In a Drude-model [48] these losses scale with λ^2 , where λ is the wavelength. As Hall effect measurements reveal, the unintentional n-doping in our samples leads to a free-carrier concentration of $2.1 \times 10^{16} \text{ cm}^{-3}$. Based on this measurement and assuming an electron mobility of $800 \text{ cm}^2/\text{V}$ [49], we can estimate the wavelength-dependent contribution of the unintentional n-doping to the propagation loss. At a wavelength of 1576 nm, we find the free-carrier contribution to the loss to be 0.14 dB/cm. As indicated in Fig. 2a, this is consistent with the microring measurement, which includes other loss mechanisms, such as scattering. While the unintentional n-doping should negligibly affect the waveguide losses at shorter wavelengths (as long as direct absorption in GaN, 2PA, and 3PA can be neglected), an increasing impact towards longer wavelengths is expected based on the Drude model, approaching 3 dB/cm at 7 μm. For even longer wavelengths, first and second harmonic

phonon absorption bands (see absorption regions shaded in gray in Fig. 2a) [50, 51] would likely become the predominant source of loss. Moreover, beyond a wavelength of $\sim 6 \mu\text{m}$, losses in the sapphire substrate can no longer be neglected.

In addition to low loss propagation, tight mode confinement in the waveguide core is critical to enable efficient and broadband supercontinuum generation. To characterize the wavelength- and polarization-dependent mode confinement, we perform numerical simulations based on a finite element model (FEM). The model includes previously obtained material data of GaN [54] while the refractive index of sapphire and aluminum nitride are measured by ellipsometry. Figure 2b shows the mode-confinement defined by

$$\eta = \frac{\iint_{\text{GaN}} I(x, y) dx dy}{\iint_{\text{all}} I(x, y) dx dy}, \quad (1)$$

for both, fundamental transverse electric (TE) and TM modes, where $I(x, y)$ is the intensity profile across the waveguide's cross-section. For wide waveguide, a mode-confinement of more than 50% of the power in the GaN core can be maintained up to a wavelength of 4000 nm in the TE polarization. In contrast, the TM mode confinement is much smaller at longer wavelengths. To achieve

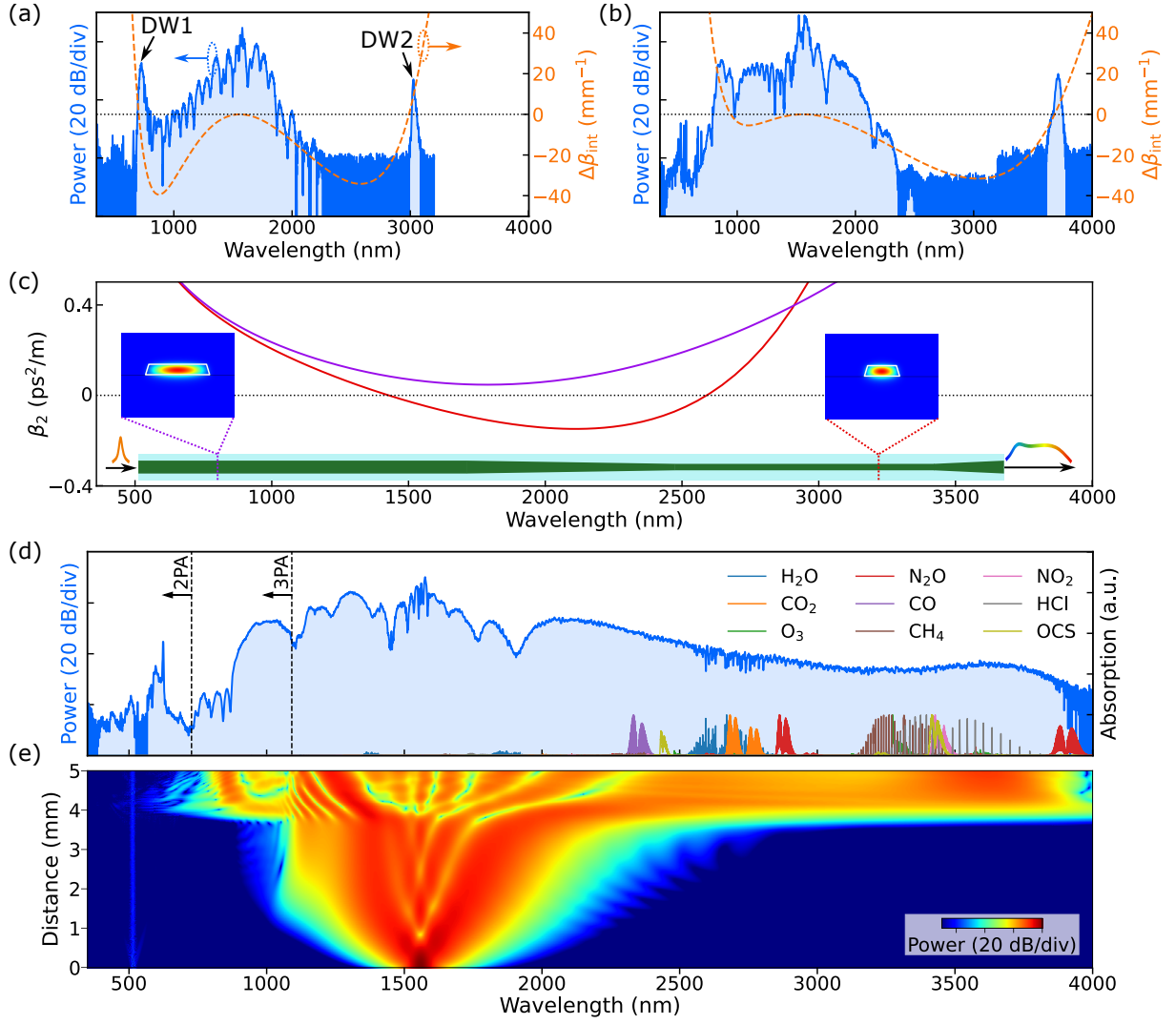


Figure 3 | (a) & (b) Supercontinua obtained from 2 mm long waveguides (blue), and simulated integrated dispersion (dashed orange lines) of fundamental TE mode for waveguide widths of 1.0 μm and 1.5 μm , respectively. (c) Simulated group velocity dispersion of 4.0 μm (purple) and 2.0 μm (red) wide waveguides. The inset shows the waveguide's width profile (top view) and the simulated mode fields at the pump wavelength in both segments of the waveguides. (d) Experimental spectrum obtained from a 5 mm long segmented waveguide (blue). The overlay represents normalized absorption spectra of different gases [52]. (e) Simulated spectral evolution [53].

efficient coupling to the chip via lensed fibers, the waveguides are tapered to a width of 4.0 μm at the coupling facets for 5 mm long chips. In the experiment, we observe a per-facet coupling loss of 4.6 dB.

3 Supercontinuum generation

To generate supercontinua, we utilize an off-the-shelf erbium-doped mode-locked laser with 100 MHz pulse repetition rate (Fig. 1f). The laser is amplified to a maximum of 150 mW of average power, and a waveshaper is included in the setup prior to amplification for dispersion compensation. Lensed fibers are utilized to couple the pulses with a center wavelength of 1560 nm and a pulse duration as short as 55 fs to the chip. The generated light is collected

by a multi-mode fluoride fiber via butt-coupling and measured by optical spectrum analyzers (OSAs).

Figure 2c shows broadband supercontinua that are observed in TM polarization with different pulse energies in a only 2 mm long waveguide of 2.5 μm width. Spectra in excess of two octaves are obtained with 253 pJ of pulse energy, wherein the 30 dB bandwidth exceeds 1.5 octaves. A pronounced dispersive wave (DW) is apparent at approximately half the pump wavelength; expected from the zero-crossing of the integrated dispersion $\Delta\beta_{\text{int}}(\omega) = \beta(\omega) - \beta(\omega_0) - \beta_{1,\omega_0}(\omega - \omega_0)$, where ω is the frequency, β is the wavenumber, ω_0 is the central frequency of the pump laser and $\beta_1 = d\beta/d\omega$.

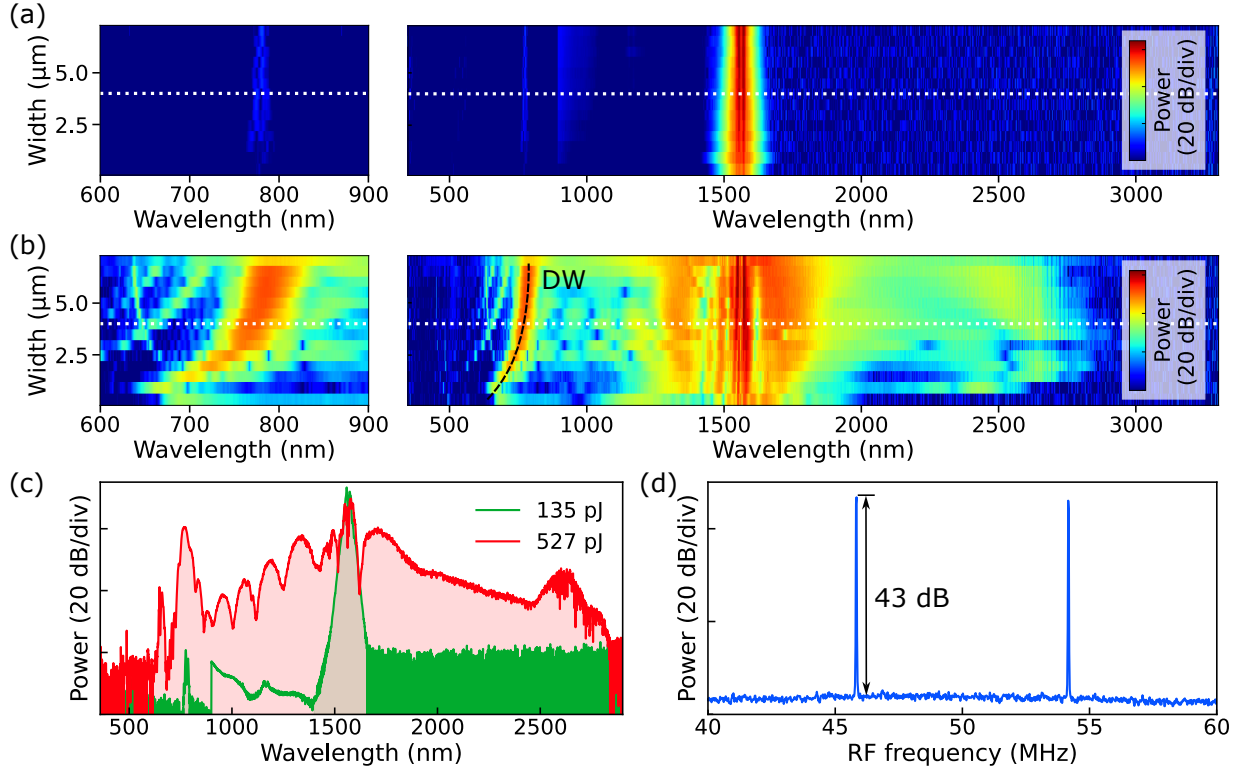


Figure 4 | (a) & (b) Measured spectra for different waveguide widths with ~ 135 pJ and ~ 527 pJ on-chip pump pulse energy. The left panels show a magnified view of the right panels between 600 nm and 900 nm. (c) Output spectra from a $4.0\ \mu\text{m}$ wide waveguide, corresponding to slices marked by dotted white lines in (a) and (b). (d) Measured f_{ceo} beatnotes after bandpass-filtering a 10 nm wide portion around 780 nm of the spectrum shown in (c). The beatnote signal is recorded with a 10 kHz resolution bandwidth (RBW) and 100 Hz video bandwidth.

3.1 Mid-infrared supercontinua

Mid-infrared spectra in the functional group fingerprint window from $2\text{--}5\ \mu\text{m}$ are of high relevance to chemical and molecular sensing [55]. Therefore, we explore the platform’s ability to support the generation of mid-infrared light from an erbium-based pump laser. We now operate the waveguides in TE polarization to benefit from the stronger mode confinement at longer wavelengths (Fig. 2b). Two DW positions are predicted by the integrated dispersion of these waveguides, where the longer wavelength one falls into the mid-infrared and can be tuned from around 3000 nm to >3700 nm by adjusting the waveguide width from $1.0\ \mu\text{m}$ to $1.5\ \mu\text{m}$, similar to observations in silicon nitride and aluminum nitride waveguides [27–29]. Figures 3a and b show the experimental results obtained in 2 mm long waveguides, accurately matching our prediction, despite the large spectral separation from the pump. We attempted shifting the DW to even longer wavelengths (using a $1.8\ \mu\text{m}$ wide waveguide); however, we did not observe any DW at the expected wavelength of 3900 nm. We attribute the absence of a longer wavelength DW to the weak mode-confinement of the only 725 nm thick waveguide layer and vanishing anomalous dispersion at the pump wavelength (preventing short pulse soliton dynamics that drive the DW).

In a separate experiment, we aim at generating a gap-

less, unstructured mid-infrared spectrum as needed for broadband spectroscopy, e.g. multi-molecular species detection. To achieve this, we design a segmented waveguide (Fig. 3c, inset) comprising a 1.5 mm long normal group velocity dispersion segment ($4.0\ \mu\text{m}$ waveguide width), followed by 1.2 mm long tapered waveguide that connects to a 1.5 mm long segment with anomalous group velocity dispersion between 1500 nm and 2600 nm ($2.0\ \mu\text{m}$ waveguide width). Such a design first broadens the pump in the normal dispersion part, which is then compressed to ultrashort temporal duration (and broad spectral bandwidth) in the anomalous dispersion part. Experimentally, a gap-free spectrum ranging approximately from 870 nm to 3900 nm is generated in the 5 mm long (including coupling tapers) segmented waveguide driven by 527 pJ on-chip energy with 55 fs pulse duration (Fig. 3d). Numerical simulations via *pyChi* [53] (Fig. 3e, $\chi^{(2)}$ set to zero) agree well with the experimental results, and suggest that the broadband spectrum is associated with an ultrashort temporal feature of <10 fs duration obtained during compression. The smooth and gap-free spectrum covers a large portion of the $2\text{--}5\ \mu\text{m}$ sensing window. The strong spectral absorption features in the spectrum between 2500 nm and 2900 nm are due to atmospheric water absorption. Importantly, as we illustrate in Fig. 3d, the generated spectrum covers the absorption spectra of important molecu-

lar species, including those of the major greenhouse gases CO_2 , N_2O , and CH_4 . In contrast to platforms utilizing fused silica cladding, we do not expect material loss to be responsible for the spectrum’s long-wavelength cutoff, and attribute it to reduced mode confinement and related strong normal dispersion at long wavelengths. These limitations result from the thin GaN layer and are not fundamental; they may be overcome through increased layer thickness and optimized waveguide geometries in future work. Regarding long-wavelength generation, we highlight the large bandgap of GaN, which effectively suppresses free-carrier generation through 2PA and 3PA at the pump wavelength, and of 2PA across nearly the entire spectrum. This prevents free-carrier generation and unwanted impact on the generated spectrum [11], particularly in the mid-infrared, due to the λ^2 -scaling of free-carrier induced loss.

3.2 On-chip f - $2f$ interferometry

The ability to efficiently generate (multi-)octave spectra is an important prerequisite for self-referencing of optical frequency combs, where f_{ceo} of the pulse train is measured via f - $2f$ interferometry. In this scheme, a longer wavelength portion of the spectrum is frequency-doubled (sum-frequency generation) to overlap with the original spectrum at a shorter wavelength. Photodetection of the beating between the doubled and original spectrum yields f_{ceo} . As GaN not only offers a strong third-order nonlinearity for broadband spectrum generation but also possesses a second-order nonlinearity, this enables implementation of the entire f - $2f$ interferometer in a GaN waveguide, similar to approaches based on lithium niobate [17, 56, 57] and aluminum nitride [15], as well as, self-organized gratings [58] and third harmonic generation [59] in silicon nitride. To access the largest $\chi^{(2)}$ -tensor element of GaN for frequency doubling, we pump the waveguides in the TM polarization. Initially, to validate the frequency doubling, we pump the 2 mm long waveguides with a pulse energy of 135 pJ, low enough to isolate a second harmonic signal from the broadband supercontinuum. In all tested waveguides with waveguide widths ranging from 0.4 μm to 7.0 μm , we observe a second harmonic signal of the pump at 780 nm (Fig. 4a) which is limited in power and bandwidth by the non-zero phase mismatch. To generate a broadband supercontinuum, reaching 780 nm, we increase the pulse energy to 527 pJ. As expected based on the integrated dispersion, the spectra exhibit a pronounced DW ranging from approximately 700 nm to 800 nm, depending on waveguide width (Fig. 4b). To achieve a high signal to noise ratio (SNR), we use a waveguide width of 4.0 μm , as here the spectral position of the DW is well matched with the frequency-doubled pump laser (Fig. 4c). Differing from the experiments where we record optical spectra, here for f_{ceo} detection we collect the light from the chip using a lensed fiber (multi-mode at 780 nm) and collimate it to free space for spectral filtering with a 10 nm wide band-

pass filter centered at 780 nm. The light is focused on a silicon photodiode, and the resulting radio-frequency signal is measured by an electrical spectrum analyzer (ESA) (Fig. 1f). The observed f_{ceo} signal is shown in Fig. 4d, exhibiting a SNR of 43 dB in a resolution bandwidth (RBW) of 10 kHz. This is more than sufficient for phase-locking of f_{ceo} in a self-referenced frequency comb for optical precision metrology. Further improvements of the SNR would likely be possible by an optimized and single-mode output coupling for the 780 nm spectral portion.

4 Conclusion

In summary, we demonstrate efficient generation of ultra-broadband, multi-octave supercontinua in GaN-on-sapphire waveguides pumped by an off-the-shelf C-band erbium-based femtosecond laser. We showcase two important use cases of supercontinua, f - $2f$ interferometry for carrier-envelope offset frequency detection in a waveguide, and efficient mid-infrared supercontinuum generation extending to nearly 4 μm that can support molecular spectroscopy. These results highlight the potential of GaN-on-sapphire for advancing broadband nonlinear photonics, and extending erbium-based laser technology to the mid-infrared wavelength range without limitations from two- and three-photon absorption (and associated free-carriers). The platform promises to extend supercontinua to even longer wavelength, where thicker GaN layers can maintain tight mode confinement. Potential free-carrier losses from unintentionally doped materials might become relevant at long wavelengths, but could be mitigated by semi-insulating GaN [60]. Importantly, GaN-on-sapphire is a widely used material in the semiconductor industry and, hence, readily available at high quality and low cost. Fabricating waveguides from orientation-poled GaN films [61] may, in the future, lead to additional opportunities.

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Data availability

Data underlying the results presented in this paper are available from the corresponding author upon reasonable request.

Disclosure

The authors declare no conflicts of interest.

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