Expanding the Horizon: Enabling Hybrid Quantum Transfer Learning for Long-Tailed Chest X-Ray Classification

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Abstract-Quantum machine learning (QML) has the potential for improving the multi-label classification of rare, albeit critical, diseases in large-scale chest x-ray (CXR) datasets due to theoretical quantum advantages over classical machine learning (CML) in sample efficiency and generalizability. While prior literature has explored QML with CXRs, it has focused on binary classification tasks with small datasets due to limited access to quantum hardware and computationally expensive simulations. To that end, we implemented a Jax-based framework that enables the simulation of medium-sized qubit architectures with significant improvements in wall-clock time over current software offerings. We evaluated the performance of our Jaxbased framework in terms of efficiency and performance for hybrid quantum transfer learning for long-tailed classification across 8, 14, and 19 disease labels using large-scale CXR datasets. The Jax-based framework resulted in up to a 58% and 95% speed-up compared to PyTorch and TensorFlow implementations, respectively. However, compared to CML, QML demonstrated slower convergence and an average AUROC of 0.70, 0.73, and 0.74 for the classification of 8, 14, and 19 CXR disease labels. In comparison, the CML models had an average AUROC of 0.77, 0.78, and 0.80 respectively. In conclusion, our work presents an accessible implementation of hybrid quantum transfer learning for long-tailed CXR classification with a computationally efficient Jax-based framework.

Index Terms—Quantum Machine Learning, Quantum Transfer Learning, Long-Tailed Classification, Multi-Label Classification, Medical Imaging, Chest X-Ray

I. INTRODUCTION

Quantum machine learning (QML) has attracted recent interest due to rapid improvements in hardware and QML methods with theoretical quantum advantages over classical machine learning (CML) methods [1]. While quantum advantage typically refers to runtime improvements, potential advantages may also exist in sample efficiency, generalizability, expressibility, and trainability [2]–[4]. These advantages are particularly applicable for medical imaging tasks, where the growing scale of chest x-ray (CXR) datasets, coupled with the presence of rare, albeit critical, diseases labels results in deep

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learning (DL) models that are biased towards high-occurrence labels [5], [6].

While other groups have explored QML for training CXR DL models to detect diseases such as cardiomegaly, pneumonia, and COVID-19, their approaches were focused on binary classification tasks using small datasets that do not resemble the current state of CML with medical images [7]–[9].

More specifically, multiple diseases may be present in a patient simultaneously, thereby emphasizing the importance of detecting all potential diseases with multi-label classification. Furthermore, Bowles *et al.* [10] suggest that it is not appropriate to extrapolate QML results from small datasets to large datasets.

The primary limitation of QML research beyond binary classification is limited access to quantum hardware and the large computational resources required for classical simulation [11]. To that end, we developed a Jax-based software framework to lower the computational requirements for classical simulation of medium-sized qubit architectures on workstation-level hardware. We evaluated the Jax-based framework for long-tailed multi-label classification across 8, 14, and 19 disease labels using two large-scale CXR datasets. We further compared the performance of QML with CML to evaluate if the theoretical advantages of QML translate into empirical success for these tasks [12]–[16].

Our contributions are two-fold:

- We develop an open-source Jax-based software framework for computationally efficient simulation of medium-sized qubit architectures on workstation-level hardware.
- We evaluate the scalability of hybrid quantum transfer learning for long-tailed multi-label classification tasks with large-scale CXR datasets.

The relevant background for our study is provided in Section II. Our methods are detailed in Section III. Implementation details of our Jax-based framework are provided in Section III-D. Our results are detailed in Section IV and discussed in Section V.

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II. BACKGROUND

A. Chest X-Ray Classification

Chest X-Ray (CXR) is the most common medical imaging study for detecting life-threatening diseases like cardiomegaly and pneumonia [17]. Due to the high co-occurrence of findings within a single CXR, the ability to simultaneously detect the presence of multiple findings with multi-label classification is crucial. As a result, numerous large-scale CXR datasets, which contain hundreds of thousands of high-resolution images with dozens of potential disease findings, have been curated to facilitate the development of DL models for CXR classification with expert-level performance [18]–[21]. These datasets are predicted to increase in size and resolution faster than improvements in hardware and software efficiency, as well as the number of radiologists in the USA [5].

This rapid growth has led to an interesting problem where the high occurrence of CXRs that are healthy or contain common findings, coupled with CXRs containing rare yet critical findings, leads to a long-tailed distribution of disease labels [6]. Training on such datasets often results in DL models with performance that is biased towards high-occurrence labels. This disparity can lead to incorrect predictions for patients with rare long-tail diseases and disastrous downstream implications on patient health outcomes. The potential theoretical advantages of QML could translate to improved performance and efficiency in long-tailed CXR classifiers. Additionally, QML has primarily been evaluated on comparatively simpler classification problems such as binary or ternary classification on artificial data distributions and benchmark datasets like MNIST [7]–[10], [22]. Thus, research on QML and long-tailed CXR classification can cooperatively benefit by using a more challenging problem to better understand where OML stands and how it can be potentially improved.

B. Quantum Transfer Learning

While there are methods to apply quantum computing to CML subroutines [23], [24] and quantum implementations of classical architectures [25]–[27], the variational quantum circuit (VQC) has been extensively evaluated within and outside medical imaging due to its theoretical properties, simple implementation, and integration with backbone models through transfer learning [28].

The VQC starts with n qubits in some initial state, often prepared with data encoding methods, where classical data is encoded as quantum states. A series of parameterized quantum operations, such as rotation and entanglement gates, are then applied to these states. Finally, data is read out from quantum states into classical states. These circuits are trained by performing gradient descent to minimize a loss function of predictions obtained from postprocessing of the measurements of the quantum gradient, and are sometimes called "quantum neural networks" for this reason. Overall, the VQC embeds classical data into an intermediate quantum kernel, and projects quantum states back into classical data [4]. The choice of circuit design (ansatz) is critical for VQC performance. While VQCs tend to avoid exploding gradients [29], they can be prone to barren plateaus [30]. Furthermore, different ansatz also have a trainability and expressibility trade-off [31], so the optimal ansatz for a classification problem must be carefully chosen. The design of the transferred model may also be important regarding the trainability of the model [32].

The abstraction of classical input and classical output with VQCs enables hybrid classical-quantum models using transfer learning [33]. The combination of a backbone model and classical preprocessing layers, followed by a VQC and classical postprocessing layers, is collectively referred to as a *Dressed Quantum Circuit* (DQC). While transfer learning potentially obscures the impact of quantum layers, it reduces the computational resources required for training models with large-scale datasets, and the qubit requirements for the intermediate scale circuits necessary for multi-label classification.

C. Computational Overhead of Quantum Simulation

Prior work has indicated a need to scale up QML experiments to larger scales to determine whether QML behavior is consistent with smaller scales [10], [34]. While the ultimate goal of quantum simulation is to demonstrate proof-of-concept scalability to real quantum hardware, VOCs are highly sensitive to quantum noise and errors [35], [36]. Work remains to implement fault-tolerant quantum error correction [37], and quantum error mitigation may be limited by theoretical superpolynomial bounds on the number of samples needed to estimate expectation values commonly used in VQC optimization [38]. In the context of multi-label CXR classifiers, even small levels of noise could result in incorrect classifications and adversely impact patient health outcomes. This limits the benefits of efficient noisy simulation [39], [40]. Thus, noiseless (ideal) quantum simulation is currently the most reliable and accessible approach to experimenting with QML.

However, the scalability of QML simulation is computationally intensive because the number of neurons in the output layer of DL models for multi-label classification is at least the number of disease labels to be classified. Given a fixed feature extraction backbone and a linear layer of size n for classification, the scalability of computations is dependent on matrix multiplications between the size of the final layer of the feature extraction backbone and the size of the classification head. While matrix multiplication is slightly less than cubic in runtime complexity $(O(n^{\log_2 7}))$ by Strassen's algorithm), since only a single dimension is variable (the length of the classification head), the scalability of a multi-label CML classifier is O(n). For DQCs, the number of qubits required is at least the number of disease labels. Assuming a classical preprocessing linear layer of n labels and an identically sized classical postprocessing linear layer, the scalability of the classical portion of the network is still O(n) by dropping constant factors. However, a DQC with n qubits requires a holding in memory a quantum state vector with 2^n length [39].

TABLE I LONG-TAILED DISTRIBUTION OF DISEASE LABELS FROM NIH-CXR-LT AND MIMIC-CXR-LT BY DATA SPLIT AND SORTED BY OCCURRENCE.

Label	NIH				MIMIC
	Train	Val	Test	Total	in mone
Infiltration	12739	1996	5159	19894	1781
Effusion	7919	1663	3735	14586	14586
Atelectasis	7587	1272	2700	11559	14014
Nodule	4359	667	1305	6331	1309
Mass	3689	764	1329	5782	1006
Pneumothorax	2432	764	2106	5302	3282
Consolidation	2626	544	1497	4667	3232
Pleural Thickening	1998	485	902	3385	590
Cardiomegaly	1590	318	868	2776	14703
Emphysema	1327	272	917	2516	649
Edema	1283	269	751	2303	8444
Subcutaneous Emphysema	957	221	813	1991	572
Fibrosis	1138	183	365	1686	271
Pneumonia	806	173	452	1431	8242
Tortuous Aorta	598	49	95	742	547
Calcification of the Aorta	368	32	55	455	704
Pneumoperitoneum	214	33	69	316	136
Pneumomediastinum	88	22	143	253	176
Hernia	130	35	62	227	739

Thus, the memory usage and compute time of a multi-label DQC classifier scales exponentially at a rate of $O(2^n)^i$.

Although the wall-clock time of quantum simulation may deviate from this theoretical runtime analysis, the computational overhead of scalability in quantum systems have been major limitations in the scalability of prior work in QML inside and outside medical imaging. While experiments have managed to achieve 16-qubit simulations using multiple GPUs [42], [43], it should be possible to achieve this scale on a single GPU, thereby lowering the computational barrier of entry to QML research in medical imaging.

III. METHODS

A. Datasets

1) NIH-CXR-LT: The dataset consists of 19 disease labels with n = 112, 120 frontal CXRs from 30,805 patients [6], [18]. We use the provided training (70%, n = 78, 605), validation (10%, n = 12, 535), and testing (20%, n = 21, 081) splits to train multi-label QML models.

2) *MIMIC-CXR-LT*: The dataset consists of the same 19 disease labels as the NIH-CXR-LT dataset with n = 377,110 CXRs from 65,379 patients [20]. We use the provided testing split with lateral CXRs discarded (n = 48,860) as our external test set to evaluate model generalizability.

B. Classification Tasks

To evaluate the scalability of QML for multi-label classification, we considered the following three sets of disease labels:

• CXR-8: Atelectasis, Cardiomegaly, Effusion, Infiltration, Mass, Nodule, Pneumonia, and Pneumothorax.

TABLE II NUMBER OF PARAMETERS BY COMPONENT.

Component	# Labels	# Parameters
ResNet50	-	23,508,032
	8	16,392
Classical Preprocess	14	28,686
	19	38,931
Quantum Preprocess	8	24
	14	42
	19	57
Classical Postprocess	8	72
	14	210
	19	380



Fig. 1. Classical deep learning model. Image features are extracted with ResNet50 and preprocessed with a linear layer before obtaining predictions.

- CXR-14: All labels from CXR-8, with the addition of Consolidation, Edema, Emphysema, Fibrosis, Pleural Thickening, and Hernia.
- CXR-19: All labels from CXR-14, with the addition of Calcification of the Aorta, Pneumomediastinum, Pneumoperitoneum, Subcutaneous Emphysema, and Tortuous Aorta.

The classification tasks were chosen based on the different versions of the NIH dataset. The long-tailed distribution of both datasets is provided in Table I.

C. Model Architecture

We implemented a DL model architecture consisting of a feature extractor and a classification head. For the feature extractor, we used an ImageNet pre-trained ResNet50 model from Hugging Face [44]. For the classification head, we considered a classical and quantum approach. Parameter counts for each model are provided in Table II.

1) Classical Deep Learning (CDL): After the feature extractor, we applied a classical preprocessing layer as the classification head (Fig. 1). It consisted of a linear fullyconnected layer of size n, equal to the number of disease labels, followed by sigmoid activation.

2) Dressed Quantum Circuit (DQC): After the feature extractor, we applied a Dressed Quantum Circuit (DQC) as the quantum classification head [10], [33] (Fig. 2). The quantum circuit starts with n qubits in the 0-state of the computational basis ($|0\rangle$). Hadamard gates are applied to each qubit to obtain a 50% superposition of $|0\rangle$ and $|1\rangle$ as follows:

$$H|0\rangle = \frac{1}{2}|0\rangle + \frac{1}{2}|1\rangle \tag{1}$$

ⁱAn alternative approach to quantum simulation is tensor networks, which are parallelizable and have linear memory scalability. However, finding the optimal contraction path for a tensor network is NP-hard, thus tensor network simulation still has fundamental scalability limits [41].



Fig. 2. Dressed quantum circuit model. Image features are extracted with ResNet50, preprocessed down to size with a linear layer, then embedded into the quantum circuit with angle encoding applied to a 50/50 superposition of $|0\rangle$ and $|1\rangle$ after the Hadamard gate. Variational parameters (yellow) and CNOT gates (white) are applied, and measurements are fed into the classical postprocessing layer to obtain predictions. Preprocessing layers are highlighted in blue, variational quantum parameters in yellow, and postprocessing layers in orange.

The classification function of the DQC classifier $f : \mathbb{R}^m \to \mathbb{R}^n$ is defined as follows:

$$\hat{y} = f(x; \theta, w_{in}, w_{out}) \tag{2}$$

$$= f_{out}(w_{out}, f_Q(\theta, f_{in}(w_{in}, x)))$$
(3)

where $f_{in} : \mathbb{R}^m \to \mathbb{R}^n$ is the classical preprocessing layers with weights $w_{in} \in \mathbb{R}^{m \times n}$, $f_Q : \mathbb{R}^n \to \mathbb{R}^n$ is the VQC with depth d and trainable angles $\theta_{ij} \in \mathbb{R}^{n \times d}$, and $f_{out} :$ $\mathbb{R}^n \to \mathbb{R}^n$ is the classical postprocessing layer with weights $w_{out} \in \mathbb{R}^{n \times n}$.

After the feature extractor, we apply a classical preprocessing layer (a linear layer of size n), followed by tanh activation and rescaling to $\left[-\frac{\pi}{2}, +\frac{\pi}{2}\right]$. Each output of the preprocessing layer is angle-embedded with a R_Y rotation gate to its corresponding qubit. After the embedding, 3 layers of parameterized R_Y gates followed by CNOT gates are appliedⁱⁱ. Then, the noise-free expectation value of each qubit is measured. The measurements are passed to a postprocessing linear layer of size n. As the number of qubits is equal to the number of labels, we apply sigmoid activation to the postprocessing layer and omit a final classical linear layer.

D. Implementation

To shorten wall-clock training time, we used Jax [46], which uses just-in-time (JIT) compilation to accelerate linear algebra operations for deep learning and quantum simulation on GPUs. Our implementation provides a QML pipeline for medical image analysis that uses Jax and Pennylane [47] to reduce the computational resources required to simulate medium-sized qubit systems on workstation-level hardware.

We implemented the DL models using Flax [48] and the following libraries from the Jax ecosystem [49]: Optax for optimizersⁱⁱⁱ, Pix for image augmentations^{iv}, and Orbax for checkpointing^v. For quantum simulation, we used Pennylane to easily experiment with different DL libraries. Pennylane circuits were optimized using the default.qubit.jax



Fig. 3. Dataloader implemented for experiments. Preprocessed images are serialized, compressed, and cached on disk ahead of time. At runtime, they are retrieved from the cache, decompressed, and deserialized. Image augmentations occur at runtime. A SQLite database tracks the file paths of the cached images.

device and the best differentiation method (backpropagation on our hardware).

To avoid potential CUDA dependency conflicts, we implemented a framework-agnostic multithreaded caching dataloader that supports image preprocessing and augmentations (Fig. 3). Images were preprocessed with the Hugging Face AutoImagePreprocessor that was used to train the ResNet50 backbone. The images were serialized with SafeTensors [50] (a non-executable binary format), compressed with Zstandard [51], and cached with Diskcache [52]. Image augmentations were not cached and were performed dynamically after retrieving the cached preprocessed image. The dataloader was multithreaded using Joblib [53].

E. Benchmarks

Pennylane supports Jax, PyTorch, and TensorFlow by offloading quantum simulation and autodifferentiation to the DL library's operations. To determine the scale of our implementation's performance gains, we benchmark wall-clock time (in s) of the training step of functionally equivalent Jax, PyTorch, and TensorFlow implementations of the CDL and DQC models. All models were JIT compiled except for PyTorch due to lack of support for compiled quantum circuits. For each DL library, we load a single batch of zero-images and zero-labels (zero-vectors of the correct shape) into GPU

ⁱⁱAlthough 3 layers were chosen arbitrarily, prior work has indicated a potential lack of sensitivity to the number of layers for DQCs in binary classification [45].

iiihttps://github.com/google-deepmind/optax/

ivhttps://github.com/google-deepmind/dm-pix/

vhttps://github.com/google/orbax/

memory to eliminate potential I/O and concurrency effects. We then perform 10 training steps to account for potential caching and compilation steps that may affect runtimes. Finally, we measure and compare the runtime of 30 additional training steps.

F. Training Procedure

We trained CDL and DOC models on CXR-8, CXR-14, and CXR-19 classification tasks using 5 random seeds. Backbone weights were initialized from the pre-trained ResNet50 checkpoint. Classical linear layer weights were randomly initialized using the default method (Lecun normal [54]). Parameterized R_Y gates of the DQC were initialized using a random uniform distribution of $[0, 2\pi]$. Images were preprocessed ahead of time by resizing to 256 pixels on the shortest side, center-cropping to 224x224, and normalizing pixel values to ImageNet statistics. Training batches were shuffled and augmented during training with random horizontal flip (p = 0.5) and random rotation ($\theta = \pm 15^{\circ}$) [55]. To ensure that CDL and DQC models with the same random seed use the same order of training examples, trials with the same random seed used the same pseudorandom permutations and augmentations for the training batches. Models were trained with a batch size of 32 to avoid running out of GPU memory, and optimized to minimize mean binary cross entropy (BCE) loss over all diseases labels using Adam (learning rate = 1e-4). Early stopping was used if validation loss did not improve after 5 epochs, with a maximum of 50 training epochs. The best performing model was determined by the model checkpoint with the lowest validation loss.

Models were trained in parallel over 4 NVIDIA RTX A6000 GPUs and Intel Xeon CPUs. All models used 4 CPU threads, except for DQCs, which used 1 or 2 threads to avoid running out of GPU memory. We used Python (version 3.12), CUDA (version 12), and other version-compatible libraries obtained from Conda-Forge. Our full open-source Jaxbased implementations, including further details on software dependencies and versions, are available at https://github.com/UM2ii/quantum-cxr.

G. Metrics and Statistical Analysis

To evaluate model trainability, we compared the convergence of the CDL and DQC models using the training and validation BCE loss across each step. To evaluate the performance of the CDL and DQC models, we measured the mean and per-label area under the receiver operating characteristic curve (AUROC) on the internal NIH and external MIMIC test sets across the CXR-8, CXR-14, and CXR-19 classification tasks. We compared the mean and per-label AUROCs of the CDL and DQC models using paired t-tests. Statistical significance was defined as p < 0.05.

To identify per-label performance trends across experiments, we generate volcano plots of these *p*-values against the percent difference in AUROC of CDL and DQC models, which is defined as follows:

TABLE III

BENCHMARKED WALL-CLOCK RUNTIMES (IN S) BETWEEN TENSORFLOW, PYTORCH, AND OUR JAX-BASED IMPLEMENTATION ACROSS CXR-8, AND CXR-14, AND CXR-19 CLASSIFICATION TASKS FOR A ZERO-BATCH.

	TensorFlow	PyTorch	Jax*			
CXR-8						
CDL	0.06 ± 0.00	0.07 ± 0.00	0.06 ± 0.00			
DQC	0.08 ± 0.00	0.13 ± 0.00	0.06 ± 0.00			
CXR-14						
CDL	0.06 ± 0.00	0.07 ± 0.00	0.06 ± 0.00			
DQC	0.43 ± 0.00	0.18 ± 0.00	0.08 ± 0.00			
CXR-19						
CDL	0.06 ± 0.00	0.07 ± 0.00	0.06 ± 0.00			
DQC	14.97 ± 0.01	1.89 ± 0.00	0.80 ± 0.00			

* Our implementation.

% diff. AUROC =
$$2 * \frac{\text{AUROC}_{CDL} - \text{AUROC}_{DQC}}{\text{AUROC}_{CDL} + \text{AUROC}_{DQC}}$$
 (4)

More specifically, we produce scatter plots where each point represents an experiment between CDL and DQC on the same classification task, and the $-\log_{10}(p\text{-value})$ of the paired t-test is plotted against the $\log_2(\% \text{ diff. AUROC})$. We include the labels in CXR-8 and the additional labels added in CXR-14, as these are present across multiple experiments.

IV. RESULTS

A. Benchmarks

Our benchmarks indicate that our Jax-based implementation is the fastest for simulating DQC across all three classification tasks when compared to functionally equivalent TensorFlow and PyTorch implementations (Table III). Extrapolated to an entire epoch of 2,454 batches:

- For CXR-8, our implementation takes 2.45 mins/epoch and is 25% faster than TensorFlow (3.27 mins/epoch) and 54% faster than PyTorch (5.32 mins/epoch).
- For CXR-14, our implementation takes 3.27 mins/epoch and is 81% faster than TensorFlow (17.59 mins/epoch) and 56% faster than PyTorch (7.36 mins/epoch).
- For CXR-19, our implementation takes 32.72 mins/epoch and is 95% faster than TensorFlow (612.27 mins/epoch) and 58% faster than PyTorch (77.30 mins/epoch).

B. Model Trainability

We observed that across the CXR-8, CXR-14, and CXR-19 classification tasks, the DQC models had a slower convergence rate compared to the CDL models, as shown in Figure 4. This resulted in DQC models taking more than twice as many epochs to converge with early stopping. Moreover, the DQC models demonstrated a higher validation loss compared to CDL models across CXR-8 (0.22 vs 0.21), CXR-14 (0.17 vs 0.15), and CXR-19 (0.13 vs 0.12) classification tasks.



Fig. 4. Training and validation loss between CDL and DQC models across CXR-8, CXR-14, and CXR-19 multi-label classification tasks.

C. Model Performance

When comparing the model performance (mean AUROC) on the internal NIH test set, we observed that the CDL models significantly outperformed the DQC models by 9.5% for CXR-8 (0.70 ± 0.02 vs 0.77 ± 0.00 , p = 0.005), by 6.6% for CXR-14 (0.73 ± 0.02 vs 0.78 ± 0.00 , p = 0.004), and by 7.8% for CXR-19 (0.74 ± 0.03 vs 0.80 ± 0.00 , p = 0.009). Figures 6, 8, and 10 illustrate the label-wise comparison in performance between the CDL and DQC models.

When evaluating model generalizability on the external MIMIC test set, we observed that DQC models had a significantly lower mean AUROCs when compared to CDL models. However, the difference in performance between the two models was lower than the differences in the internal NIH test set, with a difference of 4.5% for CXR-8 (0.65 ± 0.01 vs 0.68 ± 0.00 , p = 0.009), 4.4% for CXR-14 (0.67 ± 0.01 vs 0.70 ± 0.00 , p = 0.008), and 5.7% for CXR-19 (0.68 ± 0.01 vs 0.72 ± 0.00 , p = 0.002). Figures 7, 9, and 11 illustrate this comparative performance between the two models, stratified by disease labels.

Our volcano plots (Figures 12 and 13) summarize perlabel performance trends across paired models for CXR-8 and CXR-14 labels, respectively. Points above the dotted line are considered significant (p < 0.05), and points farther to the right have a higher (more positive) percent difference in AUC, thus indicating a stronger advantage of CDLs over DQCs. We observe that the 4 labels with the largest occurrence in the NIH dataset show the most consistent trends:

- Infiltration had no significant % diff. AUROC except for the CXR-8 task on the NIH test set.
- Effusion had significantly higher % diff. AUROC except for the CXR-8 and CXR-19 tasks on the MIMIC test set.
- Atelectasis tended to exhibit the highest % diff. AUROC among all labels. Although this difference was not statistically significant, it could potentially be considered clinically significant.
- Nodule had significantly higher % diff. AUROC in DQCs compared to CDLs on both test sets.

For CXR-14 labels on the NIH test set, every additional label exhibited significantly higher % diff. AUROC, except for Emphysema in the CXR-19 task. Conversely, for CXR-



Fig. 5. Mean AUROC between CDL and DQC models on NIH-CXR-LT and MIMIC-CXR-LT test sets across CXR-8, CXR-14, and CXR-19 classification tasks. (ns: p > 0.05, *: p < 0.05, *: p < 0.01, **:: p < 0.001).

14 labels on the MIMIC test set, only Hernia exhibited significantly higher % diff. AUROC for both CXR-14 and CXR-19 tasks.

V. DISCUSSION

In this work, we developed an open-source Jax implementation of a QML framework for medical imaging that enables long-tailed multi-label classification of CXRs. Although we find that the DQC models do not outperform the CDL models on our selected hyperparameters, the performance difference was < 10% across all our experimental setups on both



Fig. 6. Mean per-label AUROC between CDL and DQC models on NIH-CXR-LT test set for CXR-8 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, *: p < 0.01, **:: p < 0.001).



Fig. 7. Mean per-label AUROC between CDL and DQC models on MIMIC-CXR-LT test set for CXR-8 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, *: p < 0.01, **: p < 0.001).

internal and external test sets. We hope to shorten this gap with improvements in theoretical understanding and empirical utility of QML models.

Our benchmarks indicate that our Jax-based implementation is faster than functionally equivalent PyTorch and TensorFlow implementations for DQCs. If we further extrapolate from our benchmarks, a 19-qubit DQC, which takes over 24 hours to train on our hardware with Jax, would take over 48 hours on



Fig. 8. Mean per-label AUROC between CDL and DQC models on NIH-CXR-LT test set for CXR-14 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, *: p < 0.01, **:: p < 0.001).



Fig. 9. Mean per-label AUROC between CDL and DQC models on MIMIC-CXR-LT test set for CXR-14 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, *: p < 0.01, **:: p < 0.001).

PyTorch and over 2 weeks on TensorFlow. More generally, the cost of adopting a Jax-based workflow may be easily offset by these runtime improvements.

However, the wall-clock time of DQCs was higher than



Fig. 10. Mean per-label AUROC between CDL and DQC models on NIH-CXR-LT test set for CXR-19 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, *: p < 0.01, **: p < 0.001).



Fig. 11. Mean per-label AUROC between CDL and DQC models on MIMIC-CXR-LT test set for CXR-19 classification task, sorted by occurrence. (ns: $p \ge 0.05$, *: p < 0.05, **: p < 0.01, ***: p < 0.001).

CDLs due to a slow convergence rate of DQCs with the same learning rate. We observed that the DQC models tended to train up to the maximum epoch limit. This indicates that the DQCs did not end up in a barren plateau in the loss landscape,



Fig. 12. Volcano plot of performance on CXR-8 labels across experiments. Negative \log_{10} -transformed *p*-values of the paired t-tests for mean AUROC of CDL and DQC are plotted against the \log_2 -transformed % difference in AUROC between CDL and DQC. The dashed line marks the significance threshold (p < 0.05).

otherwise they would have stopped earlier. The models that did stop early likely finished in a local minimum instead of a global minimum. It is possible that with more training epochs, the performance difference between CDL and DQC for CXR-14 and CXR-19 could narrow further.

Given the high runtime and slow convergence rate of DQCs, further scalability improvements are critical to followup experiments. Parameter initialization could be optimized to enable a more favorable initial training landscape [56]. While Adam is a reliable optimizer, other optimizers could potentially provide lower memory usage and faster convergence [57]–[60]. While our batch size was chosen to fit models on



Fig. 13. Volcano plot of performance on the CXR-14 additional labels across experiments. Negative \log_{10} -transformed *p*-values of the paired t-tests for mean AUROC of CDL and DQC are plotted against the \log_2 -transformed % difference in AUROC between CDL and DQC. The dashed line marks the significance threshold (p < 0.05).

a single GPU, the batch size could be tuned to larger sizes through gradient accumulation. Mixed precision training could also lower memory requirements and shorten training time. Finally, using quantum simulation frameworks with additional optimizations could result in further speedups [41], [61]–[64].

For model performance, we observe that both CDL and QDC models were trainable and performed better than random guessing on every label, but the DQC models fail to outperform CDL on every label. This performance deviation could be due to model overparameterization. While the VQC adds a few parameters, the largest contribution of parameters comes from the postprocessing classical layer. ResNet in particular is already overparameterized for medical imaging [55], so it is not guaranteed that adding additional parameters would improve performance. It is also possible that quantum circuits could bottleneck the convergence rate or induce a regularizing effect during model training due to limitations in data embedding and measurement layers. This could result in "quantum utility" in other areas of machine learning.

Interestingly, the performance gap in mean AUROC between the CDL and DQC models narrows when testing on MIMIC compared to NIH. We observed that more of the per-label mean AUROC comparisons resulted in nonsignificant differences between CDL and DQC models. There are two potential confounders in the relatively better performance of DQCs on MIMIC. First, poor generalizability across both models was observed, which limits the applicability of generalization-based arguments. Second, the demographic distributions between NIH and MIMIC are known to differ. Thus, the DQC may have learned certain demographic features unrelated to disease states that are present in higher frequencies in MIMIC vs NIH.

Our volcano plots indicate that labels with a higher occurrence in a data distribution may exhibit more consistent performance trends across different sizes of models and classification tasks. However, these trends may be influenced by demographic or imaging factors specific to each test set, thus it is likely the unique imaging features of each label that contribute to the individual classification challenges of each label. Interestingly, DQC did not outperform CDL in cardiomegaly and pneumonia, two diseases that have been empirically successful with binary classification and QML [7], [8]. This may be due to differences in the model architectures. It's possible that tuning the learning rate and number of layers, using alternative backbones such as vision transformers [65], and exploring alternative data encoding methods and quantum circuit ansatz could further improve classification performance for QML models.

Our results point to the need for hyperparameter exploration to better understand the performance range and sensitivity across hyperparameters. While it appears intuitive to use the same hyperparameters for evaluating QML and CML models in the name of fairness, based on our results, CML and QML models are not guaranteed to perform the same due to fundamental differences between quantum and classical computation. Additional work is needed to determine if the larger variance of DQC performance is an experimental artifact or a fundamental property of DQC models. These follow-up experiments are essential and nontrivial given the large search space of hyperparameters [10], [66].

There are certain limitations to our work. 1) We focus on ideal quantum simulation without presence of noise. 2) We optimize our implementation to fit on a single GPU instead of multiple GPUs. 3) We do not tune model hyperparameters. 4) We focus on the more established Pennylane simulator instead of newer simulators. We plan to explore these areas in future work.

VI. CONCLUSION

Our novel Jax-based quantum machine learning framework for long-tailed chest X-ray classification is scalable for up to 19 qubits and disease labels. Our work is an exciting step towards reducing the computational barrier to quantum machine learning research for medical imaging applications, and opens the door to both further runtime and performance optimizations and characterization of QML behavior across the hyperparameter space.

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