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Anomalous Nernst effect in the noncollinear antiferromagnet Mn₅Si₃

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Investigating the off-diagonal components of the conductivity and thermoelectric tensor of materials hosting complex antiferromagnetic structures has become a viable method to reveal the effects of topology and chirality on the electronic transport in these systems. In this respect, Mn_5Si_3 is an interesting metallic compound that exhibits several antiferromagnetic phases below 100 K with different collinear and noncollinear arrangements of Mn magnetic moments. Previous investigations have shown that the transitions between the various phases give rise to large changes of the anomalous Hall effect. Here, we report measurements of the anomalous Nernst effect of Mn_5Si_3 single crystals. Below 25 K we observe a sign change of the zero-field Nernst signal with a concomitant decrease of the Hall signal and a gradual reduction of the remanent magnetization which we attribute to a subtle rearrangement of the magnetic moment configuration at low temperatures.

I. INTRODUCTION

Antiferromagnetic materials have attained a renaissance in condensed-matter research due to technical advantages like low stray-fields and ultrafast switching compared to ferromagnets and leading to the development of a new field coined antiferromagnetic spintronics [1, 2]. A particular class of materials are antiferromagnets in which the magnetic moments of atoms are ordered in a noncollinear fashion. They often exhibit a nonzero Berry phase curvature leading to an emergent electromagnetic response, which can be harnessed for practical purposes [3–7]. In noncollinear antiferromagnets and spin liquids a nonzero Berry phase curvature gives rise to an unusually large anomalous Hall effect (AHE). Like in ferromagnets, the intrinsic part of the AHE is obtained by integration of the Berry phase curvature of occupied electronic bands over the entire Brillouin zone [8, 9]. Similar to the AHE, its thermoelectric counterpart, the anomalous Nernst effect (ANE), generates a voltage transverse to the heat flow and magnetization. This transverse thermopower provides a measure of the Berry phase curvature only at the Fermi energy $E_{\rm F}$ [8, 9]. The AHE and ANE have been the subject of intense research and development in recent years and hold great promise for practical applications in the fields of spintronics and thermoelectronics. Both effects can be extraordinary large in chiral antiferromagnets like Mn₃Sn and Mn₃Ge despite their tiny magnetization [3, 10–14]. Here, the enhanced Berry-phase curvature is associated with the existence of Weyl points near the Fermi level where the Berry curvature diverges.

The intermetallic compound Mn_5Si_3 is a noncollinear antiferromagnet which has gained attention due to un-

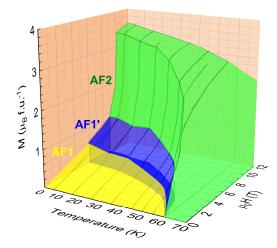


FIG. 1. Magnetic phase diagram and magnetic moment of Mn_5Si_3 obtained from individual magnetization curves, see Fig. 4(a). AF1 and AF1' exhibit noncollinear antiferromagnetic structures while AF2 is a collinear antiferromagnetic phase.

usual thermodynamic and electronic transport phenomena [15–20]. Mn_5Si_3 has hexagonal crystal structure (space group $P6_3/mcm$) with two inequivalent Mn lattice sites Mn_1 and Mn_2 at room temperature and undergoes two structural phase transitions toward orthorhombic symmetry below 100 K.

Fig. 1 shows the magnetic phase diagram of Mn_5Si_3 in a magnetic field H oriented along the crystallographic caxis. Various methods including neutron scattering have confirmed the existence of an antiferromagnetic phase AF2 between the Néel temperatures $T_{N1} = 60$ K and $T_{N2} = 100$ K with zero Mn_1 moments and collinear ar-

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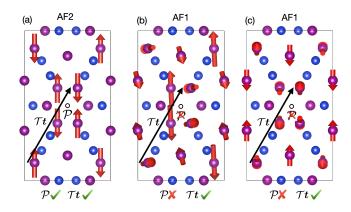


FIG. 2. Magnetic crystal structures of the low-temperature (T < 100 K) antiferromagnetic phases of bulk Mn₅Si₃. Mn and Si atoms are shown in magenta and blue color, respectively. (a) Collinear AF2 phase observed for 60 K < T < 100 K [15, 22, 28, 29]. (b) Noncoplanar AF1 phase without inversion symmetry proposed in Ref. [24] for T < 60 K [29]. (c) Illustration of the AF1 phase proposed in Ref. [26] for T < 60 K, also noncoplanar and noncentrosymmetric.

rangement of two thirds of Mn_2 moments [Fig. 2(a)] [15, 19, 21–23]. In the antiferromagnetic AF1 phase below $T_{\rm N1} = 60$ K, a highly noncollinear and noncoplanar arrangement of magnetic moments is observed where the Mn atoms acquire different magnetic moments, although the details of the moment size and orientation of the Mn atoms are still under dispute [24–26], see Fig. 2(b,c). As soon as the magnetic structure changes from collinear AF2 to noncollinear AF1 below $T_{\rm N1} = 60$ K, a strong AHE is observed [16–18]. In addition, the existence of a magnetic-field induced intermediate phase AF1' has been inferred from neutron scattering and electronic transport measurements [18, 19, 23]. Finally, at high magnetic fields, a collinear AF2 phase with similar properties like the zero field AF2 phase is reestablished [16, 18, 19, 26]. The different phases show characteristic high-energy spin dynamics observed by inelastic neutron scattering [27]. It is these different magnetic moment configurations of noncollinear and collinear order achieved at different magnetic fields and temperatures, that make the Mn₅Si₃ compound so interesting for investigations of the effect of topology and complex magnetic order on the magnetotransport properties.

For the noncollinear AF1 phase, previous firstprinciple calculations assumed a Heisenberg Hamiltonian that takes into account magnetic exchange and biaxial anisotropy [28]. Through modeling of the lowtemperature spin-wave spectrum obtained by inelastinc neutron scattering at 10 K, two additional exchange constants representing the Mn₁-Mn₁ and Mn₁-Mn₂ interactions have been proposed resulting in a ground-state spin arrangement in the AF1 phase that is very different from the AF2 phase, with Mn₁ and Mn₂ moments oriented along the b and c axis, respectively [Fig. 2(c)] [26]. Furthermore, the field-induced phase transition between AF1 and AF1' was simulated by including a Zeeman term in the Heisenberg Hamiltonian resulting in an additional magnetic phase to occur at low temperatures [26]. In this model, it is assumed that the Mn_1 moments are longitudinally susceptible, i.e., their size is affected by an external field. With increasing magnetic field a "spin flop" phase with coplanar moments in the *ab* plane is succeeded by the AF1' phase, where Mn_1 moments start to acquire a component along the *c* axis, and finally by a transition to the field-induced AF2 phase with nonvanishing Mn_1 moments aligned parallel to the direction of the magnetic field.

In addition to single crystals, thin epitaxially strained Mn_5Si_3 layers with vanishing magnetization have been studied that exhibit collinear order and a spontaneous AHE due to the breaking of time-reversal symmetry by an unconventional staggered spin-momentum interaction [30]. In this case, the zero net magnetization is generated by the non-relativistic electronic structure with altermagnetic collinear spin polarization in momentum space [31, 32]. This gives rise to an anomalous Hall and Nernst effects despite the collinear spin arrangement in the thin epitaxial films [33].

The link between the AHE and ANE via the Berryphase concept, the hitherto reports of both effects observed in other noncollinear antiferromagnets, the observation of a nonzero AHE and its strong changes at the magnetic phase boundaries motivated this study of the ANE in Mn_5Si_3 , where we focus to the noncollinear magnetic phase at low temperatures.

II. EXPERIMENTAL

 Mn_5Si_3 single crystals were obtained by a combined Bridgman and flux-growth technique and were characterized by x-ray diffraction as described earlier [18]. The single crystals have been polished and oriented by Laue diffraction, see Fig. 3(a,b).

Measurements of the AHE were performed in a physical-property measurement system (PPMS) as described in Ref. [18] with 50- μ m Pt wires attached to the crystal in an appropriate fashion with conductive silverepoxy. The ANE was obtained on the same Mn_5Si_3 single crystal of thickness t = 0.6 mm and lengths $l_x = 1.2$ mm and $l_y = 1.4$ mm along z, x, and y, respectively. Fig. 3(c) shows a cartoon of the ANE setup. The crystal was mounted between two Cu clamps electrically isolated by 20- μ m Kapton foil and a resistor $R_{\rm H}$ was attached on one clamp serving as a heater generating a temperature difference $\Delta T_{\rm x} = T_{\rm h} - T_{\rm c}$ between the hot and cold side. Both temperatures were determined by using calibrated resistive thermometers. The power of the heater was always adjusted to keep $\Delta T_{\rm x}$ below 10% of the average temperature $T_0 = (T_{\rm h} + T_{\rm c})/2$. The Nernst voltage $\Delta V_{\rm y}$ was measured along the y direction with a nanovoltmeter. The crystal was mounted with the crystallographic a, b, band c axes oriented parallel to the y, x, and z directions,

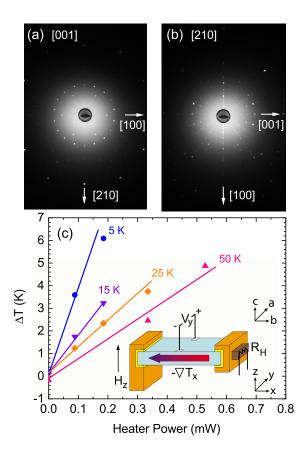


FIG. 3. (a,b) Laue diffraction patterns of a Mn₅Si₃ single crystal oriented with the x-ray beam along the (a) [001] and (b) [210] directions of the hexagonal structure at room temperature. At T < 100 K, the [100], [210], and [001] directions correspond to the *a*, *b*, and *c* axes, respectively, of the orthorhombic phase. (c) Temperature difference $\Delta T = T_{\rm h} - T_{\rm c}$ between the hot and the cold end of the sample vs heater power for different average temperatures T_0 . Solid lines indicate a linear behavior. Inset shows a cartoon of the experimental set up and the orientation of the sample with crystallographic axes *a*, *b*, and *c* of low-temperature orthorhombic phase with respect to the sample holder.

respectively, with the heat flow Q along the b axis and the magnetic field oriented along the c axis.

III. RESULTS

A. Magnetization and Anomalous Hall effect

Fig. 4(a) shows a typical magnetization curve of Mn_5Si_3 at T = 35 K with the two jumps of the magnetization $\Delta M(H_{c1})$ and $\Delta M(H_{c2})$ at magnetic fields H_{c1} and H_{c2} , respectively, attributed to the AF1/AF1' and AF1'/AF2 phase phase transitions. The heights of the jumps are plotted in Fig. 4(b) together with the remanent magnetization $M_R(0)$ vs. temperature. A remarkable detail that escaped our attention earlier is

the decrease of $M_{\rm R}(0)$ when cooling below 25 K while $\Delta M(H_{\rm c1})$ and $\Delta M(H_{\rm c2})$ continuously increase with decreasing temperature below $T_{\rm N1} = 60$ K. Moreover, the absolute value of $M_{\rm R}(0)$ below 20 K depends on the maximum applied magnetic field, i.e. ± 2 T or ± 5 T, see Fig. 4(b), indicating the formation of antiferromagnetic domains with opposite Néel vectors in this temperature range 30. Magnetic polarization at fields larger than 5 T was not possible without entering the AF1' phase.

The phase transitions are clearly observed in the AHE of Mn_5Si_3 , see Fig. 4(c-f). As discussed earlier, the intrinsic Berry-phase contribution of the AHE to σ_{xy} is dominant in the range of moderate conductivity [18, 34]. At 50 K, below $T_{\rm N1}$, the AHE strongly changes at magnetic fields $H_{\rm c1}$ and $H_{\rm c2}$. In the collinear AF2 phase the AHE vanishes. The absolute value of the transverse resistivity $\rho_{yx}(0)$ at zero field increases with decreasing temperature down to 25 K and then decreases and even vanishes at T = 5 K while $M_{\rm R}(0)$ remains non zero.

Fig. 4(g) shows the Hall conductivity $\sigma_{xy} = \rho_{yx}/(\rho_{xx}^2 + \rho_{yx}^2)$ obtained by using the temperature dependence of the longitudinal resistivity ρ_{xx} , see inset Fig. 4(h). The transverse conductivity $\sigma_{xy} = 150 \,\Omega^{-1} \text{cm}^{-1}$ and the longitudinal conductivity $\sigma_{xx} = 7400 \,\Omega^{-1} \text{cm}^{-1}$ are in agreement with the universal scaling relation of σ_{xy} and σ_{xx} [14, 18, 34].

The absolute values of $\sigma_{xy}(0)$ and $\sigma_{xy}(H_{c1})$ plotted in Fig. 4(h) gradually increase between $T_{\rm N1} = 60$ K and ≈ 25 K but then drop to very low values fro $T \leq 25$ K. We emphasize that $\sigma_{\rm xv}(0)$ completely vanishes for $T \leq 5$ K while $\sigma_{xy}(H_{c1})$ remains at a low value of 17 Ω^{-1} cm⁻¹ at T = 2 K. The decrease of the AHE toward low temperatures is unusual for a well established magnetic order but could arise from domain reformation around zero field inferred from the reduced magnetization $M_R(0)$. However, the fact that both contributions to the AHE, $\sigma_{xy}(0)$ and $\sigma_{xy}(H_{c1})$, decrease toward zero temperature while the magnetization $\Delta M(H_{c1})$ is not reduced demonstrates that a different mechanism might be at hand. For antiferromagnetic Mn₃Sn, a sharp drop of σ_{zx} and σ_{yz} in connection with a strong increase of σ_{xy} was observed in the low temperature spin-glass phase below 50 K [3, 14]. This suggests that in Mn_5Si_3 the magnetic moments possibly rearrange at low temperatures as previously inferred from analyzing the evolution of spin-wave energies, revealing another field induced phase-transition below the AF1/AF1' phase boundary [26].

B. Anomalous Nernst effect

In the following we focus on the ANE obtained on the same Mn₅Si₃ single crystal. Theoretically, the ANE generates an electric field $\mathbf{E} = Q_{\rm S}\mu_0 \mathbf{M} \times (-\nabla T)$ perpendicular to the directions of the magnetization \mathbf{M} and temperature gradient $-\nabla T$, where $Q_{\rm S}$ is the anomalous Nernst coefficient and μ_0 is the magnetic permeability of free space. For the present configuration with H_z paral-

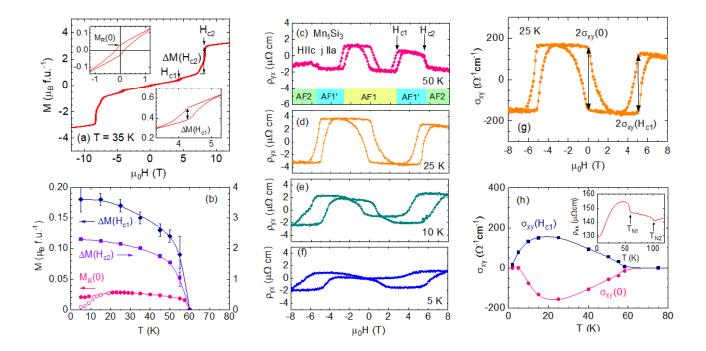


FIG. 4. (a) Magnetization M(H) at T = 35 K. Insets show a close up of M(H) near zero field (top left) and around the transition at H_{c1} (bottom right). (b) Remanent field $M_{\rm R}(0)$ and magnetization jumps $\Delta M(H_{c1})$ and $\Delta M(H_{c2})$ obtained from M(H) vs temperature. Closed (open) circles indicate data obtained after applying a magnetic field of ± 5 T (± 2 T) before measuring M(0). (c-f) Anomalous Hall effect for various temperatures. (g) Anomalous Hall conductivity $\sigma_{xy}(H)$ at T = 25 K. (h) Temperature dependence of $\sigma_{xy}(0)$ and $\sigma_{xy}(H_{c1})$. Inset shows the resistivity $\rho_{xx}(T)$ with indicated Néel temperatures $T_{\rm N1}$ and $T_{\rm N2}$ at the magnetic phase transitions AF1/AF1' and AF1'/AF2, respectively. The magnetic field was always oriented along the crystallographic c axis.

lel to the easy axis of magnetization c, $|\mathbf{M}| = M_z$, and with a temperature gradient along x, this simplifies to $E_y = -S_{yx}\nabla T_x$.

The Nernst signal S_{yx} is experimentally measured by

$$S_{\rm yx} = \frac{\Delta V_{\rm y} \, l_{\rm x}}{\Delta T_{\rm x} \, l_{\rm y}} \tag{1}$$

where we made use of the fact that $E_y = -\Delta V_y/l_y$ and $\nabla T_x = \Delta T_x/l_x$.

Fig. 5(a-d) shows S_{yx} vs magnetic field H applied parallel to the c direction and heat flow along the b direction for different temperatures below $T_{\rm N1}$. At 50 K, the transitions between the different magnetic phases are observed as clear changes of S_{yx} with a hysteresis, very similar to the behavior of the AHE [Fig. 4(c-f)]. S_{yx} is zero in the collinear AF2 phase for temperatures T > 60K, see *e.g.* Fig. A.1(a), concomitant with a vanishing AHE and magnetization. Again, after attaining a maximum the magnitude of S_{yx} decreases with decreasing temperature below 25 K, similar to the behavior of the AHE, *cf.* Fig. 4(c-f). However, a remarkable difference is the sign change of the remanent $S_{yx}(0)$ below 25 K [see Figs. 5(b,c)] before it vanishes at lower temperatures. This behavior is also observed for H applied parallel to the c direction and heat flow along the a direction but not for H applied parallel to the a or b directions where no AHE appeared at zero field, see Appendix.

The temperature dependence is seen more clearly in plots of $S_{yx}(0,T)$ and $S_{yx}(H_{c1},T)$, Fig. 5(e). $S_{yx}(0)$ rapidly changes sign by cooling to below 25 K, strongly deviating from the approximately linear temperature dependence observed for $S_{yx}(H_{c1})$ below 25 K. Both coefficients vanish toward zero temperature due to Nernst's theorem [35]. The sign change of $S_{yx}(0,T)$ occurs at the same temperature where we observe a decrease of the remanent magnetization $M_{\rm R}(0)$, in contrast to $\Delta M(H_{\rm c1})$ which appears more like a magnetically saturated state at low temperatures, see Fig. 4(b). While the vanishing $\sigma_{\rm xy}(0)$ and reduced $M_{\rm R}(0)$ could be considered as indications for the reformation of antiferromagnetic domains, this cannot explain the reappearance of a positive $S_{\rm vx}(0)$ below 20 K supporting the idea of a weak modification of the magnetic structure at low temperatures.

The transverse thermoconductivity, i.e. transverse Peltier coefficient, arising from the Berry phase at $E_{\rm F}$

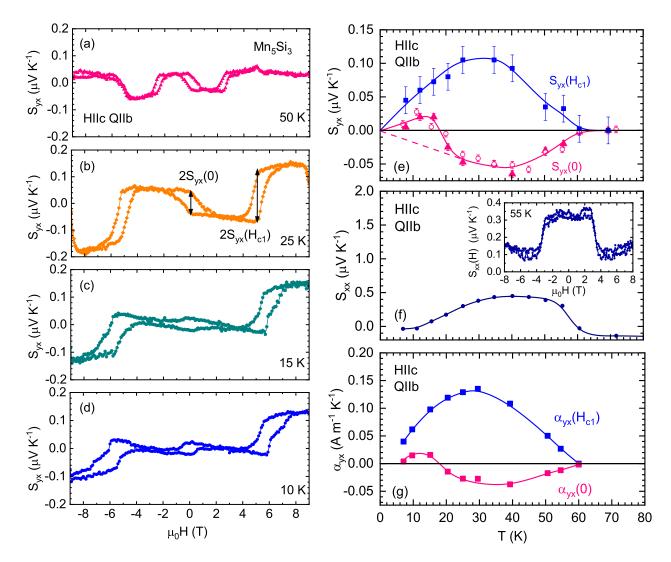


FIG. 5. (a-d) Anomalous Nernst effect $S_{yx}(H)$ for various temperatures. (e) $S_{yx}(0)$ and $S_{yx}(H_{c1})$ vs temperature T. Solid symbols indicate data taken from individual $S_{yx}(H)$ sweeps, see panels (a-d). Open circles were calculated from the difference between $S_{yx}(H)$ measured in two consecutive temperature sweeps at positive or negative remanence. Dashed line indicates a linear behavior toward zero temperature. (f) Temperature dependence of the Seebeck coefficient S_{xx} in zero field. Inset shows $S_{xx}(H)$ at T = 55 K. (g) Transverse Peltier coefficients $\alpha_{yx}(0)$ and $\alpha_{yx}(H_{c1})$ vs temperature T.

[8], can be calculated in zero magnetic field by

$$\alpha_{\rm yx} = S_{\rm yx}\sigma_{\rm xx} - S_{\rm xx}\sigma_{\rm xy} \tag{2}$$

Here, $S_{\rm xx} = \Delta V_{\rm x} / \Delta T_{\rm x}$ is the Seebeck coefficient measured in the same setup and plotted in Fig. 5(f) for different temperatures using $\sigma_{\rm yx} = -\sigma_{\rm xy}$. An interesting detail is the magnetic field behavior of $S_{\rm xx}(H)$ in the inset of Fig. 5(f). At magnetic fields below H_{c2} the Seebeck coefficient is almost independent of H but precipituously drops at H_{c2} when crossing the phase boundary between the field-induced noncollinear AF1' phase and the high-field collinear phase AF2. This extraordinary sharp change of the magneto-Seebeck effect with magnetic field is observed only at H_{c2} where the magnetic order changes from noncollinear to collinear. It is correlated with the strong change of the magnetoresistance $\rho_{\rm xx}(H)$ by ≈ 10 % at H_{c2} and T = 45 K [18]. This is expected from the Mott relation between the thermo-electric and electronic conductivity

$$\alpha_{\rm xx} = \sigma_{\rm xx} S_{\rm xx} = \frac{\pi^2 k_{\rm B}^2}{3e} T \left(\frac{\partial \sigma_{\rm xx}}{\partial E} \right)_{\mu} \tag{3}$$

where $k_{\rm B}$ is the Boltzmann constant, e the electron charge, and μ the electrochemical potential. A modification of the Fermi surface when crossing the AF1'/AF2 phase boundary can be also inferred from the strong variation of the carrier density obtained from the ordinary Hall effect of Mn₅Si₃ films [16].

It has been shown previously that the Mott relation between σ_{xx} and α_{xx} can also be applied for the transverse coefficient $\alpha_{xy} = -\alpha_{yx} [8, 36, 37]$

$$\alpha_{\rm xy} = \frac{\pi^2 k_{\rm B}^2}{3e} T \left(\frac{\partial \sigma_{\rm xy}}{\partial E} \right)_{\mu}.$$
 (4)

The transverse coefficient α_{yx} [Fig. 5(g)] obtained from Eq. 2 essentially shows the same behavior as $S_{yx}(0)$ [Fig. 5(e)]. Since $|S_{xx}\sigma_{xy}| \ll |S_{yx}\sigma_{xx}|$, α_{yx} is dominated by $S_{yx}\sigma_{xx}$ (Eq. 2). Hence, the ANE mostly arises from the transverse heat flow (90 %) and the sign change of α_{yx} occurs due to the sign change of S_{yx} .

IV. DISCUSSION

A. Temperature dependence of the ANE

A sign change of the ANE with temperature was reported earlier for the ferromagnetic semiconductor $Ga_{1-x}Mn_xAs$ and was attributed to the scatteringindependent nature of the intrinsic AHE following a behavior $\rho_{yx} \propto \rho_{xx}^2$ [37]. The sign change of S_{yx} was found to be correlated with a sharp maximum in S_{xx} thus compensating this contribution to the transverse coefficient α_{yx} which did not change sign. In contrast, for Mn₅Si₃ the sign change occurs for S_{yx} and α_{yx} but not for S_{xx} . An analysis of the temperature dependence of α_{xy} based on the power law $\rho_{yx}^{AHE} = \lambda M_z \rho_{xx}^n$ [37] is not possible because λ of Mn₅Si₃ is strongly temperature dependent [16] in contrast to itinerant ferromagnets where it is usually temperature independent at low temperatures.

In the pyrochlore molybdate $R_2 Mo_2 O_7$ (R = Nd, Sm) with noncoplanar spin structure the variations of S_{xy} and α_{xy} were attributed to a contribution from the spin chirality of the system which was considered to be responsible for an enhanced AHE and a positive ANE at low temperatures [38]. A strong magnetic field reduces the amplitude of the spin chirality by aligning the Mn moments along the magnetic field direction leading to a reduced σ_{xy} and α_{xy} . It is interesting to note that this is observed only for R = Nd, Sm with non-coplanar spin structure and not for collinearly ordered Gd₂Mo₂O₇. In the present case, it is therefore conceivable that a similar behavior occurs due to a small change of the spin structure by moment reorientation and decrease of chirality/noncollinearity at small magnetic fields.

We only mention that for the Weyl semimetal $Co_3Sn_2S_2$ different behaviors of α_{yx} have been reported [39–41]. In these cases, however, S_{xy} did not change its sign with the temperature.

For Mn₅Si₃, maximum values $|S_{yx}(0)| = 0.05 \ \mu V K^{-1}$ and $|S_{yx}(H_{c1})| = 0.11 \ \mu V K^{-1}$ are reached at magnetizations $M_{\rm R}(0) = 0.028 \ \mu_{\rm B}/{\rm f.u.}$ and $M_{\rm R}(H_{c1}) = 0.17 \ \mu_{\rm B}/{\rm f.u.}$, respectively. Note that the former is a lower limit due to the thermal resistances between the sample holder and the single crystal which give rise to a lower applied thermal gradient in the crystal than the measured $\Delta T_{\rm x} = T_{\rm h} - T_{\rm c}$. Hence, an even larger $|S_{yx}|$ derived from the low magnetization is expected. Similar values $|S_{yx}| = 0.6 \,\mu \text{VK}^{-1}$ and $\mu_0 M = 1 \text{ mT}$ corresponding to $M = 0.01 \,\mu_{\text{B}}/\text{f.u.}$ have been reported for chiral Mn₃Sn [12]. Compared to ferromagnetic metals, $|S_{yx}|$ is strongly enhanced outside the broad range for which $|S_{yx}| \propto M$ is observed, similar to antiferromagnets with chiral magnetic order like Mn₃Sn [12, 14] and Mn₃Ge [13, 14].

Below $T_{\rm N1} = 60$ K, $\alpha_{yx}(H_{\rm c1})$ first increases with decreasing temperature together with a concomitant increase of $\Delta M(H_{\rm c1})$, eventually saturates and then decreases towards low temperatures. This is similar to the behavior of an itinerant ferromagnet and due to the dominant *T*-linear term in Eq. 4 after saturation of *M* [35]. In contrast, in the AF1 phase below $H_{\rm c1}$ the ANE strongly deviates from this behavior at temperatures below ≈ 25 K. We speculate that the reduction of $M_{\rm R}(0)$ and the simultaneous sign changes of $\alpha_{yx}(H_{\rm c1})$ and $S_{yx}(0)$ with temperature could arise from the different compensation of opposed Mn moments. In this respect it bears some similarity to the magnetization behavior of garnets or rare-earth transition-metal ferrimagnets below and above the compensation point.

B. Symmetry analysis

To gain further insights into the low-temperature behavior of Mn_5Si_3 , we analyze the symmetries of the anomalous Hall and Nernst effects under a small external magnetic field. The Onsager relations establish strong symmetry requirements for each response tensor. The (thermo-)electric responses measured in our experiments are approximately odd under the reversion of a small external magnetic field (Figs. 4 and 5). Up to second order, the only odd-in-field transverse electric (thermo-electric) responses are the intrinsic and quadratic anomalous Hall (Nernst) effects [42]. These response tensors are even under space inversion \mathcal{P} and odd under the combined time reversal and lattice translation symmetry $\mathcal{T}t$ [42, 43]. According to Neumann's principle, the transport coefficients must also be invariant under all the symmetries of the material. In the next paragraph, we combine the implications of the Onsager relations with Neumann's principle to investigate the symmetry constraints of the AHE and ANE in the antiferromagnetic phases AF1 and AF2 of Mn_5Si_3 (Fig. 2).

Consider the collinear AF2 phase shown in Fig. 2(a). The system is invariant under both \mathcal{P} and $\mathcal{T}t$. Because the response tensors are also invariant under \mathcal{P} , this symmetry operation does not impose any constraint. On the other hand, the $\mathcal{T}t$ invariance of the system imposes that the response coefficients be even under time reversal. Since the Onsager relations require the response tensors to be odd under \mathcal{T} , the intrinsic and quadratic anomalous Hall/Nernst effects are prohibited in the AF2 phase, in agreement with our experimental results for 60 K < T < 100 K [Figs. 4(h) and 5(e,g)] [16–18]. As mentioned above, the magnetic configurations of Mn₅Si₃

for T < 60 K are still under discussion [26]. The AF1 phases shown in Fig. 2(b) and Fig. 2(c) break \mathcal{P} but (as well as other proposals in the literature) are invariant under $\mathcal{T}t$, which allows for a p-wave non-relativistic spin splitting of the energy bands [44]. However, even though the bands are not spin-degenerate, the $\mathcal{T}t$ symmetry prohibits the anomalous responses. We conclude that, due to $\mathcal{T}t$ invariance, none of the proposed AF1 phases can explain our experimental signals. This suggests a slight tilting of the magnetic state for T < 60 K, which breaks the combined $\mathcal{T}t$ symmetry. Below T < 25 K, the reduction in the magnitude of the anomalous Hall conductivity and sign change of the anomalous Nernst conductivity hints to either a new phase or a weak rearrangement of the spins due to magnetic frustration or magnetic anisotropies, as pointed out by N. Biniskos et al. [26].

V. CONCLUSION

The anomalous Nernst effect of Mn_5Si_3 single crystals displays characteristic variations with magnetic field and temperature in agreement with the magnetic-field induced transitions between different antiferromagnetic phases. Detailed analysis of the low-temperature behavior below 25 K shows that the anomalous Nernst effect, anomalous Hall conductivity, and magnetization in low magnetic fields exhibit an unusual temperature dependence hinting a subtle modification of the magnetic structure in the AF1 phase. Furthermore, the experimentally observed Hall and Nernst effects in the noncollinear AF1 phase are in contrast to a symmetry analysis of the proposed magnetic AF1 structures, according to which these effects should disappear. These results should be taken into account in a refined model of the magnetic structure. While first ab initio calculations of the electronic band structure and Berry curvature have been performed for the collinear magnetic phase observed in thin films [30, 31], the behavior of the AHE and ANE in the noncollinear AF1 phase of Mn₅Si₃ at low temperatures is not yet fully understood and requires further investigation.

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Appendix A: Supplementary data

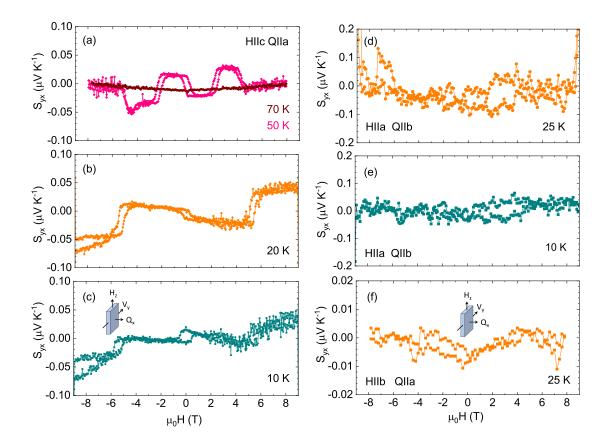


FIG. A.1. Anomalous Nernst effect of Mn_5Si_3 for magnetic fields H and heat flows Q applied along different crystallographic directions. (a-c) H along c, heat flow along a. (d-f) Measurements with H applied along the orthorhombic a or b direction. The measurements with heat flow along the a direction were obtained on a thin plate of 0.52 mm thickness along x.