Baryonic screening masses in QCD at high temperature

Leonardo Giusti^{a,b}, Tim Harris^c, Davide Laudicina^{a,b}, Michele Pepe^b, Pietro Rescigno^{a,b}

^aDepartment of Physics, University of Milano-Bicocca, Piazza della Scienza 3, 20126, Milano, Italy ^bINFN, sezione di Milano - Bicocca, Piazza della Scienza 3, 20126, Milano, Italy ^cInstitut fur Theoretische Physik, ETH Zurich, Wolfgang-Pauli-Str. 27, Zurich, 8093, Switzerland

Abstract

We compute the baryonic screening masses with nucleon quantum numbers and its negative parity partner in thermal QCD with $N_f = 3$ massless quarks for a wide range of temperatures, from $T \sim 1$ GeV up to ~ 160 GeV. The computation is performed by Monte Carlo simulations of lattice QCD with O(a)-improved Wilson fermions by exploiting a recently proposed strategy to study non-perturbatively QCD at very high temperature. Very large spatial extensions are considered in order to have negligible finite volume effects. For each temperature we have simulated 3 or 4 values of the lattice spacing, so as to perform the continuum limit extensional confidence at a few permille accuracy. The degeneracy of the positive and negative parity-state screening masses, as the exploration with confidence at a few permille accuracy. The degeneracy of the positive and negative parity partner in thermal QCD with form $T \sim 1$ GeV up to ~ 160 GeV. The restoration of chiral symmetry in the high temperature regime of QCD. In the entire range of temperatures explored, and cannot be explained by the expected leading behavior in the QCD coupling constant g over the entire range of temperatures, are a finite explained by the expected leading behavior in the QCD coupling constant g over the entire range of temperatures, the perturbative approach for studying the QCD dynamics is limited by the so-called infrared problem [1]. On the one hand, finding analytic solutions to overcome this problem is by itself the propersor of the perturbative proposed in Ref. [9]. Technically this is fessible because, at asymptotically large temperatures, the perturbative approach for studying the QCD over the last few years, it became possible to study thermal QCD were the last few years, it became possible to study thermal QCD were the last few years, it became possible to study thermal QCD were the last few years, it became possible to study thermal QCD were the last few years, it became possible to study thermal QCD were the last few years, it became p We compute the baryonic screening masses with nucleon quantum numbers and its negative parity partner in thermal QCD with $N_f = 3$ massless quarks for a wide range of temperatures, from $T \sim 1$ GeV up to ~ 160 GeV. The computation is performed by

doubt that the contributions which are computable in perturbation theory are not enough to explain the non-perturbative result up to temperatures of at least two orders of magnitude above the critical one [10, 8]. More recently the computation of the QCD mesonic screening masses showed that the known perturbative result cannot explain their values up to temperatures of the order of the electro-weak scale or so [9]. These results point straight to the fact that, for a reliable determination of the thermal properties of QCD, a fully non-perturbative treatment of the theory is required up to temperatures of the order of the electro-weak scale or so.

The purpose of this study is to perform the first non-

imation [13, 14] and in the full theory [15], have been restricted to very low temperatures and no extrapolation to the continuum limit has ever been performed, see Refs. [16, 17, 18] for more recent efforts on the subject.

This letter is organized as follows. In Section 2 we introduce the definition of nucleon screening masses, and we discuss how these quantities can probe chiral symmetry restoration. In Section 3 we briefly review the strategy that we have used to simulate QCD up to the electro-weak scale, and we give the definition of the baryonic correlation functions and screening masses on the lattice. In Section 4 the values of the screening masses in the continuum limit at all temperatures considered are

Preprint submitted to Elsevier May 8, 2024 given. In Section 5 we discuss our final results, and present our conclusions. Various technical details are discussed in several appendices.

2. Definition of baryonic screening masses

We are interested in the screening masses related to the fermion fields

$$N = \epsilon^{abc} \left(u^{aT} C \gamma_5 d^b \right) d^c , \quad \overline{N} = \overline{d}^e \left(\overline{d}^f C \gamma_5 \overline{u}^{gT} \right) \epsilon^{feg} , \quad (1)$$

where the transposition acts on spinor indices, latin letters indicate color indices, and $C = i\gamma_0\gamma_2$ is the charge-conjugation matrix. The contraction with the totally anti-symmetric tensor ϵ^{abc} guarantees that the nucleon field is a color singlet.

The two-point correlation functions we are interested in are

$$C_{N^{\pm}}(x_3) = \int dx_0 dx_1 dx_2 e^{-i\frac{x_0}{L_0}\pi} \langle \operatorname{Tr} \left[P_{\pm} N(x) \overline{N}(0) \right] \rangle , \qquad (2)$$

where $P_{\pm} = (1 \pm \gamma_3)/2$ are the projectors on positive (N^+) and negative (N^-) x_3 -parity states respectively, and the trace is over the free Dirac indices of the fermion fields in Eq. (1). The integral in Eq. (2) selects the component associated to the Matsubara frequency π/L_0 , which is the lowest one due to the antiperiodic boundary conditions of fermion fields in the compact direction of length L_0 . The screening masses are defined as

$$m_{N^{\pm}} = -\lim_{x_3 \to \infty} \frac{d}{dx_3} \ln \left[C_{N^{\pm}}(x_3) \right],$$
 (3)

and they characterize the exponential decay of the two-point correlation functions at large spatial distances.

The comparison of m_{N^+} with m_{N^-} provides a quantitative test of the restoration of chiral symmetry in the high temperature regime. Indeed when chiral symmetry is not spontaneously broken, the positive and negative parity correlation functions are equal up to a sign in the chiral limit, see Eq. (A.5) in Appendix A, and therefore $m_{N^+} = m_{N^-}$. This is at variance of the zero temperature case, where the screening masses m_{N^+} and m_{N^-} correspond to the chiral limit values of the nucleon and of the N(1535) masses. Due to the spontaneous breaking of chiral symmetry, they differ by several hundreds of MeV [19].

2.1. Shifted boundary conditions

In the rest of this letter, we define the thermal theory in a moving frame by requiring that the fields satisfy shifted boundary conditions in the compact direction [20, 21, 22], while we set periodic boundary conditions in the spatial directions. The former consist in shifting the fields by the spatial vector $L_0\xi$ when crossing the boundary of the compact direction, with the fermions having in addition the usual sign flip. For the gluon and the quark fields these boundary conditions read

$$A_{\mu}(x_{0} + L_{0}, \mathbf{x}) = A_{\mu}(x_{0}, \mathbf{x} - L_{0}\xi),$$

$$\psi(x_{0} + L_{0}, \mathbf{x}) = -\psi(x_{0}, \mathbf{x} - L_{0}\xi),$$

$$\overline{\psi}(x_{0} + L_{0}, \mathbf{x}) = -\overline{\psi}(x_{0}, \mathbf{x} - L_{0}\xi).$$
(4)

In the presence of shifted boundary conditions the periodic direction is identified by the vector $L_0(1, \xi)$. As a consequence, a relativistic thermal field theory in the presence of a shift ξ is equivalent to the very same theory with usual periodic (anti-periodic for fermions) boundary conditions but with a longer extension of the compact direction by a factor γ^{-1} = $\sqrt{1+\xi^2}$ [22], i.e. the standard relation between the temperature and the extension in the compact direction is modified as $T^{-1} = L_0/\gamma = L_0\sqrt{1+\xi^2}$. The momentum projection on the lowest Matsubara frequency has also to be modified accordingly. Thanks to the rotational symmetry of the theory, we can choose one of the axes to be in the direction of the shift, and restrict our discussion to the case $\xi = (\xi, 0, 0)$. If we define (x_0, x_1) the first two coordinates of a point in the system with temporal extent L_0 and shifted boundary conditions, and (x'_0, x'_1) the corresponding ones in the rotated system with temporal extent L_0/γ and periodic boundary conditions, the coordinates are mapped into each other by a Euclidean Lorentz transformation

$$\begin{cases} x'_0 = (x_0 + \xi x_1) \gamma \\ x'_1 = (x_1 - \xi x_0) \gamma . \end{cases}$$
 (5)

The projection of the baryonic correlation function on the first Matsubara frequency is then achieved by

$$C_{N^{\pm}}(x_3) = \int dx_0 dx_1 dx_2 e^{-i\frac{x_0 + \xi x_1}{L_0} \gamma^2 \pi} \langle \operatorname{Tr} \left[P_{\pm} N(x) \overline{N}(0) \right] \rangle , \quad (6)$$

where at variance with Eq. (2), the expectation value is computed in the presence of shifted boundary conditions¹.

3. Lattice strategy, correlation functions and screening masses

We compute the screening masses in QCD with $N_f = 3$ massless quarks² at the 12 temperatures T_0, \ldots, T_{11} given in Table 1, i.e. for T from about 1 GeV up to approximately 160 GeV.

We adopt shifted boundary conditions in the compact direction with $\xi = (1,0,0)$ and, in order to extrapolate the results to the continuum limit with confidence, several lattice spacings are simulated at each temperature with the extension of the compact direction being $L_0/a = 4,6,8,10$ while the length of the spatial directions is always L/a = 288. See Appendices A and B of Ref. [9] for the details on the lattice actions and for the bare parameters of the simulations.

The key idea for reaching very high temperatures on the lattice with a moderate computational effort is to determine lines of constant physics by fixing the value of a renormalized coupling defined non-perturbatively in a finite volume [8, 9]. The coupling can be computed precisely on the lattice for

¹We use the same notation for correlation functions with or without shifted boundary conditions since the precise meaning is clear from the context.

²Technically it is feasible to simulate massless quarks thanks to the large spectral gap πT induced by the temperature in the spectrum of the Dirac operator.

values of the renormalization scale μ which span several orders of magnitude [23, 24, 25]. To make a definite choice, we adopt the definition based on the Schrödinger functional (SF) [23] for the temperatures T_0, \ldots, T_8 and on the gradient flow (GF) [26, 24, 27] for T_9, T_{10} and T_{11} .

T	T(GeV)	$\frac{m_{N^+}}{3\pi T}$	$\frac{m_{N^+}-m_{N^-}}{3\pi T}$
T_0	165(6)	1.047(3)	0.0006(4)
T_1	82.3(2.8)	1.0544(19)	-0.0001(3)
T_2	51.4(1.7)	1.0569(28)	0.0002(3)
T_3	32.8(1.0)	1.0583(27)	0.0003(4)
T_4	20.6(6)	1.0596(28)	-0.0011(4)
T_5	12.8(4)	1.0662(28)	0.0001(4)
T_6	8.03(22)	1.068(3)	0.0001(6)
T_7	4.91(13)	1.075(4)	0.0004(9)
T_8	3.04(8)	1.077(4)	0.0003(9)
T_9	2.83(7)	1.076(4)	0.0009(12)
T_{10}	1.82(4)	1.089(4)	0.0007(20)
T_{11}	1.167(23)	1.078(6)	0.0016(15)

Table 1: Temperatures considered in this letter together with the best results for the nucleon mass, m_{N^+} , and the mass difference with its parity partner, $m_{N^+} - m_{N^-}$, in the continuum limit.

Once the coupling, e.g. $\bar{g}_{SF}^2(\mu)$, is known in the continuum limit for $\mu \sim T$ [24, 25], the theory is renormalized by fixing its value at fixed lattice spacing a to be

$$\bar{g}_{SF}^2(g_0^2, a\mu) = \bar{g}_{SF}^2(\mu) , \quad a\mu \ll 1 .$$
 (7)

This is the condition that fixes the so-called lines of constant physics, i.e. the dependence of the bare coupling constant g_0^2 on the lattice spacing, for values of a at which the scale μ and therefore the temperature T can be easily accommodated. In other words, at different temperatures we renormalize the theory by imposing the value of the renormalized coupling constant at different scales or equivalently we impose different renormalization conditions which, however, define the very same renormalized theory at all temperatures. As a consequence, at each T the theory can be simulated efficiently at various lattice spacings without suffering from large discretization errors, and the continuum limit of the observables can be taken with confidence. All technical details on how the renormalization procedure is implemented in practice are given in Appendices A and B of Ref. [9].

The lattice transcription of Eq. (6) for $\xi = (1, 0, 0)$, which is the relevant case to this study, reads³

$$C_{N^{\pm}}(x_{3}) = a^{3} \sum_{x_{0}, x_{1}, x_{2}} e^{-i\frac{x_{0} + x_{1}}{2L_{0}}\pi} \langle \operatorname{Tr} \left[P_{\pm} N(x) \overline{N}(0) \right] \rangle$$

$$= a^{3} \sum_{x_{0}, x_{1}, x_{2}} e^{-i\frac{x_{0} + x_{1}}{2L_{0}}\pi} \langle \left[W_{\pm}^{1} - W_{\pm}^{2} \right] \rangle , \qquad (8)$$

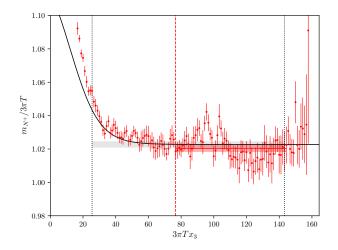


Figure 1: Plot of the effective mass $m_{N^+}(x_3)$, normalized to $3\pi T$, at the temperature T_1 for $L_0/a = 6$. For the explanation of the various fit curves and bands see the main text.

where the two terms in the second line are the Wick contractions obtained by integrating over the fermion fields. Their expressions read

$$W_{N^{\pm}}^{1} = \text{Tr} \left[S^{agT}(x,0)C\gamma_{5}S^{bf}(x,0)C\gamma_{5} \right] \text{Tr} \left[S^{ce}(x,0)P_{\pm} \right] \epsilon^{abc} \epsilon^{feg} ,$$

$$W_{N^{\pm}}^{2} = \text{Tr} \left[S^{agT}(x,0)C\gamma_{5}S^{be}(x,0)P_{\pm}S^{cf}(x,0)C\gamma_{5} \right] \epsilon^{abc} \epsilon^{feg} , \quad (9)$$

where S(x, y) is the quark propagator of the degenerate quarks. Once the correlators have been computed, the effective screening masses are defined as

$$m_{N^{\pm}}(x_3) = -\frac{1}{a} \ln \left[\frac{C_{N^{\pm}}(x_3 + a)}{C_{N^{\pm}}(x_3)} \right].$$
 (10)

As a representative example of the data, the nucleon effective mass is shown in Fig. 1 for T_1 and $L_0/a = 6$. In order to determine the value of the screening mass, we start by fitting the effective mass to a constant plus a correction deriving from the contamination of the first excited state (solid black line) from a minimum value up to the last point where we have a good signal (black dashed lines). The minimum value is chosen to have a good quality of the fit and to have, at the same time, a non vanishing contribution from the first excited state. On one hand, for the ensembles where the signal is good enough at a large distance, from this fit we estimate the minimum value x_3^{\min}/a (red dashed line) from which the excited state contamination is below the target statistical precision. The screening mass is then obtained by averaging the plateau (red band) from x_3^{\min}/a up to the last point where we have a good signal. On the other hand, for the lowest temperatures and for the ensembles corresponding to $L_0/a = 10$, where the loss of signal is more relevant at a large distance, the screening mass is directly estimated from the results of the effective mass fit (grey band).

Our best estimates of the screening masses are reported in Tables B.2 and B.3 of Appendix B for all the lattices simulated. The statistical error varies from a few permille to at most 5 permille for the smallest temperature. In order to profit from the correlations in our data for reducing the statistical errors,

³Even if the use of shifted boundary conditions is not crucial for the calculation of the screening masses, we have chosen to use them so as to share the cost of generating the gauge configurations with other projects [28, 29].

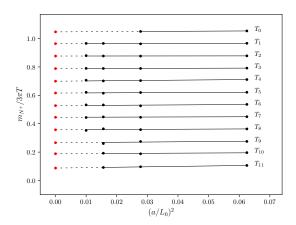


Figure 2: Numerical results for the tree-level improved nucleon screening mass at finite lattice spacing (black dots, error bars smaller than symbols). The lines in the panel represent the linear extrapolations in $(a/L_0)^2$ to the continuum limit. Each temperature is analyzed independently from the others. Data corresponding to T_i ($i=0,\ldots,11$) are shifted downward by $0.09\times i$ for better readability.

we also compute $(m_{N^+} - m_{N^-})/(3\pi T)$ and report its values in Tables B.2 and B.3 as well. This combination is particularly interesting because it is a measure of the chiral symmetry restoration which can be computed very precisely.

We have explicitly checked that finite volume effects are negligible within our statistical errors: we have generated three more lattices at the highest and at the lowest temperatures for the smallest spatial volumes corresponding to $L_0/a=6$, $L_0/a=10$, and $L_0/a=8$ for T_0 , T_1 , and T_{11} respectively. These lattices have the same dimensions in the compact and in the x_3 directions as those used to extract the results in Tables B.2 and B.3 but smaller extensions in the other two spatial directions. The screening masses computed on them are in agreement with those calculated on the larger volume, see Appendix B for details. Therefore we can safely assume that our results have negligible finite-volume effects within the statistical precision as expected by the theoretical analysis in Ref. [9].

4. Continuum limit of baryonic screening masses

The results that we have collected at finite lattice spacing have to be extrapolated to the continuum limit along lines of constant physics. For O(a)-improved actions, the Symanzik effective theory predicts the leading behaviour of the lattice artifacts to be of order a^2 . We can accelerate the convergence to the continuum by introducing the tree-level improved definitions

$$m_{N^{\pm}} \longrightarrow m_{N^{\pm}} - \left[m_{N^{\pm}}^{\text{free}} - 3\pi T \right],$$
 (11)

where $m_{N^{\pm}}^{\text{free}}$ is the mass in the free lattice theory. As shown in the Appendix D, where the computation is reported, the latter is the same for both the m_{N^+} and the m_{N^-} masses. From now on we will consider always the tree-level improved definition of the screening masses and indicate them with $m_{N^{\pm}}$.

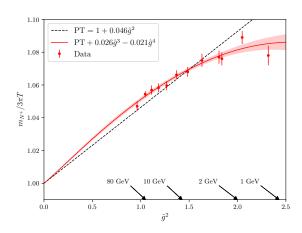


Figure 3: Nucleon screening mass versus \hat{g}^2 . The band represent the best fit to Eq. (14), while the dashed line is the analytically known contribution in Eq. 13.

All data for the improved nucleon screening mass are represented in Fig. 2 where, in order to improve the readability, data corresponding to T_i (i = 0, ..., 11) are shifted downward by $0.09 \times i$. At each temperature, lattice artifacts are well described by a single correction proportional to $(a/L_0)^2$. Indeed by fitting each data set linearly in $(a/L_0)^2$, the values of χ^2/dof are all around 1 with just a few outliers which, however, are not surprising given the large amount of data and fits. The results of the fits are shown in Fig. 2 as straight lines. For the mass difference $(m_{N^+} - m_{N^-})$, the coefficient of $(a/L_0)^2$ is found to be compatible with zero at all temperatures. We take the continuum limit values from these fits as our best results for the nucleon screening mass and for the difference $(m_{N^+} - m_{N^-})$. They are reported in Table 1 for all the 12 temperatures considered. As a further check of the extrapolations, we have fitted the data by excluding the coarsest lattice spacing, i.e. $L_0/a = 4$, for the temperatures T_1, \ldots, T_8 for which we have 4 data points. The intercepts are in excellent agreement with those of the previous fits, albeit with a slightly larger error. For the same sets of data, we have also attempted to include in the fit a $(a/L_0)^2 \ln(a/L_0)$ or a $(a/L_0)^3$ term. The resulting coefficients are compatible with zero. Given the high quality of the fits and of the data, it is not necessary to model the temperature dependence of the discretization effects so as to perform a global fit of the data.

5. Discussion and conclusions

The main results of this paper are the baryonic screening masses reported in Table 1. They have been computed in a wide temperature range starting from $T \sim 1$ GeV up to ~ 160 GeV or so with a precision of a few permille.

The first observation is that, as anticipated in section 3, within our rather small statistical errors we find an excellent agreement between m_{N^+} and m_{N^-} . This is a clear manifestation of the restoration of chiral symmetry occurring at high temperature in line with the analogous results for mesonic screening masses in Ref. [9]. For this reason in the following we discuss the nucleon mass m_{N^+} only.

A second observation is that the bulk of the nucleon screening mass is given by the free-theory value, $3\pi T$, plus 4-8% positive contribution over the entire range of temperatures explored.

To scrutinize in detail the temperature dependence induced by the non-trivial dynamics, we introduce the function $\hat{g}^2(T)$ defined as

$$\frac{1}{\hat{g}^2(T)} \equiv \frac{9}{8\pi^2} \ln \frac{2\pi T}{\Lambda_{\overline{\rm MS}}} + \frac{4}{9\pi^2} \ln \left(2 \ln \frac{2\pi T}{\Lambda_{\overline{\rm MS}}} \right) , \qquad (12)$$

where $\Lambda_{\overline{\rm MS}}=341$ MeV is taken from Ref. [30]. It corresponds to the 2-loop definition of the strong coupling constant in the $\overline{\rm MS}$ scheme at the renormalization scale $\mu=2\pi T$. For our purposes, however, this is just a function of the temperature T, suggested by the effective theory, that we use to analyze our results, see Ref. [9] for more details.

The screening masses versus $\hat{g}^2(T)$ are plotted in Fig. 3. The dashed line in this plot is the next-to-leading contribution to the nucleon screening mass which has been computed in the effective theory only very recently [31, 32]. For three massless quarks, the expression reads

$$\frac{m_{N^+}^{\text{nlo}}}{3\pi T} = 1 + 0.046g^2 \,, \tag{13}$$

where g is the QCD coupling constant. It is rather clear that from $T = T_0 \sim 160$ GeV down to $T = T_7 \sim 5$ GeV the perturbative expression is within half a percent or so with respect to the non-perturbative data. If a quick convergence of the perturbative series is assumed, this result would suggest that the bulk of the contribution due to the interactions is given by the $O(g^2)$ term. The full set of data, however, shows a distinct negative curvature which requires higher orders in \hat{g}^2 to be parameterized. We thus fit the values of m_{N^+} reported in the third column of Table 1 to a quartic polynomial in \hat{g} of the form

$$\frac{m_{N^+}}{3\pi T} = b_0 + b_2 \,\hat{g}^2 + b_3 \,\hat{g}^3 + b_4 \,\hat{g}^4 \,. \tag{14}$$

The intercept b_0 turns out to be compatible with 1, as predicted by the free theory, within a large error. We thus enforce it to be the free-theory value, $b_0 = 1$, and we fit the data again. The coefficient of the \hat{g}^2 term turns out to be compatible with the theoretical expectation in Eq. 13 within again a large uncertainty. We have thus fixed also this coefficient to its analytical value, $b_2 = 0.046$, and we have performed again the quartic fit of the form in Eq. 14. As a result, we obtain $b_3 = 0.026(4)$, $b_4 = -0.021(3)$ and $\cos(b_3, b_4)/[\sigma(b_3)\sigma(b_4)] = -0.99$ with $\chi^2/\text{dof} = 0.64$. This is indeed the best parameterization of our results over the entire range of temperatures explored.

For completeness, we notice that if the cubic coefficient is enforced to vanish, i.e. $b_3=0$, the fit returns $b_2=0.062(3)$, $b_4=-0.011(2)$ and $\cos(b_2,b_4)/[\sigma(b_2)\sigma(b_4)]=-0.97$ with again an excellent value of $\chi^2/\mathrm{dof}=0.68$. The coefficient b_2 , however, turns out to be in disagreement with the analytic determination. Data can also be fit to the function in Eq. 14 with $b_0=1$ and $b_4=0$ but again the coefficient b_2 would be in disagreement with the perturbative result.

Finally we observe that it has been possible to reach a precision on the nucleon screening mass of a few permille because, at asymptotically large temperatures, baryonic correlators do not suffer from the exponential depletion of the signal-to-noise ratio

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Appendix A. Ward Identity in the continuum

Under the infinitesimal axial non-singlet transformation

$$\delta\psi(x) = i\epsilon\sigma_3\gamma_5\psi(x), \quad \delta\overline{\psi}(x) = i\epsilon\overline{\psi}(x)\gamma_5\sigma_3,$$
 (A.1)

with $\overline{\psi} = (\overline{u}, \overline{d})$ and analogously for ψ and where σ_3 is the third Pauli matrix acting on the flavour index, the nucleon fields in Eq. (1) transform as

$$\delta N(x) = -i\epsilon \gamma_5 N(x) , \quad \delta \overline{N}(x) = -i\epsilon \overline{N}(x) \gamma_5 .$$
 (A.2)

If we consider the composite field

$$O(x,0) = i \operatorname{Tr} \left[\gamma_5 P_{\pm} N(x) \overline{N}(0) \right], \qquad (A.3)$$

then

$$\delta O(x,0) = \epsilon \operatorname{Tr} \left[P_{\pm} N(x) \overline{N}(0) \right] + \epsilon \operatorname{Tr} \left[P_{\mp} N(x) \overline{N}(0) \right] \ . \tag{A.4}$$

In the chiral limit, and if the symmetry is not spontaneously broken, it holds $\langle \delta O(x,0) \rangle = 0$ which in turn implies, see for instance [33] for a recent derivation,

$$\langle \operatorname{Tr} \left[P_+ N(x) \overline{N}(0) \right] \rangle \, = \, - \langle \operatorname{Tr} \left[P_- N(x) \overline{N}(0) \right] \rangle \; . \tag{A.5}$$

Appendix B. Simulation details and lattice results

We have simulated three-flavour QCD as described in Appendix E of Ref. [9]. We have accumulated a certain number of configurations for the computation of the EoS [29]. Among those, we have selected some that we have used for the computation of the screening masses. In particular in Tables B.2 and

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$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	T	L_0/a	n .	n		$\underline{m_{N^+}-m_{N^-}}$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			mau	nsrc	$3\pi T$	$3\pi T$
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	T_0	4	300	4	0.9863(15)	0.0002(3)
$T_1 \begin{vmatrix} 6 & 310 & 4 & 1.0204(20) & 0.0002(4) \\ 8 & 500 & 4 & 1.0371(18) & -0.00013(23) \\ 10 & 500 & 4 & 1.0438(28) & 0.0003(5) \\ 4 & 300 & 4 & 0.9909(23) & 0.0001(4) \\ T_2 & 8 & 490 & 4 & 1.0385(30) & 0.00026(29) \\ 10 & 500 & 4 & 1.048(5) & 0.0005(6) \\ 4 & 300 & 4 & 0.9945(25) & 0.0006(4) \\ T_3 & 6 & 340 & 4 & 1.027(3) & 0.0002(4) \\ T_3 & 8 & 490 & 4 & 1.048(6) & 0.0003(7) \\ 4 & 440 & 4 & 1.048(6) & 0.0003(7) \\ T_4 & 6 & 310 & 4 & 1.0317(26) & -0.0007(4) \\ 10 & 500 & 4 & 1.0430(29) & -0.0001(4) \\ 10 & 500 & 4 & 1.054(5) & -0.0013(6) \\ T_5 & 6 & 310 & 4 & 1.038(3) & 0.0005(8) \\ 4 & 310 & 4 & 1.004(3) & -0.0007(6) \\ T_5 & 6 & 310 & 4 & 1.038(3) & 0.0005(8) \\ T_6 & 6 & 320 & 4 & 1.0466(26) & -0.0001(3) \\ 10 & 500 & 4 & 1.059(4) & -0.0001(5) \\ T_6 & 8 & 500 & 4 & 1.059(4) & -0.0002(7) \\ T_6 & 8 & 500 & 4 & 1.054(4) & -0.0002(7) \\ T_7 & 6 & 310 & 4 & 1.004(4) & 0.0005(12) \\ T_7 & 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ T_7 & 8 & 500 & 4 & 1.043(4) & 0.0006(7) \\ T_7 & 8 & 500 & 4 & 1.046(4) & -0.0001(8) \\ 10 & 500 & 4 & 1.059(3) & -0.0001(8) \\ 10 & 500 & 4 & 1.062(6) & 0.0026(17) \\ 4 & 320 & 8 & 1.016(4) & 0.0023(14) \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0001(11) \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0001(11) \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0007(8) \\ \hline \end{tabular}$		6	390	4	` ′	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		4	300	4	0.9892(18)	0.0001(3)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	T	6	310	4	1.0204(20)	0.0002(4)
$T_2 = \begin{cases} 4 & 300 & 4 & 0.9909(23) & 0.0001(4) \\ 6 & 320 & 4 & 1.0242(24) & -0.00017(28) \\ 8 & 490 & 4 & 1.0385(30) & 0.00026(29) \\ 10 & 500 & 4 & 1.048(5) & 0.0005(6) \\ \hline \\ T_3 = \begin{cases} 6 & 340 & 4 & 1.027(3) & 0.0002(4) \\ 4 & 300 & 4 & 1.027(3) & 0.0002(4) \\ 10 & 500 & 4 & 1.048(6) & 0.0003(7) \\ \hline \\ T_4 = \begin{cases} 6 & 310 & 4 & 1.044(6) & 0.0007(5) \\ 310 & 4 & 1.0317(26) & -0.0007(4) \\ 10 & 500 & 4 & 1.0430(29) & -0.0001(4) \\ 10 & 500 & 4 & 1.034(3) & -0.0007(6) \\ \hline \\ T_5 = \begin{cases} 6 & 310 & 4 & 1.034(3) & -0.0007(6) \\ 310 & 4 & 1.034(3) & -0.0007(6) \\ \hline \\ T_6 = \begin{cases} 6 & 310 & 4 & 1.034(3) & -0.0001(5) \\ \hline \\ 8 & 500 & 4 & 1.059(4) & -0.0001(5) \\ \hline \\ T_6 = \begin{cases} 6 & 320 & 4 & 1.034(3) & -0.0002(7) \\ 8 & 500 & 4 & 1.054(4) & -0.0002(7) \\ \hline \\ 10 & 500 & 4 & 1.054(4) & -0.0002(5) \\ \hline \\ 10 & 500 & 4 & 1.059(3) & -0.0001(8) \\ \hline \\ T_7 = \begin{cases} 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ 8 & 500 & 4 & 1.059(3) & -0.0001(8) \\ \hline \\ 10 & 500 & 4 & 1.059(3) & -0.0001(8) \\ \hline \\ 10 & 500 & 4 & 1.059(3) & -0.0001(8) \\ \hline \\ 10 & 500 & 4 & 1.062(6) & 0.0023(14) \\ \hline \\ T_8 = \begin{cases} 6 & 300 & 8 & 1.046(4) & -0.0001(11) \\ -0.0007(8) & -0.0001(11) \\ \hline \\ T_8 = \begin{cases} 6 & 300 & 8 & 1.046(4) & -0.0001(11) \\ -0.0007(8) & -0.0007(8) \\ \hline \end{cases}$	<i>I</i> 1	8	500	4	1.0371(18)	-0.00013(23)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		10	500	4	1.0438(28)	0.0003(5)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		4	300	4	0.9909(23)	0.0001(4)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	T	6	320	4	1.0242(24)	-0.00017(28)
$T_3 = \begin{cases} 4 & 300 & 4 & 0.9945(25) & 0.0006(4) \\ 340 & 4 & 1.027(3) & 0.0002(4) \\ 8 & 490 & 4 & 1.0406(23) & 0.0005(3) \\ 10 & 500 & 4 & 1.048(6) & 0.0003(7) \\ \hline \\ 4 & 440 & 4 & 1.0040(16) & 0.0007(5) \\ 6 & 310 & 4 & 1.0317(26) & -0.0007(4) \\ 10 & 500 & 4 & 1.0430(29) & -0.0001(4) \\ 10 & 500 & 4 & 1.054(5) & -0.0013(6) \\ \hline \\ T_5 = \begin{cases} 6 & 310 & 4 & 1.004(3) & -0.0007(6) \\ 310 & 4 & 1.038(3) & 0.0005(8) \\ 8 & 500 & 4 & 1.0466(26) & -0.0001(3) \\ 10 & 500 & 4 & 1.059(4) & -0.0001(5) \\ \hline \\ T_6 = \begin{cases} 6 & 320 & 4 & 1.034(3) & -0.0002(7) \\ 8 & 500 & 4 & 1.054(4) & -0.0002(5) \\ 10 & 500 & 4 & 1.054(4) & -0.0002(5) \\ 10 & 500 & 4 & 1.043(4) & 0.0006(7) \\ \hline \\ T_7 = \begin{cases} 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ 8 & 500 & 4 & 1.059(3) & -0.0001(8) \\ 10 & 500 & 4 & 1.062(6) & 0.0023(14) \\ \hline \\ T_8 = \begin{cases} 6 & 300 & 8 & 1.016(4) & 0.0023(14) \\ 8 & 500 & 4 & 1.066(4) & -0.0007(8) \\ \hline \end{cases}$	12	8	490	4	1.0385(30)	0.00026(29)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		10	500	4	1.048(5)	0.0005(6)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		4	300	4	0.9945(25)	0.0006(4)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		6	340	4	1.027(3)	0.0002(4)
$T_4 = \begin{cases} 4 & 440 & 4 & 1.0040(16) & 0.0007(5) \\ 6 & 310 & 4 & 1.0317(26) & -0.0007(4) \\ 8 & 490 & 4 & 1.0430(29) & -0.0001(4) \\ 10 & 500 & 4 & 1.054(5) & -0.0013(6) \\ \hline T_5 = \begin{cases} 6 & 310 & 4 & 1.004(3) & -0.0007(6) \\ 8 & 500 & 4 & 1.0466(26) & -0.0001(3) \\ 10 & 500 & 4 & 1.0466(26) & -0.0001(5) \\ \hline T_6 = \begin{cases} 6 & 320 & 4 & 1.0089(25) & -0.0002(7) \\ 8 & 500 & 4 & 1.0089(25) & -0.0002(7) \\ 8 & 500 & 4 & 1.054(4) & -0.0002(5) \\ 10 & 500 & 4 & 1.061(6) & 0.0004(10) \\ \hline T_7 = \begin{cases} 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ 8 & 500 & 4 & 1.059(3) & -0.0001(8) \\ 10 & 500 & 4 & 1.062(6) & 0.0023(14) \\ \hline T_8 = \begin{cases} 6 & 300 & 8 & 1.016(4) & 0.0023(14) \\ 8 & 500 & 4 & 1.066(4) & -0.0007(8) \\ \hline \end{cases}$	T_3	8	490	4	1.0406(23)	0.0005(3)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$		10	500	4	1.048(6)	0.0003(7)
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	T	4	440	4	1.0040(16)	0.0007(5)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		6	310	4	1.0317(26)	-0.0007(4)
$T_5 \begin{vmatrix} 4 & 310 & 4 & 1.004(3) & -0.0007(6) \\ 6 & 310 & 4 & 1.038(3) & 0.0005(8) \\ 8 & 500 & 4 & 1.0466(26) & -0.0001(3) \\ 10 & 500 & 4 & 1.059(4) & -0.0001(5) \\ 4 & 300 & 4 & 1.0089(25) & -0.0006(9) \\ 6 & 320 & 4 & 1.034(3) & -0.0002(7) \\ 10 & 500 & 4 & 1.054(4) & -0.0002(5) \\ 10 & 500 & 4 & 1.061(6) & 0.0004(10) \\ T_7 & 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ 4 & 320 & 4 & 1.043(4) & 0.0006(7) \\ T_7 & 8 & 500 & 4 & 1.059(3) & -0.0001(8) \\ 10 & 500 & 4 & 1.062(6) & 0.0023(14) \\ T_8 & 6 & 300 & 8 & 1.016(4) & 0.0023(14) \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0007(8) \\ \end{tabular}$	14	8	490	4	1.0430(29)	-0.0001(4)
$T_5 \begin{vmatrix} 6 & 310 & 4 & 1.038(3) & 0.0005(8) \\ 8 & 500 & 4 & 1.0466(26) & -0.0001(3) \\ 10 & 500 & 4 & 1.059(4) & -0.0001(5) \\ \hline \\ A & 300 & 4 & 1.0089(25) & -0.0006(9) \\ 6 & 320 & 4 & 1.034(3) & -0.0002(7) \\ 10 & 500 & 4 & 1.054(4) & -0.0002(5) \\ 10 & 500 & 4 & 1.061(6) & 0.0004(10) \\ \hline \\ T_7 & 6 & 310 & 4 & 1.012(4) & 0.0005(12) \\ T_7 & 6 & 310 & 4 & 1.043(4) & 0.0006(7) \\ 8 & 500 & 4 & 1.059(3) & -0.0001(8) \\ 10 & 500 & 4 & 1.062(6) & 0.0023(14) \\ T_8 & 6 & 300 & 8 & 1.016(4) & 0.0023(14) \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0001(11) \\ \hline \\ T_8 & 8 & 500 & 4 & 1.066(4) & -0.0007(8) \\ \hline \end{tabular}$		10	500	4	1.054(5)	-0.0013(6)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		4	310	4	1.004(3)	-0.0007(6)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		6	310	4	1.038(3)	0.0005(8)
$T_6 \begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	15	8	500	4	1.0466(26)	-0.0001(3)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		10	500	4	1.059(4)	-0.0001(5)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		4	300	4	1.0089(25)	-0.0006(9)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		6	320	4	1.034(3)	-0.0002(7)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	16	8	500	4	1.054(4)	-0.0002(5)
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		10	500	4	1.061(6)	0.0004(10)
T_7 8 500 4 1.059(3) -0.0001(8) 10 500 4 1.062(6) 0.0026(17) 4 320 8 1.016(4) 0.0023(14) T_8 6 300 8 1.046(4) -0.0001(11) 8 500 4 1.066(4) -0.0007(8)		4	320	4	1.012(4)	0.0005(12)
8 500 4 1.059(3) -0.0001(8) 10 500 4 1.062(6) 0.0026(17) 4 320 8 1.016(4) 0.0023(14) 6 300 8 1.046(4) -0.0001(11) 8 500 4 1.066(4) -0.0007(8)	T_7	6	310	4	1.043(4)	0.0006(7)
4 320 8 1.016(4) 0.0023(14) 6 300 8 1.046(4) -0.0001(11) 8 500 4 1.066(4) -0.0007(8)		8	500	l	1.059(3)	-0.0001(8)
$egin{array}{ c c c c c c c c c c c c c c c c c c c$		10	500	4	1.062(6)	0.0026(17)
18 8 500 4 1.066(4) -0.0007(8)	T_8	4	320	8	1.016(4)	
18 8 500 4 1.066(4) -0.0007(8)		6	300	8	1.046(4)	-0.0001(11)
10 500 5 1.061(4) 0.0013(13)		8	500	I	1.066(4)	
		10	500	5	1.061(4)	0.0013(13)

Table B.2: Results for the nucleon screening mass, m_{N^+} , and the mass difference with its parity partner, $(m_{N^+} - m_{N^-})$, normalized to $3\pi T$ at finite lattice spacing for the temperatures T_0, \ldots, T_8 . The number of molecular dynamic units (MDUs) generated, $n_{\rm mdu}$, and the number of local sources per configuration on which the two-point correlation functions have been computed, $n_{\rm nsrc}$, are also reported. The latter are always calculated by skipping $n_{\rm skip} = 10$ MDUs between two consecutive measurements.

B.3 we report the number of MDUs considered and the number of local sources per configuration on which the two-point correlation functions have been computed. For each configuration, the best estimates of $C_{N^\pm}(x_3)$ in Eq. (8) have been obtained by properly averaging their values from all local sources. The screening masses have then been extracted as described in Section 3. The results are reported in Tables B.2 and B.3 for the 9 highest temperatures T_0, \ldots, T_8 and for the lowest ones, T_9, T_{10} and T_{11} respectively.

To explicitly check that finite volume effects are negligible within our statistical errors, we have generated three more lat-

T	L_0/a	$n_{ m mdu}$	$n_{ m nsrc}$	$\frac{m_{N^+}}{3\pi T}$	$\frac{m_{N^+}-m_{N^-}}{3\pi T}$
	4	400	4	1.0180(26)	-0.0008(12)
T_9	6	390	4	1.0526(28)	0.0005(10)
	8	390	4	1.052(5)	0.0002(10)
	4	410	4	1.029(4)	-0.0019(21)
T_{10}	6	400	4	1.056(3)	-0.0021(14)
	8	390	4	1.074(3)	0.0013(17)
	4	400	4	1.029(4)	0.0001(21)
T_{11}	6	390	4	1.055(6)	-0.0015(17)
	8	390	4	1.063(5)	0.0016(11)

Table B.3: As in Table B.2 but for T_9 , T_{10} and T_{11} .

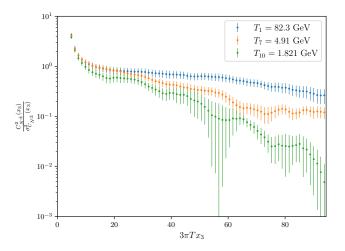


Figure C.4: Signal-to-noise ratio squared at $T = T_1$, T_7 and T_{10} for $L_0/a = 6$.

tices at T_0 ($L_0/a = 6$), T_1 ($L_0/a = 10$) and T_{11} ($L_0/a = 8$) at three smaller spatial volumes, namely $6 \times 144^2 \times 288$, $10 \times 120^2 \times 288$, and $8 \times 144^2 \times 288$ (direction 3 the longest) respectively. On these lattices we have computed the screening masses. They turn out to be in very good agreement with the analogous ones reported in Tables B.2 and B.3, and therefore they confirm the theoretical expectations that finite volume effects are negligible.

Appendix C. Signal-to-noise ratio for baryon correlation functions at finite temperature

The signal-to-noise ratio squared of baryonic correlation functions goes as

$$\frac{C_{N^{\pm}}^{2}(x_{3})}{\sigma_{C_{N^{\pm}}}^{2}(x_{3})} \propto \exp\{-(2m_{N^{\pm}} - 3m_{P})x_{3}\} + \dots$$
 (C.1)

where $\sigma_{C_{N^{\pm}}}^2(x_3)$ is the variance of $C_{N^{\pm}}$ and the ... stand for sub-leading exponential contributions. At asymptotically large temperatures, and up to discretization errors, $m_{N^{\pm}} \to 3\pi T$ and $m_P \to 2\pi T$. As a consequence no exponential depletion of the

signal-to-noise ratio with x_3 is expected when $T \to \infty$. This is at variance of what happens for $T \to 0$, where there is a severe exponential degradation of the signal-to-noise ratio because, for instance, $(2m_{N^+} - 3m_P) \to (2m_N - 3m_\pi)$ with m_N and m_π being the nucleon and the pion masses.

In Fig. C.4 it is shown the signal-to-noise ratio squared for C_{N^+} as a function of $(3\pi T x_3)$ for 3 temperatures considered in this letter. As expected the depletion of the signal-to-noise ratio with x_3 becomes more severe when the temperature is lowered, and the estimate of the correlation function becomes noisier. Similar considerations apply to C_{N^-} .

Appendix D. Baryonic screening masses in the free lattice theory

In order to accelerate the extrapolation to the continuum limit, we have computed the baryonic screening masses in the free theory on the lattice. In the infinite spatial volume limit, the baryonic correlation functions can be written in the form

$$C_{N^{\pm}}(x_3) = \pm \sum_{p_0, q_0} \int dp_1 dp_2 dq_1 dq_2 \mathcal{M}(p, q) e^{-2\Omega(p, q, k)x_3}, \quad (D.1)$$

where for shift vectors of the form $\boldsymbol{\xi} = (\xi, 0, 0)$

$$p_0 = (2n_0 + 1)\frac{\pi}{L_0} - p_1 \xi$$
, $n_0 = 0, \dots, L_0/a - 1$, (D.2)

analogously for q_0 , and the spatial momenta are $p_k \in [-\pi/a, \pi/a)$. The function $\Omega(p, q, k)$ is given by

$$\Omega(p,q,k) = \hat{\omega}(p) + \hat{\omega}(q) + \hat{\omega}(k)$$
 (D.3)

where $\hat{\omega}$ encodes each quark line contribution to the screening correlator as defined in Appendix F in Ref. [9], while the matrix $\mathcal{M}(p,q)$ is a calculable function of the momenta which does not play a rôle in the computation of the baryonic screening mass. For the lowest Matsubara frequency and for shift vectors of the form $\boldsymbol{\xi} = (\xi,0,0)$, the energy-momentum conservation implies

$$\begin{cases} p_0 + q_0 + k_0 &= \frac{\pi}{L_0} \gamma^2 \\ p_1 + q_1 + k_1 &= \frac{\pi}{L_0} \xi \gamma^2 \\ p_2 + q_2 + k_2 &= 0 \end{cases}$$
 (D.4)

The screening mass is obtained by minimizing $\Omega(p,q,k)$ with respect to the momenta. For the shift vector $\boldsymbol{\xi}=(1,0,0)$, the minimum is attained at

$$p = q = \frac{\pi}{2L_0}(1, 1, 0)$$
, $k = \frac{\pi}{2L_0}(-1, -1, 0)$. (D.5)

Notice that, since $\hat{\omega}$ is an even function of the momenta, each quark line gives the same contribution to Ω . In Table D.4 we list the value of the screening mass normalized to $3\pi T$ for the temporal extents relevant to this work.

L_0/a	$m_{N^{\pm}}^{\mathrm{free}}/3\pi T$
4	0.932614077
6	0.967811412
8	0.981401809
10	0.987944825

Table D.4: Tree-level values of the baryonic screening mass on lattices with temporal extent L_0/a , infinite spatial volume and shift vector $\boldsymbol{\xi} = (1,0,0)$

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